

# Forging of Advanced Disk Alloy LSHR

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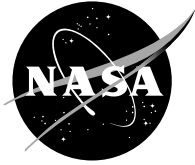
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## Introduction

The powder metallurgy disk alloy LSHR was designed with a relatively low  $\gamma'$  solvus temperature and high refractory element content to allow versatile heat treatment processing combined with high tensile, creep and fatigue properties (ref. 1). When processed to produce microstructures with fine grains near 10  $\mu\text{m}$  in diameter, the alloy can exhibit high tensile strength, creep resistance, and fatigue resistance at temperatures up to 650 °C. When alternatively processed to produce microstructures with coarser grains near 50  $\mu\text{m}$  in diameter, the alloy can exhibit high tensile strength, creep resistance, and fatigue crack propagation resistance to temperatures exceeding 700 °C. Grain size is predominantly controlled by the solution heat treatment temperature in relationship to the  $\gamma'$  solvus temperature (ref. 2). “Subsolvus” solution heat treatments below the solvus temperature allow coarse remnant “primary”  $\gamma'$  particles 1 to 5  $\mu\text{m}$  in diameter to remain and constrain grain growth. “Supersolvus” solution heat treatments above the solvus temperature dissolves the coarse remnant “primary”  $\gamma'$  particles, and grains can grow significantly larger.

However, forging process conditions can also significantly affect solution heat treatment-grain size response. Forging process conditions influence the as-forged grain size of the microstructure. Furthermore, the forging process conditions also introduce varying amounts of dislocations and associated internal energy within the microstructure, which drives grain growth during solution heat treatments (ref. 3). Therefore, it is necessary to understand the relationships between forging process conditions and the eventual grain size of solution heat treated material. This would allow selection of appropriate forging conditions having sufficient tolerances for production processes, in order to produce uniform fine grain and coarse grain microstructures. This is especially important for low cycle fatigue resistance, where fatigue life can be sensitive to both mean and as-large-as (ALA) grain size (refs. 4 and 7).

The objective of this study was to perform forging and heat treatment experiments (“thermomechanical processing” or “TMP” experiments) on small compression test specimens of extruded LSHR material, in order to identify viable forging process conditions allowing uniform fine grain and coarse grain microstructures after the appropriate heat treatments. Selected forging conditions could then be applied to a production-size forging.

## Material and Procedure

Specimen machining, testing, and heat treatments were performed by Wyman-Gordon Forgings, Houston, Texas. A 28 mm thick cross-section of a 15.3 cm diameter extrusion was removed using an abrasive disk saw. Specimen blanks were then electrodischarge machined along a 7.6 cm diameter circle centered in the cross section. Fifteen right circular cylinder (RCC) specimens having a diameter

of 12.3 mm and length of 19 mm were then machined. RCC specimens have fairly uniform strain and strain rate as a function of location within the specimen interior when compression tested. Two double cone (DC) specimens were also machined according to figure 1 (ref. 4). DC specimens have varying strains and strain rates as a function of interior location when compression tested. The matrix of test conditions for the RCC and DC specimens is illustrated in figure 2. RCC specimens were tested at three temperatures of 1050, 1080, and 1110 °C using 3 strain rates of 0.0003, 0.003, and 0.03 sec<sup>-1</sup>, after being presoaked at the test temperature for times of 1 to 8 h. This design of experiments (DOE) represents a central composite statistical test matrix, but includes no repeats of the center point. All RCC tests were continued to an upset of at least 50 percent, and true strain of 0.70. DC specimens were tested at 1080 °C and two extreme approximate strain rates of 0.0003 and 0.03 sec<sup>-1</sup> after a 3h presoak. All DC tests were also continued to an upset of 50 percent.

After the tests, all specimens were sliced into four quarters. Single quarters of each specimen were heat treated together on a tray in a resistance heated furnace using subsolvus heat treatments of 1135 °C for 1 and 4h. Second quarters were given simple supersolvus heat treatments of 1171 °C for 1 and 4 h. Third quarters were give a compound heat treatment consisting of a subsolvus solution heat treatment of 1135 °C/1h, followed by supersolvus treatments of 1171 °C for 1 and 4h. Heat treated and as-forged quarters were then sectioned, metallographically prepared, and swab etched using Kallings reagent. Five fields near the center of the forging specimen were measured to determine mean grain size (G) in each case, using a circular overlay grid according to ASTM E112. The largest grain observed on each metallographic section was measured for ALA grain size according to ASTM E930. Statistical evaluations of flow stress and grain sizes were then performed. Controlled variables were orthogonally scaled to standardized form in all cases, using the relationship  $v_i' = (v_i - v_{mid}) / (0.5 * (v_{max} - v_{min}))$ . This produced a range for each standardized variable of -1 to +1, and gave standardized variables for temperature (T'), log presoak time (log(P')), log strain rate (log(R')), and log solution time (log(S')) of:

$$\begin{aligned} T' &= (T - 1080)/30 \\ \log(P)' &= (\log(P) - 4.5)/3.5 \\ \log(R)' &= (\log(R) + 2.523)/1 \\ \log(S)' &= (\log(S) - 2.5)/1.5 \end{aligned}$$

Regression model equations were derived by comparing the results of both forward and reverse stepwise term selection, with a 90 percent probability of significance required for term inclusion. After model selection, analysis of variance and residuals were examined to assess goodness of fit and normality. The effect of each significant variable on the response after adjustment for other variables (“adjusted effects”) was then directly assessed. Finally, predicted responses and confidence intervals were also examined for each response at centerpoint and extreme variable values.

## Results and Discussion

### Forging Stress-Strain Response

Typical engineering stress-strain curves are shown for RCC tests, and load-displacement curves for DC tests are shown in figures 3 to 6. Stress at a given strain clearly increased with increasing strain rate and presoak temperature, and decreased with increasing temperature. Flow stress at a true strain of 0.5 for each RCC test was employed for regression analyses. Plots of this flow stress (S) vs. log (strain rate) are shown for the various test temperatures and presoak times in figure 7. A strong dependence of flow stress with strain rate and temperature is obvious. Reverse stepwise selection linear regression of log (stress) on temperature, log (presoak time), log (strain rate), and their interactive products were performed. The resulting linear regression equation was:

$$\log(\text{stress}) = 1.595152 - 0.08334T' + 0.056251\log(P)' + 0.431000\log(R)', \quad (1)$$

with a correlation coefficient  $R^2_{\text{adj}} = 0.9759$  and rms error = 0.05867. The complete statistical output is included in appendix A-1. This equation indicated flow stress moderately decreased with increasing temperature, strongly increased with increasing strain rate, and moderately increased with increasing presoak time for the range of conditions investigated. This result is favorable for producibility, as average and local strain rate can be well-controlled and modeled in modern isothermal forging operations, while small variations in the actual presoak time and temperature of each forging would be permissible without large influence on flow stress. A plot of the predicted and actual flow stress indicated very good agreement, figure 8.

It is highly preferable that the alloy exhibit superplastic flow during a forging process. This allows complete flow of the material into all forging die cavities with uniform strain and strain rates in the disk, while minimizing the buildup of stresses in the dies. Superplastic flow is present when a material exhibits high strain rate sensitivity ( $m$ ), as usually defined by the relationship  $\sigma = K(d\varepsilon/dt)^m$ . A material is considered superplastic in deformation conditions where a strain rate sensitivity  $m$  of at least 0.3 is observed. The strain rate sensitivity  $m$  was evaluated by fitting linear regression equations to the  $\log(\text{stress})$  data as a function of  $\log(\text{strain rate})$  at constant temperatures and presoak times, according to the equation:

$$\log(\sigma) = \log K + m \log(d\varepsilon/dt) \quad (2)$$

The resulting plot and equations are shown in figure 9. The strain rate sensitivity  $m$  was defined by the slope of each line and remained well above 0.3 for all conditions. The material therefore exhibited superplastic flow for the evaluated conditions.

## Grain Size Response

**1. As-Forged.**—Images of the typical microstructures observed for all specimens in the as-forged state are compared in figures 10 to 12, and suggest only minor variations in grain size with forging conditions. The images are arranged as isotherms of the DOE in order to indicate the prior forging temperatures, strain rates, and presoak times. The macrostructures of as-forged RCC and DC specimens appeared uniform in all cases. Mean grain size at the center of DC specimens in figure 13 appeared comparable to that of RCC specimens tested at the equivalent approximated strain and strain rate conditions. Plots of as-forged mean grain size (AFG) versus  $\log(\text{strain rate})$  at various temperatures ( $T$ ) and presoak times ( $P$ ) of the RCC specimens are shown in figure 14. Mean grain size number appeared to moderately decrease with increasing temperature. Stepwise linear regression of mean ASTM grain size number on temperature,  $\log(\text{presoak time})$ ,  $\log(\text{strain rate})$ , and their interactive products was performed. The resulting linear regression equation indicated as-forged grain size number (AFG) only significantly decreased with increasing temperature for the range of conditions investigated, according to the equation:

$$\text{AFG} = 12.1 - 0.39 T', \quad (3)$$

with a correlation coefficient  $R^2_{\text{adj}} = 0.3938$  and rms error = 0.3882. The complete statistical output is given in appendix A-2. A plot of the predicted and actual mean grain size indicated reasonable agreement, figure 15.

**2. Subsolvus Heat Treatment Response.**—Images of the typical microstructures produced after subsolvus solution heat treatments of 1135 °C for 1 and 4 hours are shown in figures 16 to 21. Mean grain size at the center of DC specimens in figure 22 again appeared comparable to that of RCC specimens tested at the equivalent approximate strain and strain rate conditions. Plots of mean grain size versus

log (strain rate) at various temperatures, presoak times, and solution heat treat times of the RCC specimens are shown in figure 23. Mean grain size number appeared to decrease with increasing temperature and solution heat treatment time. Stepwise linear regression of mean grain size number on temperature, log (presoak time), log (strain rate) and log (solution time) was performed. The resulting equation indicated subsolvus mean grain size number (SBG) strongly decreased with increasing log(solution time), and moderately decreased with increasing temperature, log (strain rate), and log (presoak time) for the range of conditions investigated, according to the equation:

$$\text{SBG} = 10.803077 - 0.120 T' - 0.0120009 \log(R)' - 0.165107 \log(P)' - 0.560037 \log(S)' - 0.2125 T' \log(R)' - 0.140009 \log(R)' \log(S)', \quad (4)$$

with a correlation coefficient of  $R^2_{\text{adj}} = 0.8755$  and rms error = 0.2355. The  $T' \log(R)'$  interaction term indicated enhanced subsolvus grain growth for combinations of high temperature and high log (strain rate). The  $\log(R)' \log(S)'$  interaction term indicated enhanced subsolvus grain growth for combinations of high log (strain rate) and high log (solution time). The complete statistical output is given in appendix A-3. A plot of predicted and actual mean grain size indicated very good agreement, figure 25.

The macrostructures of subsolvus heat treated specimens were appeared uniform in all cases, suggesting well-controlled grain size. Plots of observed ALA subsolvus grain size versus log (strain rate) at various temperatures, presoak times, and solution times for the RCC specimens are shown in figure 24. No consistent trends are visually apparent. The results of linear regression with stepwise selection of terms indicated (appendix A-4) ALA subsolvus grain size number (SBALA) only significantly decreased with increasing log (strain rate) for the range of conditions investigated:

$$\text{SBALA} = 7.65 - 0.525 \log(R)', \quad (5)$$

with a poor correlation coefficient of  $R^2_{\text{adj}} = 0.1920$  and rms error = 0.8359. A plot of predicted and actual grain size number indicated only modest agreement, figure 25.

**Supersolvus Heat Treatment Response.**—The microstructures of supersolvus heat treated specimens are shown in figures 26 to 32. Mean grain size at the center of DC specimens again appeared comparable to that of RCC specimens tested at the equivalent approximated strain and strain rate conditions. Plots of mean grain size number vs. log (strain rate) are shown for the various temperatures, presoaks, and solution heat treat times of the RCC specimens in figure 33. Mean grain size number appeared to decrease with increasing forging temperature. Linear regression using stepwise selection of terms indicated (appendix A-5) supersolvus mean grain size number (SPG) only moderately decreased with increasing temperature, log(presoak time), and log(solution time) for the range of conditions investigated according to the equation:

$$\text{SPG} = 5.966475 - 0.275 T' - 0.167369 \log(P)' - 0.0223348 \log(S)', \quad (6)$$

with a relatively low correlation coefficient of  $R^2_{\text{adj}} = 0.3439$  and rms error = 0.4429. This suggested a relatively stable mean grain size for the ranges of conditions tested. However, inspection of figure 33 indicates more divergence in grain size at the highest forging temperature of 1110 °C. A plot of predicted and actual grain size number showed fair agreement, figure 34.

The macrostructures of supersolvus heat treated specimens are shown in figures 35 to 41. Reduced uniformity and large grains are evident for specimens forged at 1110 °C and a strain rate of 0.03 s<sup>-1</sup>. The “rims” of DC specimens tested at 1080 °C and 0.03 s<sup>-1</sup> approximated average strain rate also show large grains. Plots of ALA grain size number vs. log(strain rate) at various presoaks and solution times for the RCC specimens are shown in figure 42. Stable ALA grain sizes are evident for all specimens forged at 1050 and 1080 °C. However, very low ALA grain size numbers corresponding to large grain are present for specimens forged at 1110 °C and a strain rate of 0.03 s<sup>-1</sup>. Linear regression would be expected to have

difficulty handling such sharp, isolated changes in response. However, a relationship for supersolvus ALA grain size number (SPALA) could be derived by stepwise selection (appendix A–6):

$$\text{SPALA} = 1.696504 - 1.166139 T' - 1.191710 \log(R)' - 0.698321 \log(P)' - 1.3125 T' \log(R)' - 0.783 T' \log(P)' - 0.732556 \log(R)' \log(P)', \quad (7)$$

with a correlation coefficient of  $R^2_{\text{adj}} = 0.5347$  and rms error = 1.689. In this equation, SPALA number decreased with increasing temperature, log (strain rate) and log (presoak time). The  $T' \log(R)'$  interaction term indicated enhanced ALA grain growth for combinations of high temperature and high log (strain rate). The  $T' \log(P)'$  interaction term indicated enhanced ALA grain growth for combinations of high temperature and high log (presoak time). The  $\log(R)' \log(P)'$  interaction term indicated enhanced ALA grain growth for combinations of high log (strain rate) and high log (presoak time). This equation fit was strongly influenced by the critical grain growth occurrences, and a plot of predicted and actual grain size number showed only fair agreement, figure 43. However, the equation clearly signifies that the combination of 1110 °C and strain rate of 0.03 s<sup>-1</sup> should be avoided.

**Combined Subsolvus + Supersolvus Heat Treatment Response.**—The microstructures of subsolvus + supersolvus heat treated specimens are shown in figures 44 to 50. Mean grain size at the center of DC specimens again appeared comparable to that of RCC specimens tested at the equivalent approximated strain and strain rate conditions. Plots of mean grain size number vs. log (strain rate) are shown for the various temperatures, presoaks, and solution heat treatment times of the RCC specimens in figure 51. No consistent trends are visually obvious in these figures. Linear regression with stepwise selection of terms indicated (appendix A–7) mean subsolvus + supersolvus grain size number (SBPG) varied for the range of conditions investigated according to the equation:

$$\text{SBPG} = 5.91332 - 0.193346 \log(S)' + 0.31875 T' \log(R)', \quad (8)$$

with a correlation coefficient of  $R^2_{\text{adj}} = 0.3733$  and rms error = 0.3775. This again suggested a relatively stable mean grain size for the ranges of conditions tested. The equation indicated SBPG number decreased with increasing log (solution time). The  $T' \log(R)'$  interaction term indicated enhanced grain growth for combinations of low log (strain rate) with high temperature, and high log(strain rate) with low temperature. A plot of predicted versus actual mean grain size in figure 52 showed reasonable agreement.

The macrostructures of subsolvus + supersolvus heat treated specimens are shown in figures 53 to 59. Plots of ALA grain size number vs. log (strain rate) at various presoaks and solution times for the RCC specimens are shown in figure 60. As for supersolvus heat treated specimens, ALA grain size was relatively stable for most conditions. The “rims” of DC specimens tested at 1080 °C and 0.03 s<sup>-1</sup> approximated average strain rate also now showed stable ALA grain growth with the combined subsolvus plus supersolvus heat treatment, unlike the supersolvus heat treatment case. However, for the combination of 8h forging presoak, 1110 °C, and 0.03 s<sup>-1</sup> strain rate, very low ALA grain size numbers corresponding to very large grains are evident in the plots and macrostructures. These few critical grain growth occurrences in RCC specimens again strongly influenced the linear regression, producing a complex relationship (appendix A–8) for subsolvus + supersolvus ALA grain size number (SBPALA) for the range of conditions investigated:

$$\text{SBPALA} = 1.862922 - 0.66806 T' - 0.542313 \log(R)' - 0.685123 \log(P)' - 0.613291 T' \log(P)' - 0.679285 \log(R)' \log(P)', \quad (9)$$

with a relatively low correlation coefficient of  $R^2_{\text{adj}} = 0.3039$  and rms error = 1.466. This indicated ALA grain size number decreased with increasing temperature, log (strain rate), and log (presoak time). The  $\log(R)' \log(P)'$  interaction term again indicated enhanced ALA grain growth for combinations of high log (strain rate) and high log (presoak time). This equation fit was again strongly influenced by the critical

grain growth occurrences, but a plot of predicted and actual grain size number showed fair agreement, figure 61. However, the equation produced less satisfactory ALA grain size predictions for critical grain growth conditions than in the supersolvus heat treatment case.

***Selection of Appropriate Forging Conditions for Uniform Microstructures.***—In general terms, as-forged, subsolvus, supersolvus, and subsolvus plus supersolvus mean and as-large-as grain sizes were smallest for the lowest forging temperature of 1050 °C, and were relatively insensitive to strain rate and presoak time at that temperature. As-forged, subsolvus, supersolvus, and subsolvus plus supersolvus mean and as-large-as grain sizes were largest for the highest forging temperature of 1110 °C, and were more sensitive to strain rate and presoak time. The intermediate forging temperature of 1080 °C allowed intermediate mean and as-large-as grain sizes, with still relatively low strain rate and presoak time sensitivity. This would generally argue for a forging temperature range of 1050 to 1080 °C, to insure uniform microstructures while allowing some random variations in exact temperature and presoak times expected during production runs, and systematic variations in strain rate expected within forging dies.

The microstructures of subsolvus heat treated specimens were generally quite uniform over the entire range of forging conditions investigated. However, mean subsolvus grain size was least sensitive to strain rate and presoak time for the forging temperature range of 1050 to 1080 °C. As-large-as subsolvus grain size was also minimized over this forging temperature range. Therefore selection of this forging temperature range for material intended for subsolvus heat treatment would allow full latitude in strain rate and presoak time within the range of conditions investigated. Increasing subsolvus solution heat treat time from 1 to 4 hours allowed some coarsening of mean grain size number from near 11.5 (6.7 μm) to near 10.5 (9.4 μm), without adversely increasing as-large-as grain size.

The microstructures of supersolvus heat treated specimens were generally uniform over the temperature range of 1050 to 1080 °C for the forging conditions investigated. Mean supersolvus grain size remained near 6.0 (45 μm) and was not usually sensitive to strain rate and presoak time for this forging temperature range. As-large-as supersolvus grain size was also minimized to near 2 (180 μm) over this forging temperature range for the right circular cylinder specimens. For double cone specimens tested at 1080°C and an approximated strain rate of 0.03 s<sup>-1</sup>, a divergence in response was observed between supersolvus and subsolvus plus supersolvus heat treatments. Supersolvus heat treated DC specimens exhibited critical grain growth to produce very large grains up to -6 (3100 μm) in the rims of DC specimens, while subsolvus plus supersolvus heat treatments minimized their as-large-as grain size to 2 (180 μm). The highest localized strain rates induced in the rims of DC specimens apparently encouraged enhanced deformation in the microstructure, to encourage the critical grain growth in direct supersolvus heat treatments as observed for Rene' 88DT (ref 4). Addition of a prior subsolvus heat treatment step before the supersolvus heat treatment apparently helps anneal out some of this localized forging deformation (ref. 3). For these reasons, forging at 1050 to 1080 °C would be advisable, followed by a subsolvus plus supersolvus heat treatment to achieve a uniform microstructure with mean grain size near 6.0 (45 μm) and as-large-as grain size minimized to 2.0 (180 μm). This would allow forging presoaks of 1 to 8 hours and strain rates of 0.0003 to 0.03 s<sup>-1</sup> without adverse effects.

At 1110 °C, mean supersolvus grain size was more sensitive to strain rate and presoak time. Slower strain rates and longer presoak times allowed coarser mean supersolvus grain size near 5 (65 μm). This trend of coarser mean supersolvus grain size with higher forging temperature, slower strain rates, and longer presoak times has been previously observed in another powder metallurgy disk superalloy (ref. 6). As-large-as grain size remained near 2 (180 μm) at strain rates of 0.0003 to 0.003 s<sup>-1</sup>, but critical grain growth produced very large grains for a forging strain rate of 0.03 s<sup>-1</sup>. Therefore, forging at this temperature followed by a subsolvus plus supersolvus heat treatment could be used to achieve a coarser mean grain size near 5.0, provided that the forging strain rates are maintained between 0.0003 and 0.003 s<sup>-1</sup>. Forging presoak times between 1 and 8 h would be allowable in these conditions.

***Comparison of TMP Specimen and Disk Forging Results.***—The forging condition recommendations based on TMP test results were compared to disk forging results for the supersolvus



case, where grain size control can be more critical for high temperature applications. Grain size control can be especially important in low cycle fatigue resistance, where coarser grain size can reduce fatigue life (refs. 4 and 7). An extrusion mult 16.5 cm in diameter and 20 cm long was forged at 1080 °C after a presoak time of 3 hours, using an average strain rate of 0.003 s<sup>-1</sup>. The mult was forged to a final height of 4 cm, representing an 80 percent upset. This forged disk was then given a subsolvus solution heat treatment of 1135 °C/1h, followed by a supersolvus treatment of 1171 °C for 3 hours. Equation 8 predicted a mean grain size of 5.8 (48 μm) for these conditions, while equation 9 predicted an as-large-as grain size of 1.8 (190 μm). Measurements on duplicate specimens extracted from the disk indicated mean grain sizes of 6.7 (35 μm) and 7.2 (30 μm). As-large-as grain sizes were 2.5 (150 μm) and 3.0 (125 μm). The experimental forging grain size results were conservatively finer than those predicted using the TMP specimen data, and quite satisfactory. The finer grain sizes observed in the disk could be related to the much greater forging upset of 80 percent and true strain of 1.6 in the disk forging, compared to the 50 percent upset and true strain of 0.7 percent incurred in TMP test specimens. The higher strains within the forging could encourage more grain recrystallization, for finer resulting heat treated grain sizes.

## Summary and Conclusions

A series of forging experiments were performed with subsequent subsolvus and supersolvus heat treatments, in search of suitable forging conditions for producing uniform fine grain and coarse grain microstructures. Forging temperatures of 1050 to 1110 °C and strain rates of 0.0003 to 0.03 s<sup>-1</sup> were used, after presoaks of 1h to 8h. Subsolvus, supersolvus, and combined subsolvus plus supersolvus heat treatments were then applied with final solution times of 1h or 4h. The findings over this range of test conditions can be summarized as follows:

- 1) The material displayed the desired superplastic response under these compression testing conditions.
- 2) Forging flow stress strongly increased with increasing strain rate, but only moderately increased with decreasing temperature and increasing presoak time.
- 3) As-forged grain size number varied between 13.0 and 11.4 (4.0 and 7.0 μm), and only moderately coarsened with increasing temperature.
- 4) Subsolvus heat treated mean grain size number varied between 12 and 9.5 (5.6 and 13 μm), strongly coarsened with increasing log (solution time), and moderately coarsened with increasing temperature, log (strain rate), and log (presoak time).
- 5) Subsolvus as-large-as grain size number was very well controlled at between 9.5 and 5.5 (13 and 55 μm), and only significantly coarsened with increasing log (strain rate).
- 6) Supersolvus heat treated mean grain size number varied between 6.6 and 4.2 (36 and 85 μm), and substantially coarsened with increasing temperature, log (presoak time), and log (solution time).
- 7) Supersolvus as-large-as grain size number varied between 4.0 and -6.5 (90 and 3100 μm), and substantially coarsened with increasing temperature, log (strain rate) and log (presoak time).
- 8) Subsolvus plus supersolvus heat treated mean grain size number varied between 6.8 and 5.0 (34 and 65 μm), and coarsened with increasing log (solution time).
- 9) Subsolvus plus supersolvus heat treated as-large-as grain size number varied between 3.5 and -6.0 (105 and 2600 μm), and coarsened with increasing temperature, log (strain rate), and log (presoak time).
- 10) Forging conditions combining high temperature, high presoak time, and high strain rate produced very large, macroscopic grains.

It can be concluded from this work that:

- 1) Forging at temperatures of 1050 to 1080 °C over the full range of presoak times and strain rates investigated is recommended to achieve mean grain sizes of 10.5 to 11.5 and ALA grain sizes of 6.5 for applications utilizing subsolvus heat treatments.
- 2) Forging at temperatures of 1050 to 1080 °C over the full range of presoak times and strain rates investigated is recommended to achieve mean grain size near 6.0 and as-large-as grain size of 2.0, for applications utilizing a subsolvus plus supersolvus heat treatment.
- 3) Alternatively forging near 1110 °C over the full range of presoak times and strain rates of 0.0003 to 0.003 s<sup>-1</sup> is recommended to achieve coarser mean grain size near 5.0 and as-large-as grain size of 2.0, when using a subsolvus plus supersolvus heat treatment.
- 4) Forging at 1050 to 1080 °C and strain rates of 0.0003 to 0.003 s<sup>-1</sup> is recommended for material intended for direct supersolvus heat treatments, in order to avoid critical grain growth.

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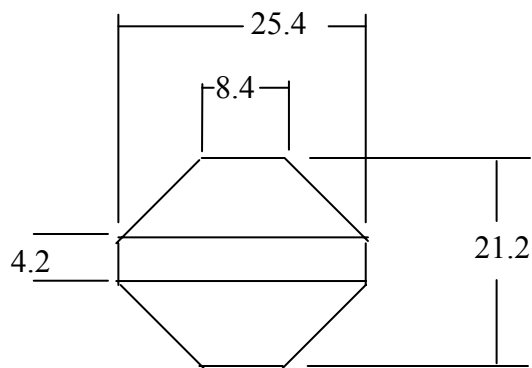


Figure 1.—Double cone specimen configuration,  
with dimensions in millimeters.

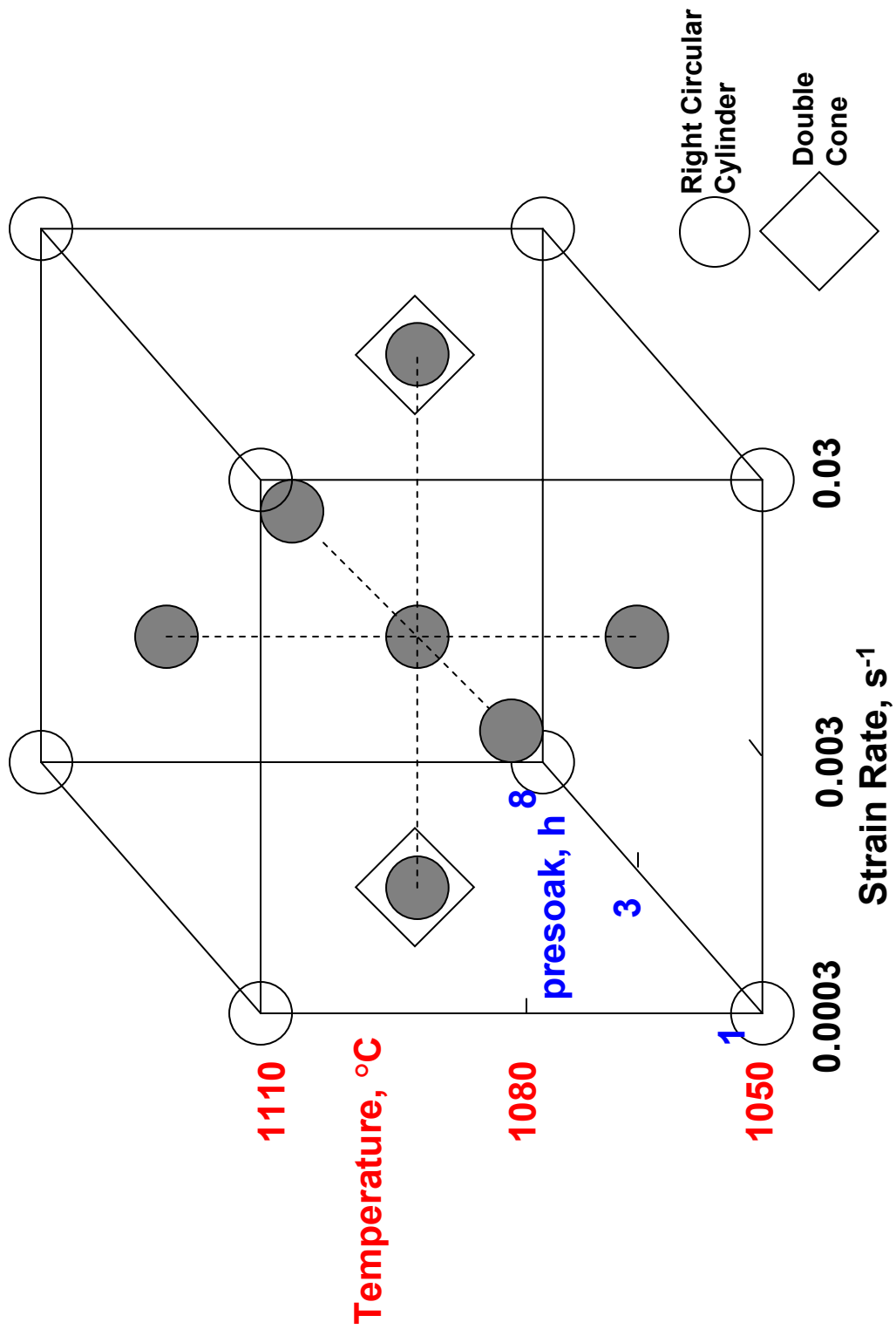


Figure 2.—Diagram showing the design of experiments with experimental conditions.

1050C

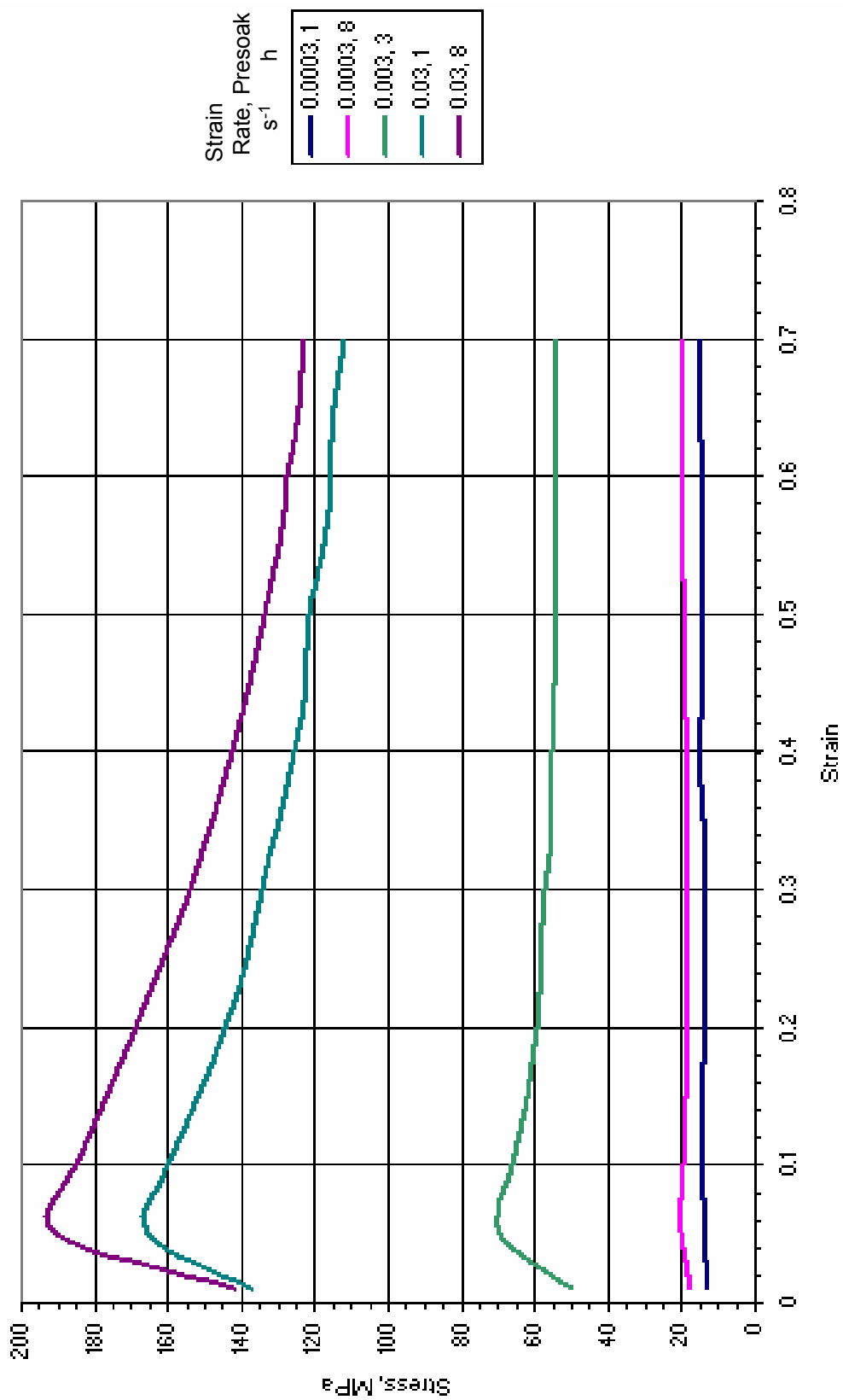


Figure 3.—Compression test stress-strain responses at 1050 °C.

1080°C

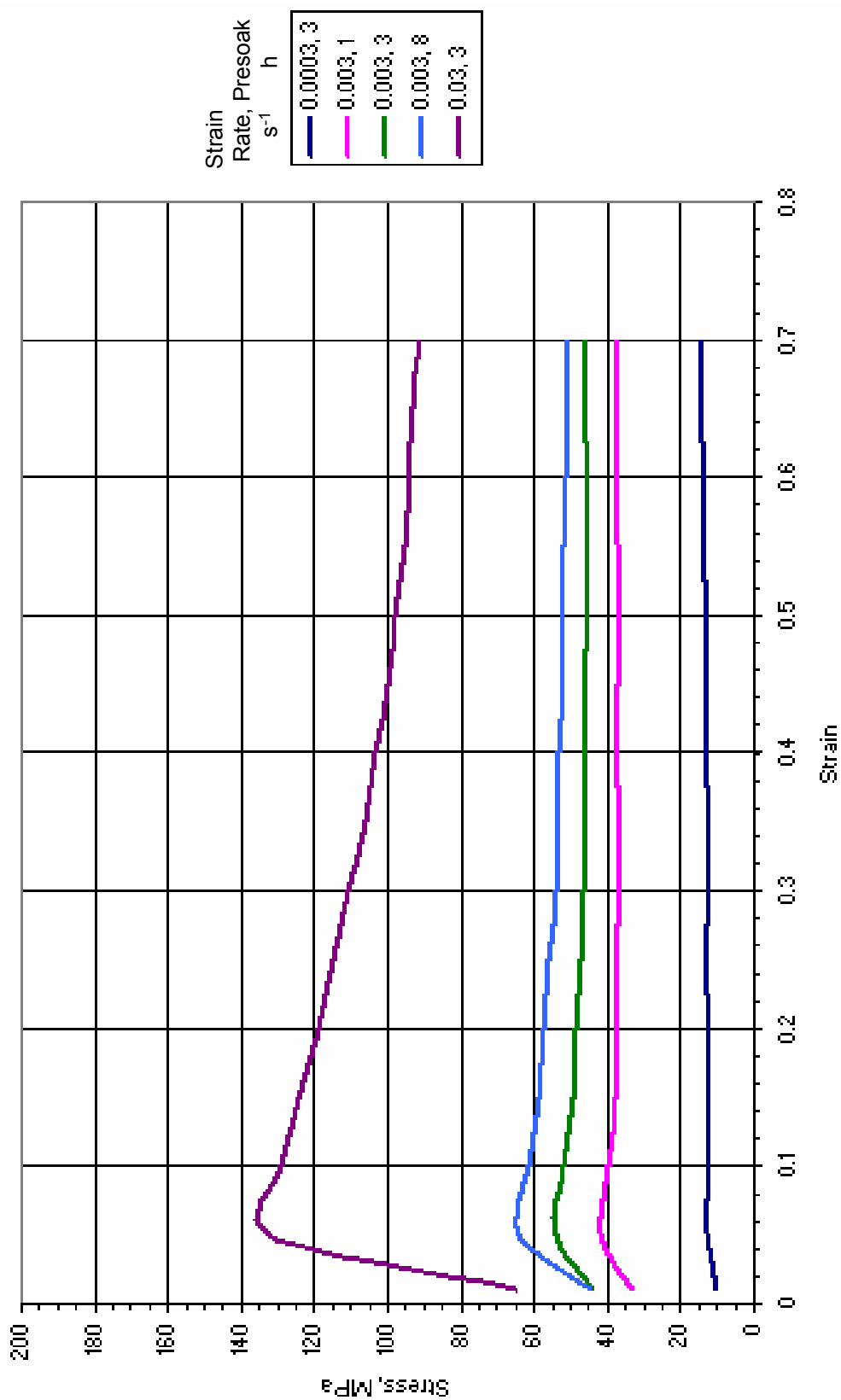


Figure 4.—Compression test stress-strain responses at 1080 °C.

1110°C

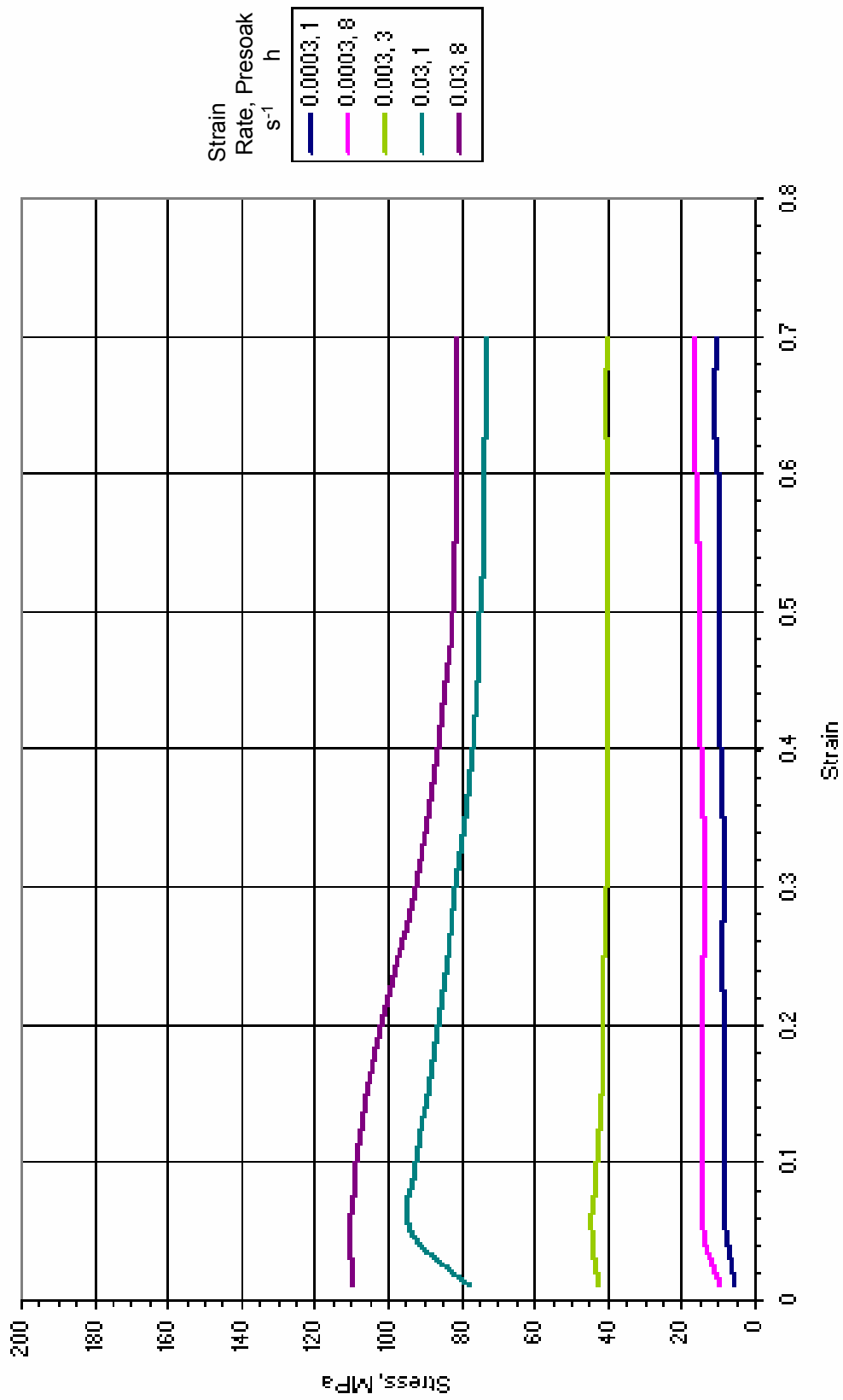


Figure 5.—Compression test stress-strain responses at 1110 °C.

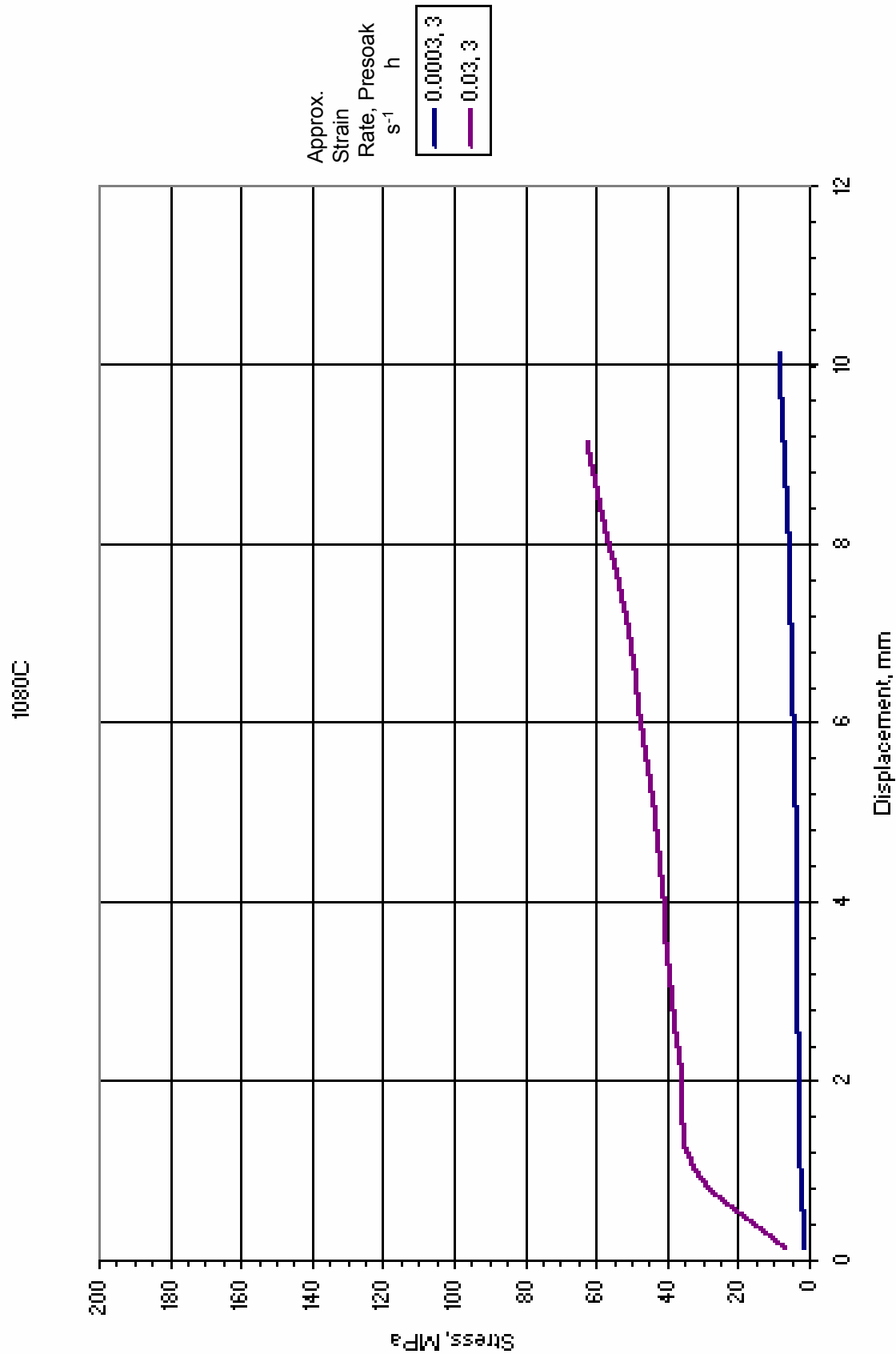


Figure 6.—Compression test stress-displacement responses for double cone specimens at 1080 °C.



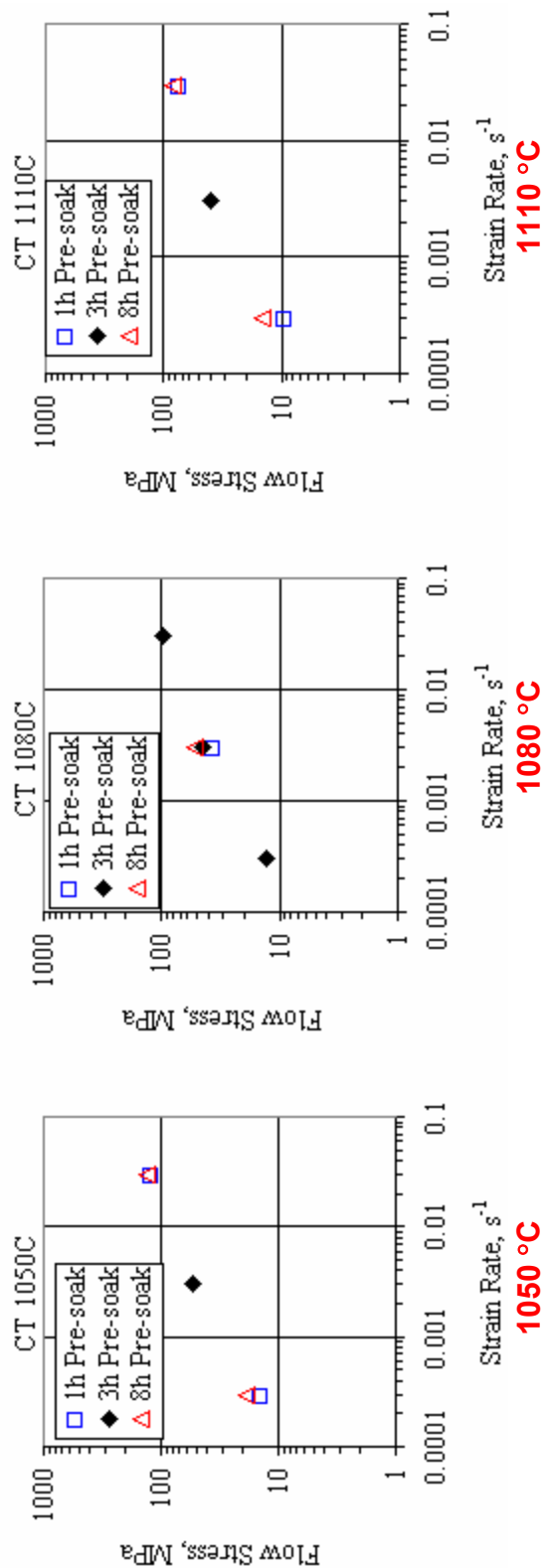


Figure 7.—Compression test true flow stress vs. strain rate.

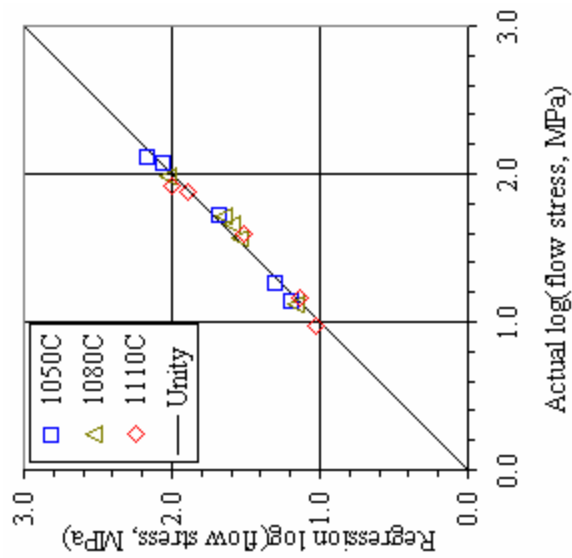


Figure 8.—Comparison of actual vs. regression flow stresses.

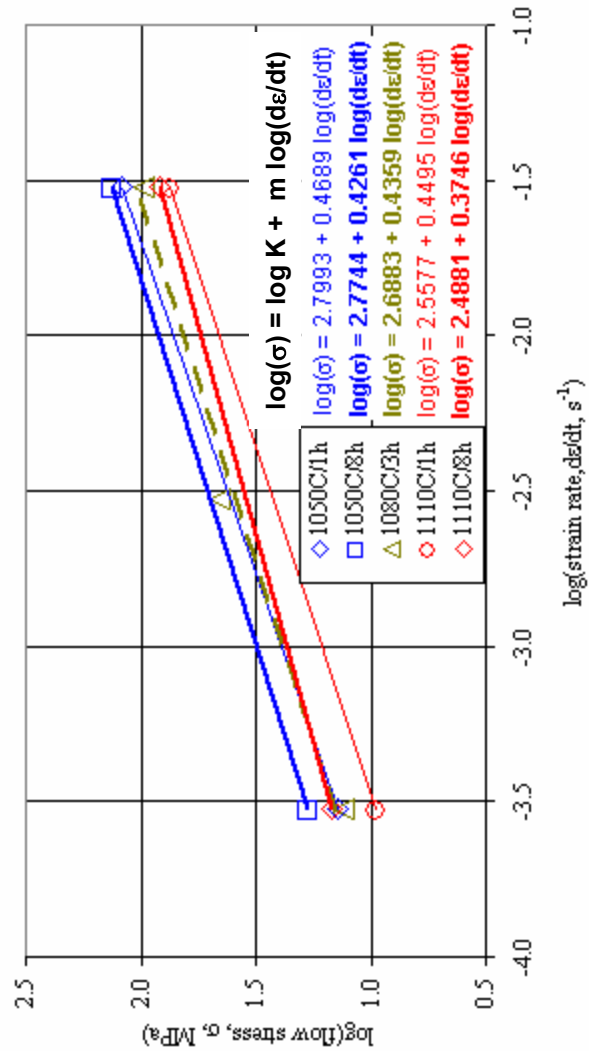


Figure 9.—Log (flow stress) vs. log (strain rate) plots with superplasticity (m) determinations.

# As-Forged 1050 °C

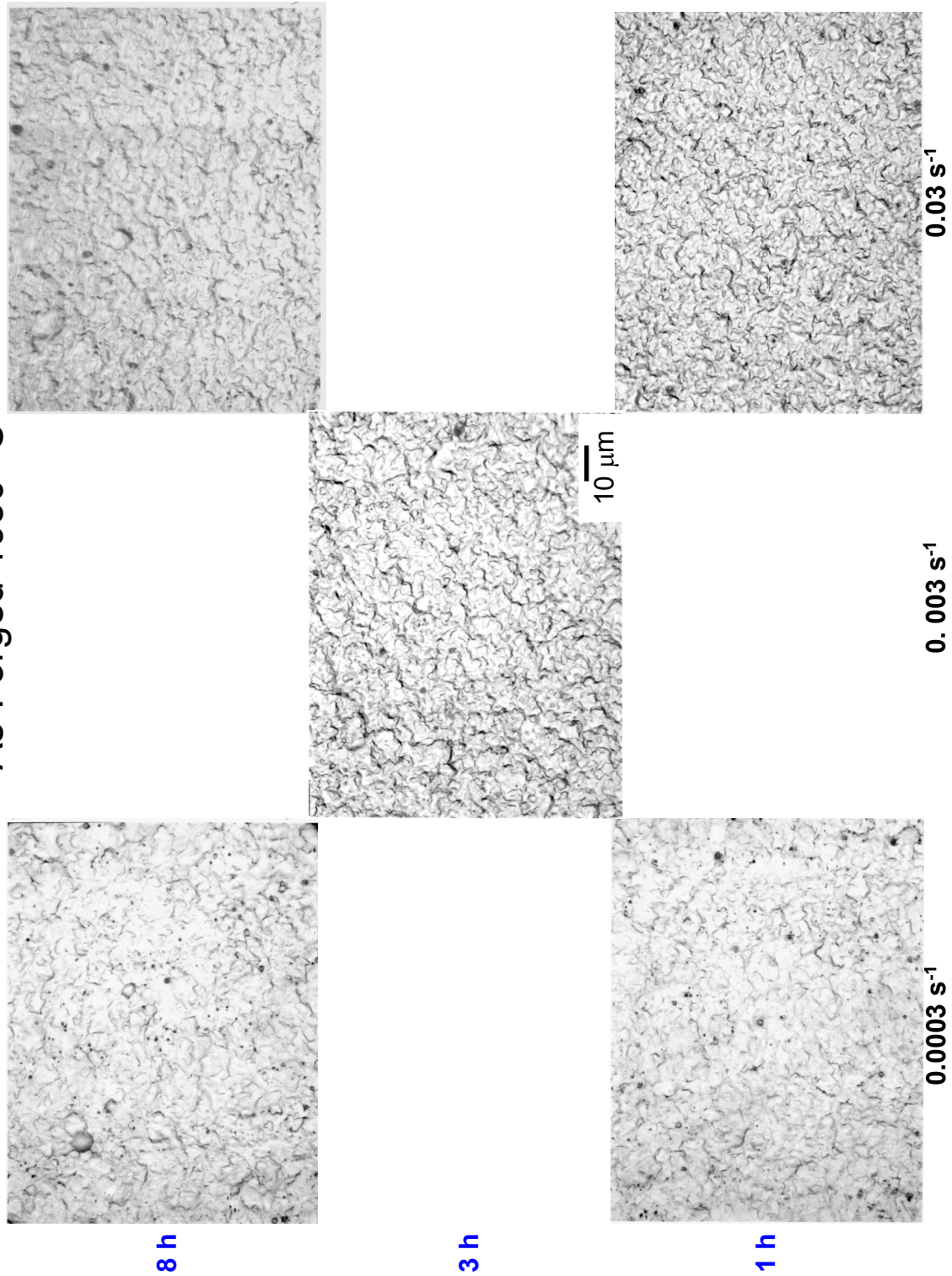


Figure 10.—Typical microstructures of specimens forged at 1050 °C with the indicated pre-soak times and strain rates.

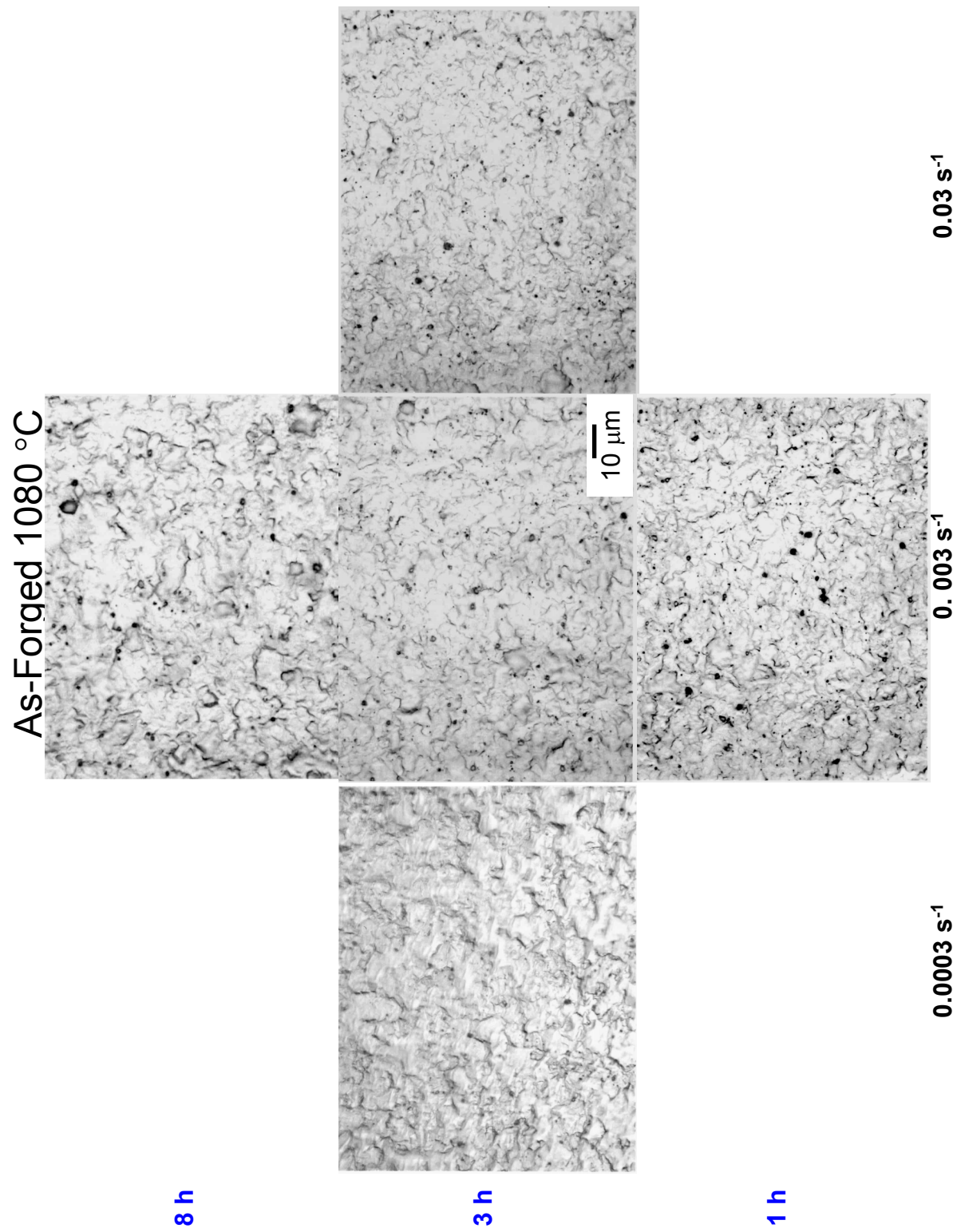


Figure 11.—Typical microstructures of specimens forged at 1080 °C with the indicated pre-soak times and strain rates.



# As-Forged 1110 °C

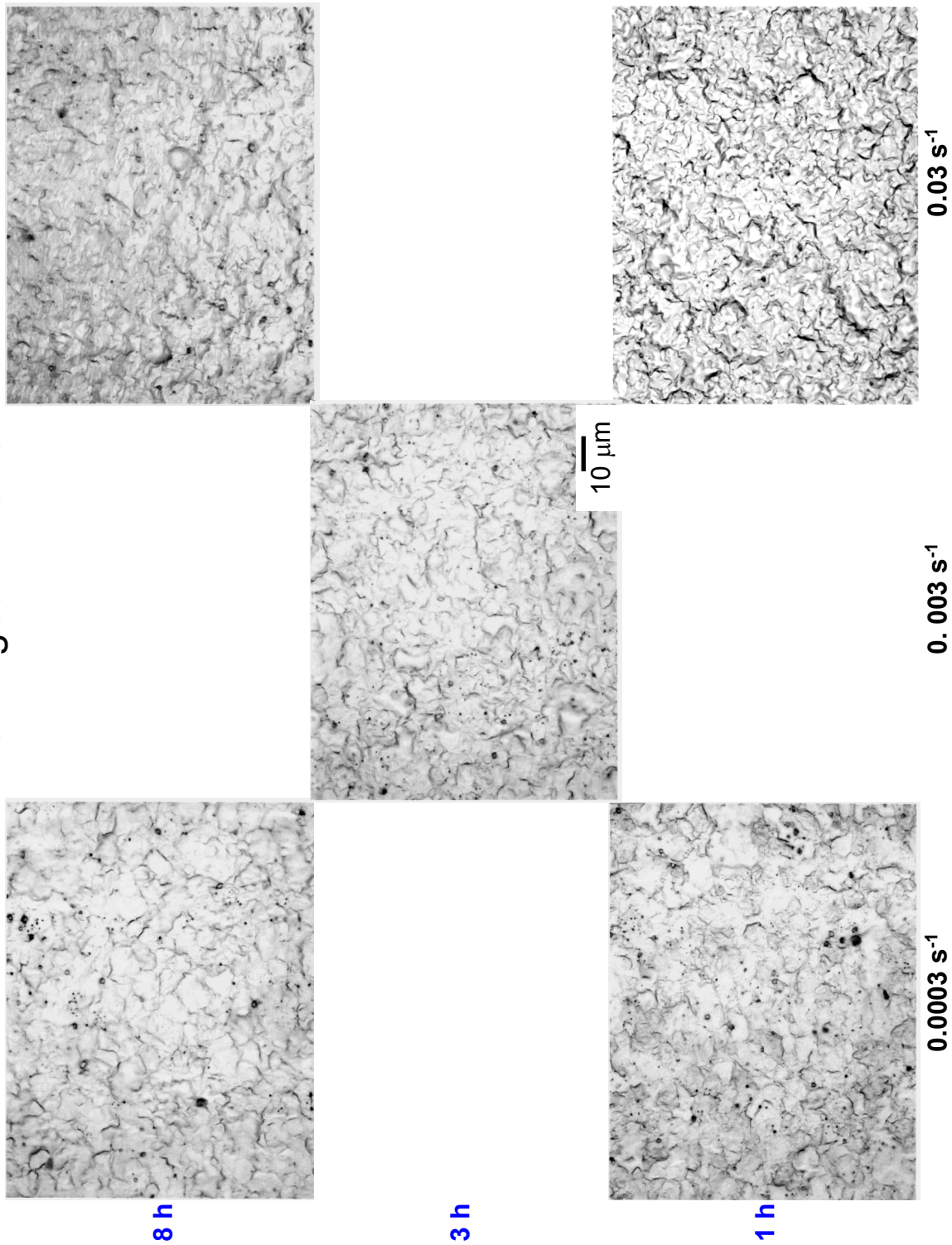


Figure 12.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates.

## As-Forged DC Specimens 1080 °C



**~0.0003 s<sup>-1</sup>**

**~0.03 s<sup>-1</sup>**

Figure 13.—Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and approximate average strain rates.

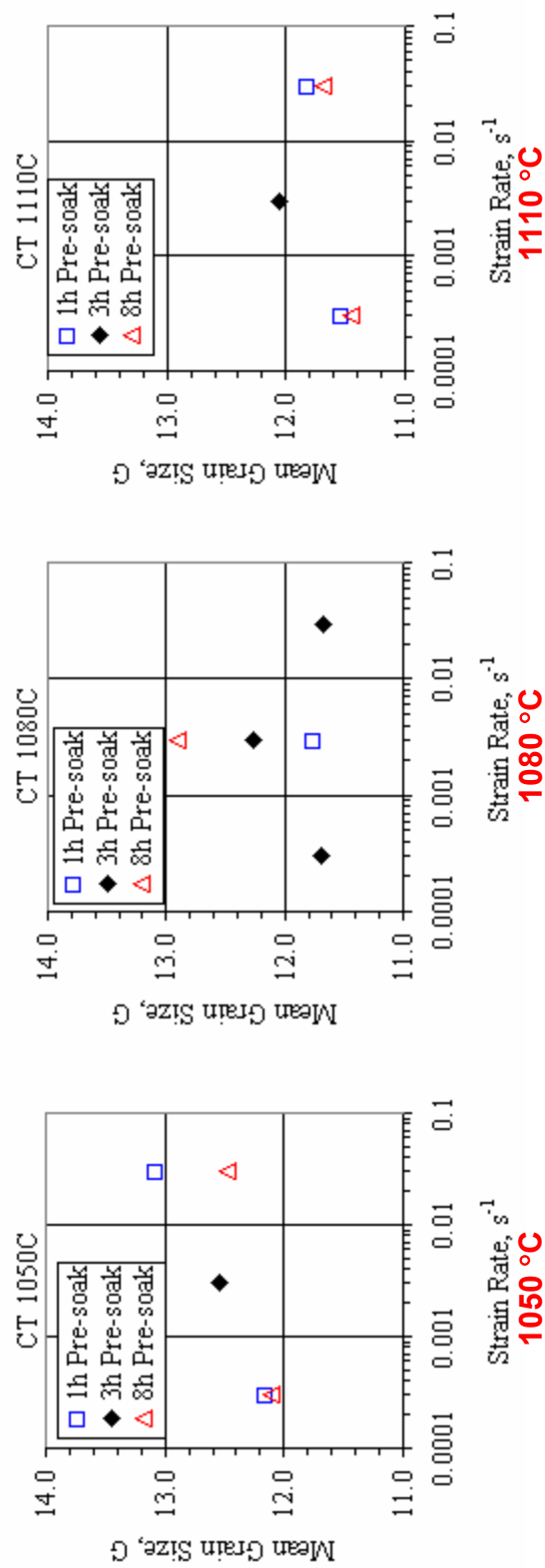


Figure 14.—Mean as-forged grain size vs. strain rate for the indicated forging pre-soak times and temperatures.

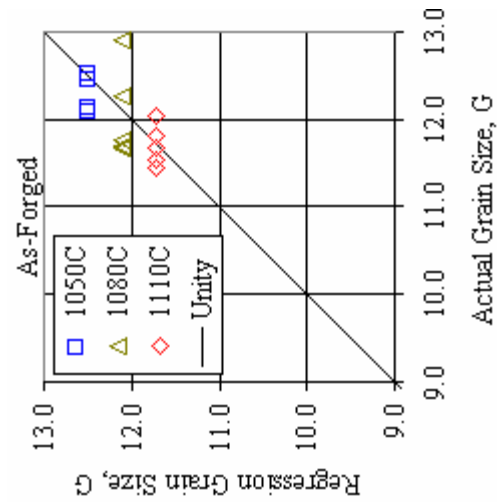
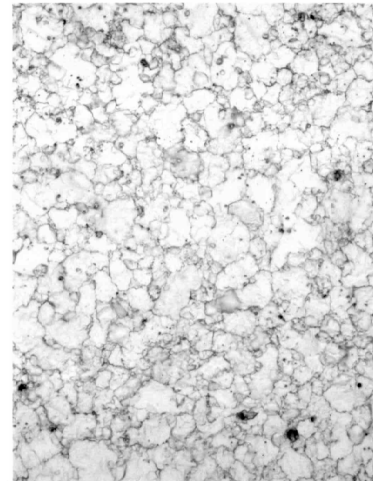
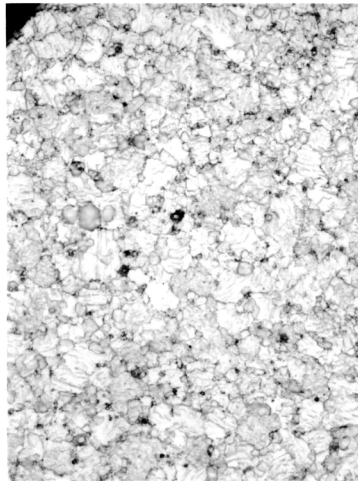
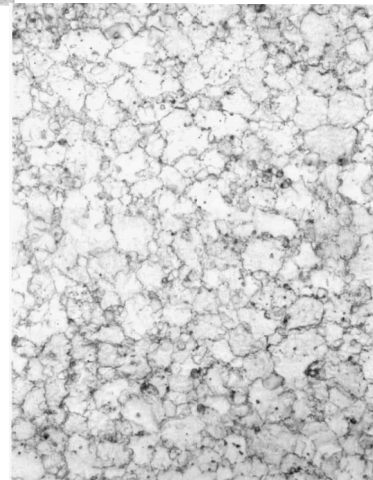
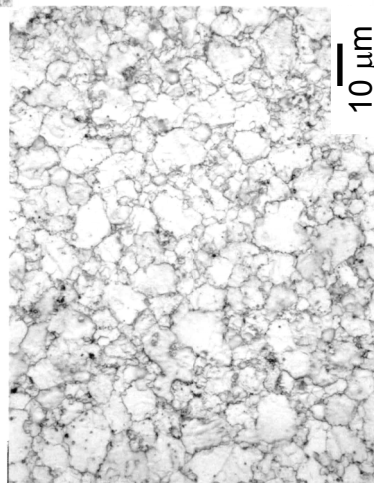


Figure 15.—Comparison of actual vs. regression as-forged mean grain sizes.

SUB1 1050 °C



**0.0003 s<sup>-1</sup>**

**0.003 s<sup>-1</sup>**

**0.03 s<sup>-1</sup>**

Figure 16.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 1h.



# SUB4 1050 °C

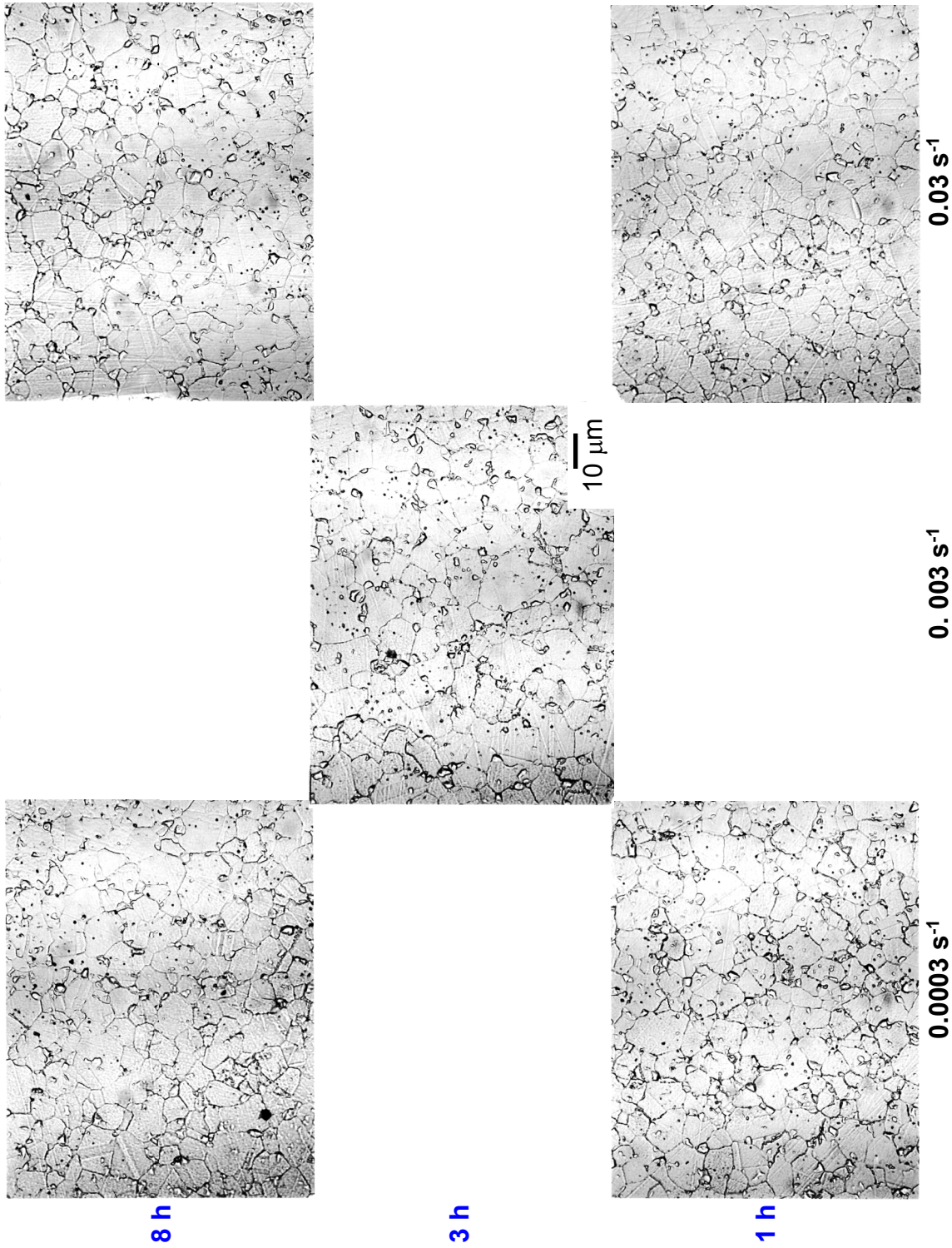


Figure 17.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 4h.

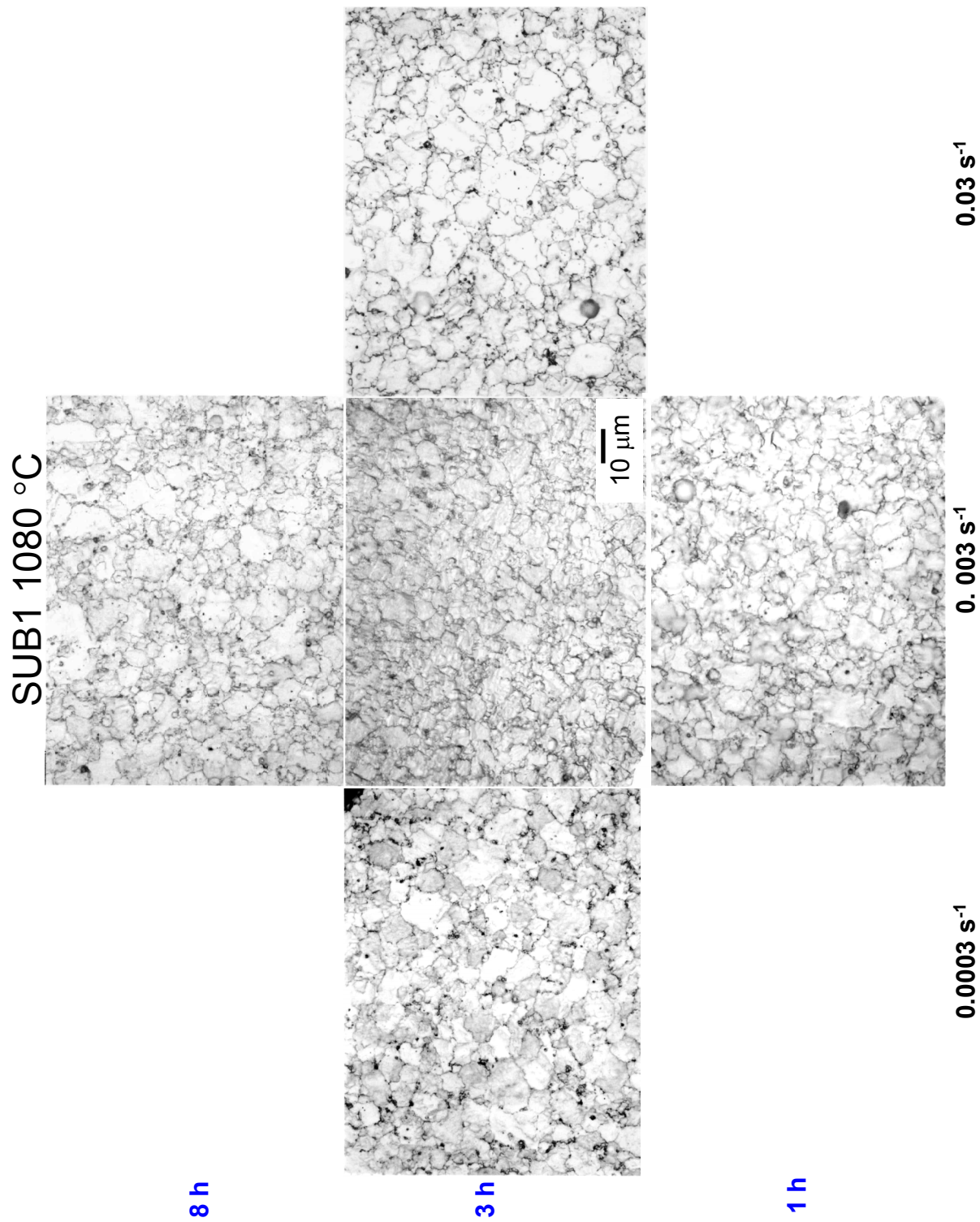


Figure 18. Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 1 h.



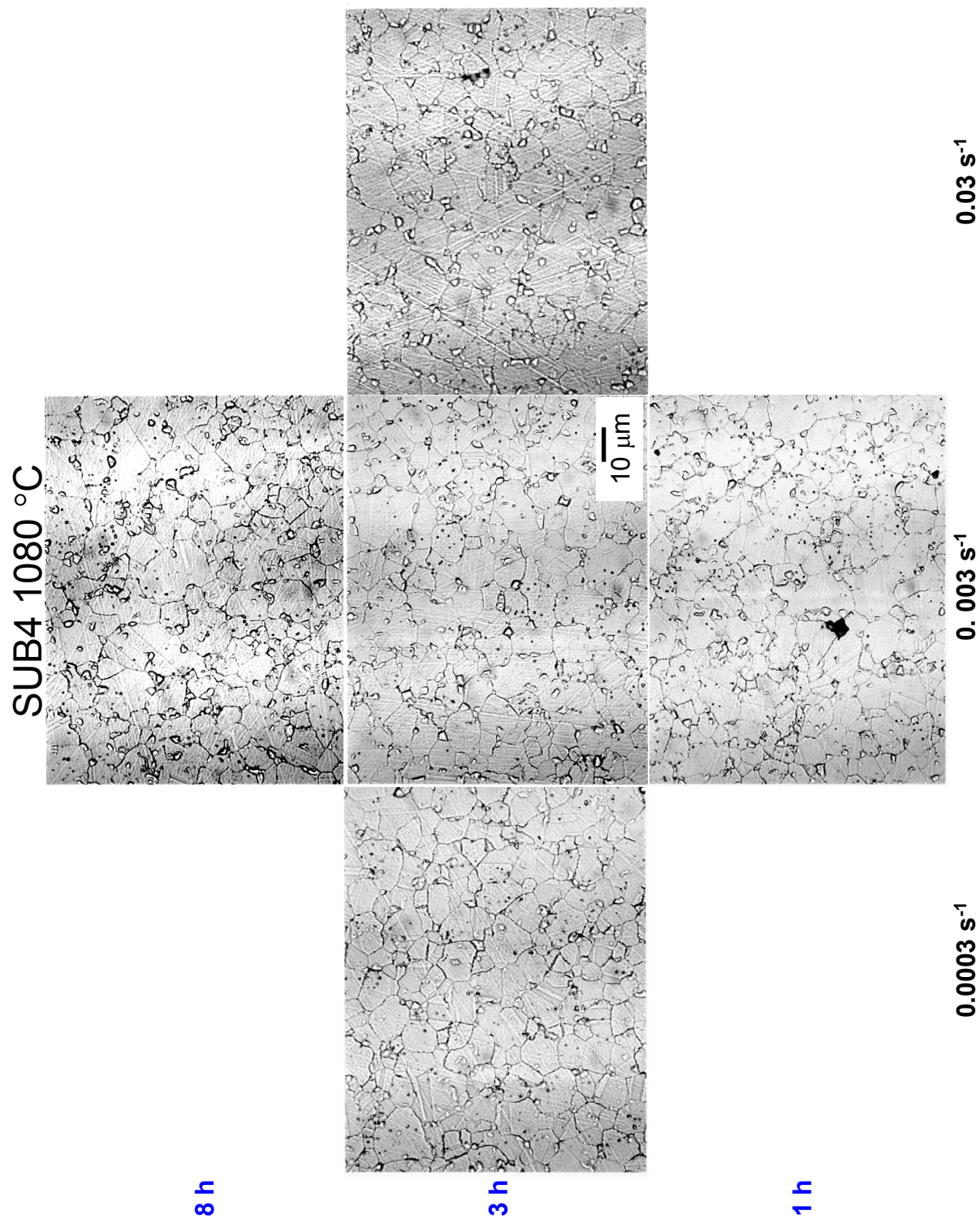


Figure 19.—Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 4h.

# SUB1 1110 °C

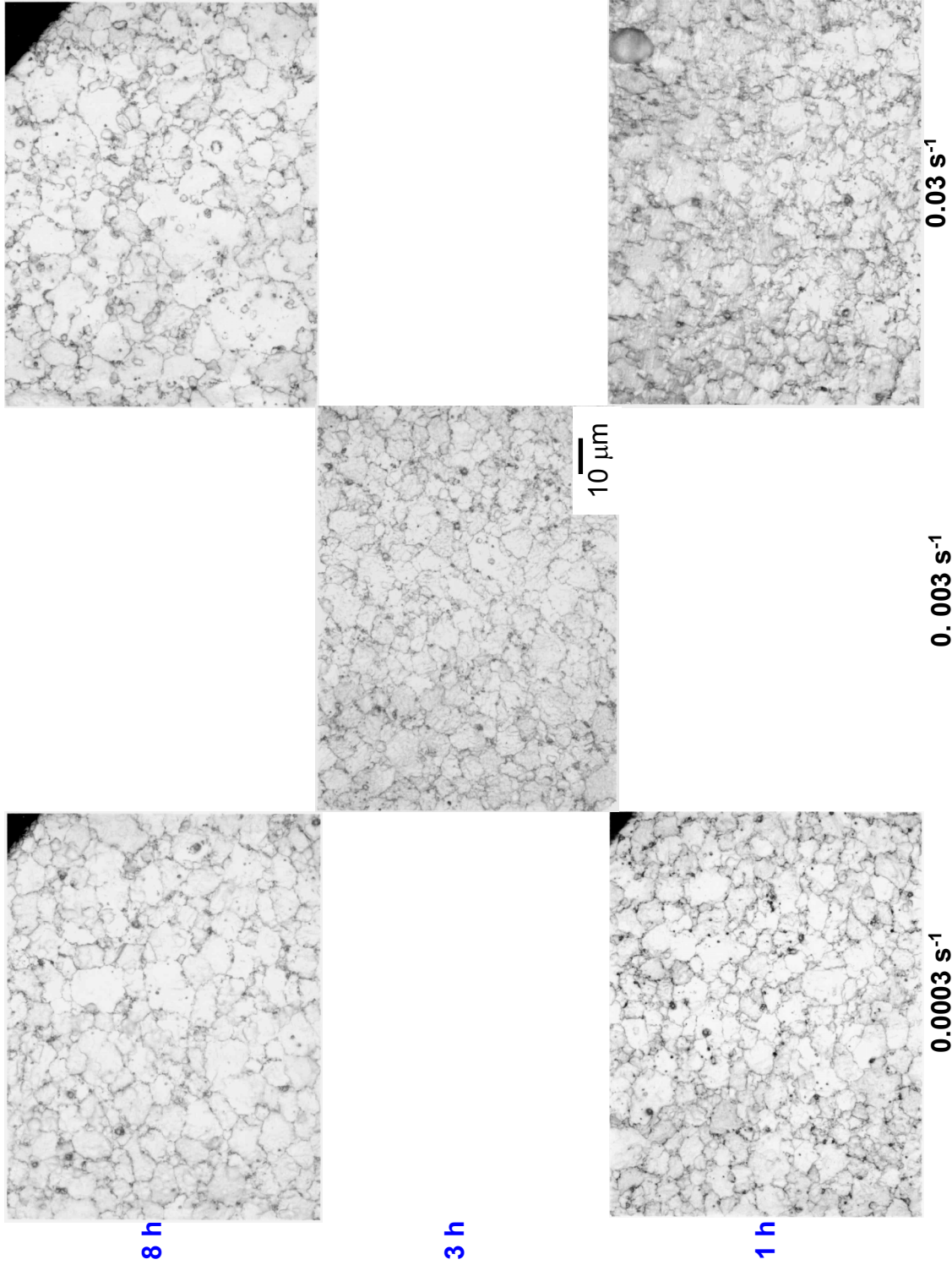


Figure 20.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 1h.



# SUB4 1110 °C

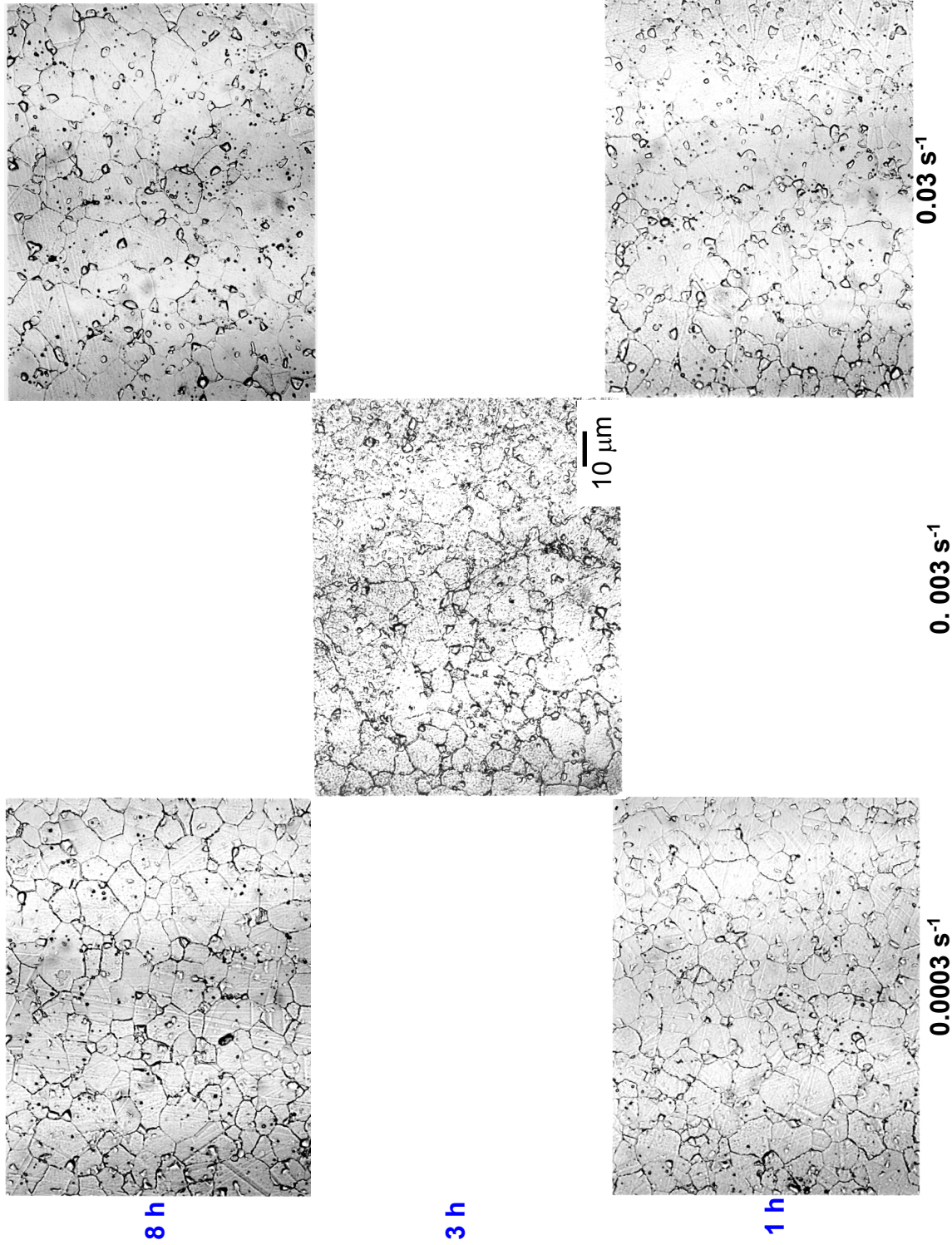


Figure 21. Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then subsolvus solution heat treated 4h.

## SUB DC Specimens 1080 °C

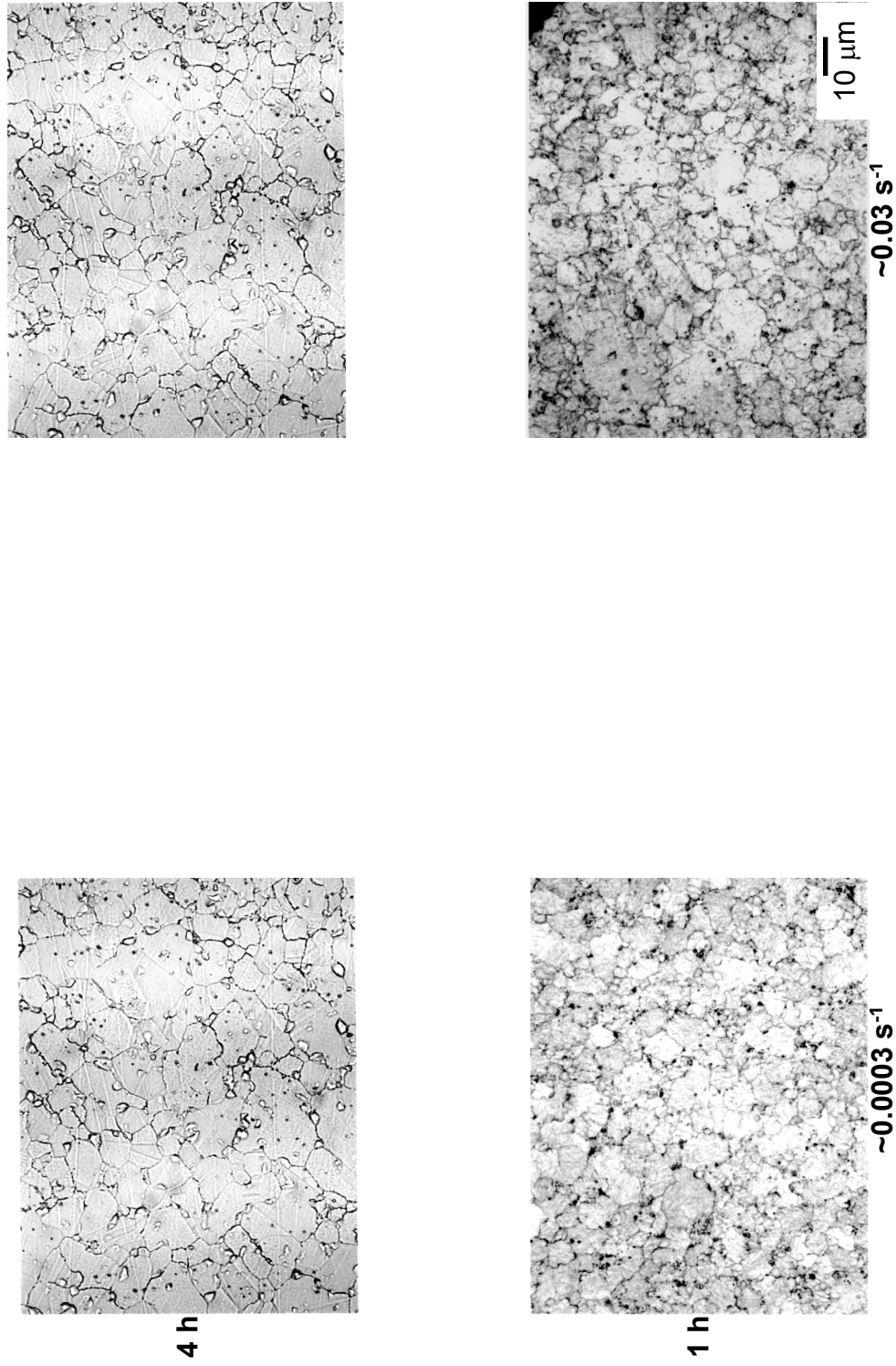


Figure 22.—Typical microstructures of double cone specimens forged at 1080 °C with the indicated approximate average strain rates, then subsolvus solution heat treated 1 and 4h.

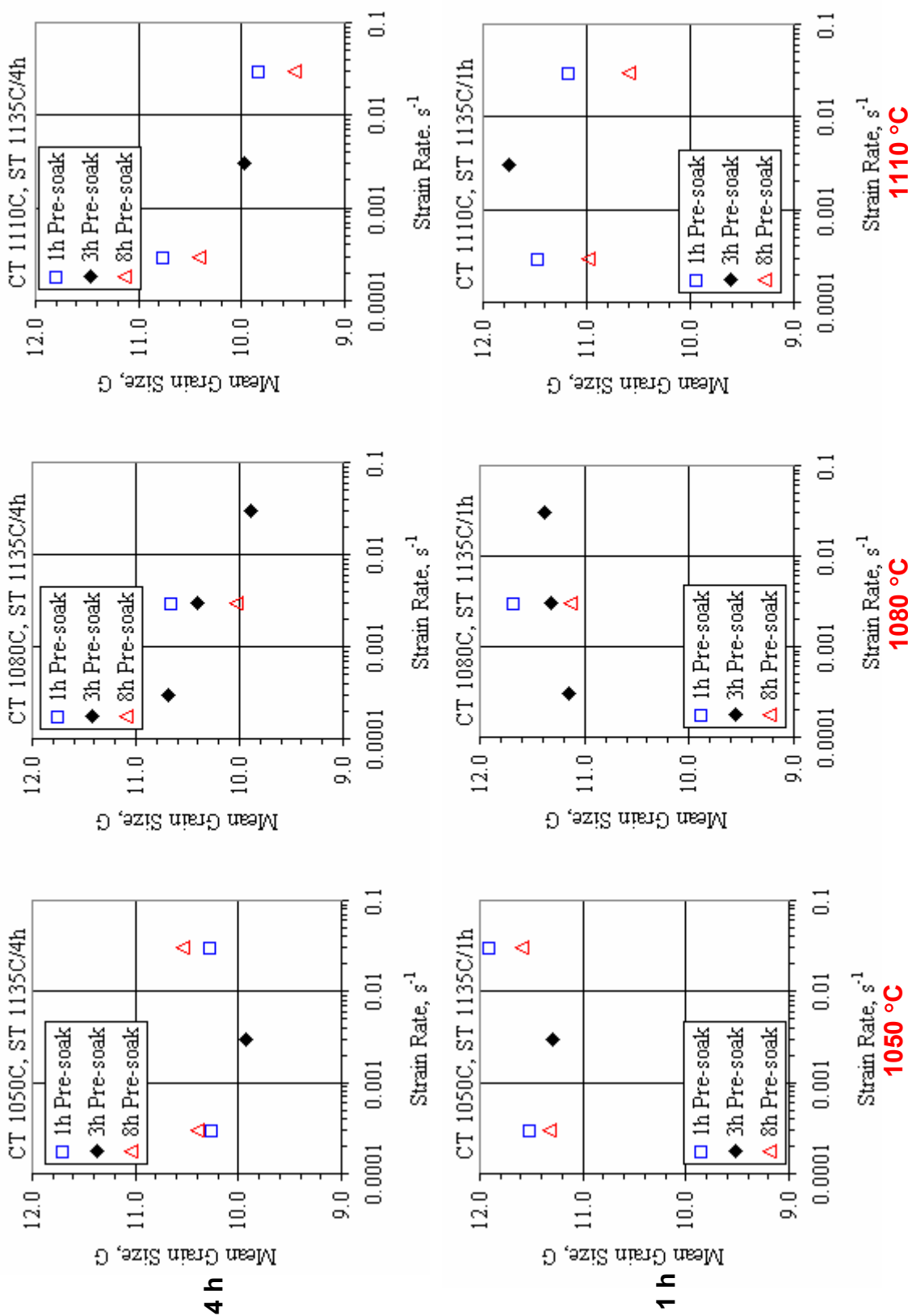


Figure 23.—Mean grain size vs. strain rate for the indicated forging presoak times and temperatures, with subsequent 1h and 4h subsolvus solution heat treatments.

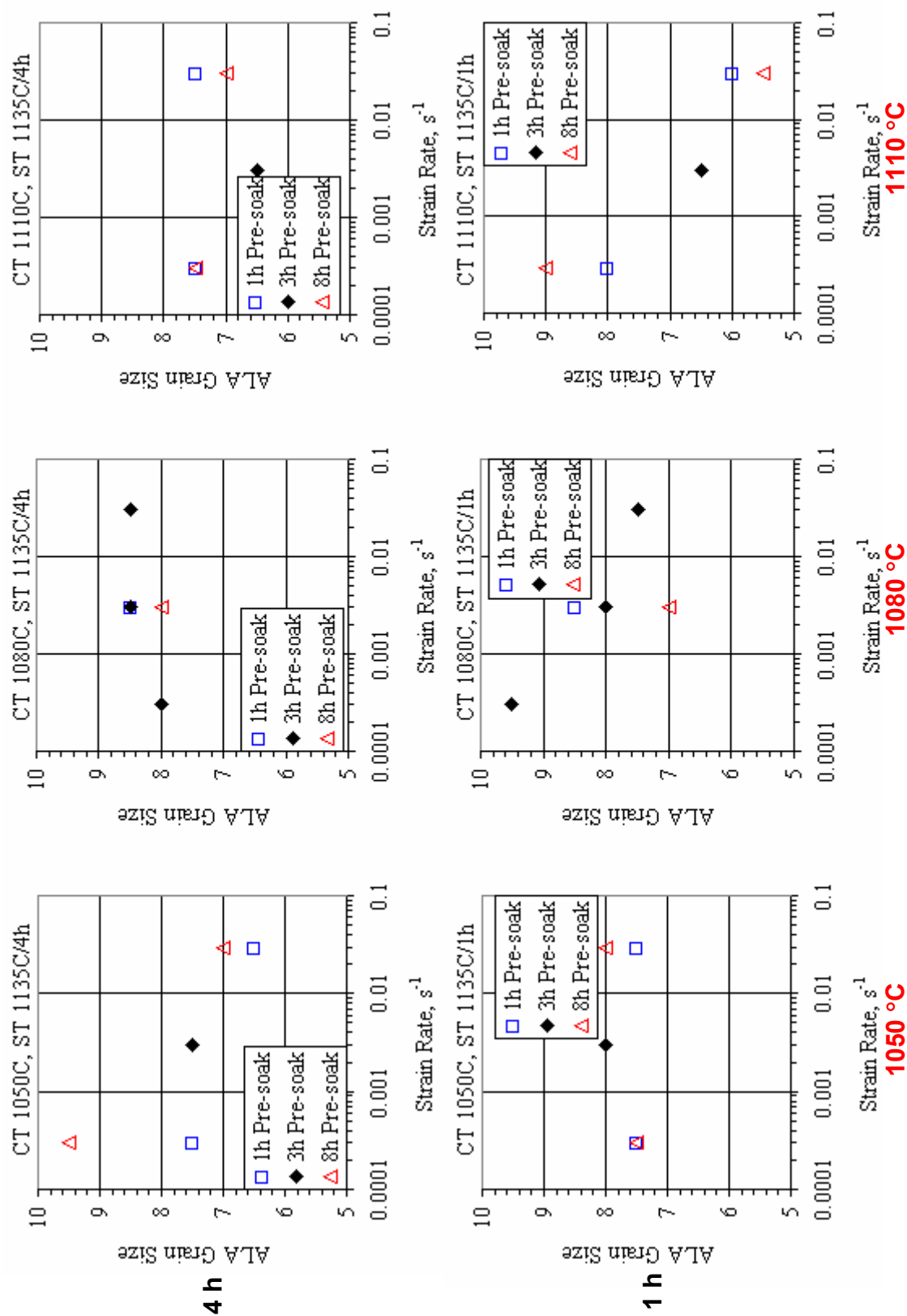


Figure 24.—As-large-as grain size vs. strain rate for the indicated forging pre-soak times and temperatures, with subsequent 1 and 4h subsolvus solution heat treatments.



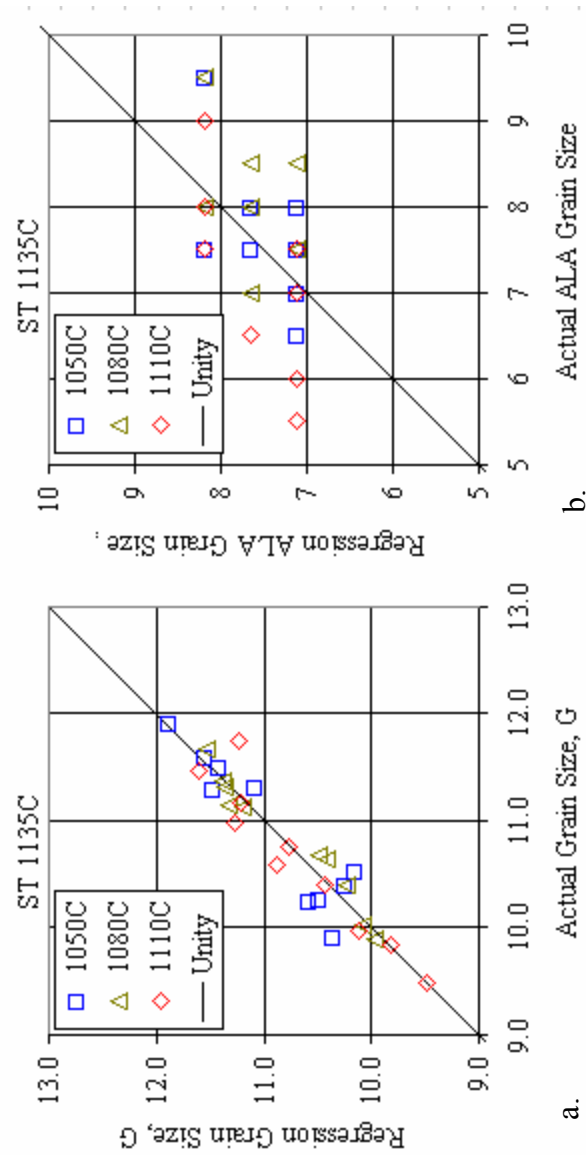


Figure 25.—Comparison of actual vs. regression subsolvus heat treated grain sizes:  
a) mean grain sizes, b) as-large-as grain sizes.

# SUP1 1050 °C

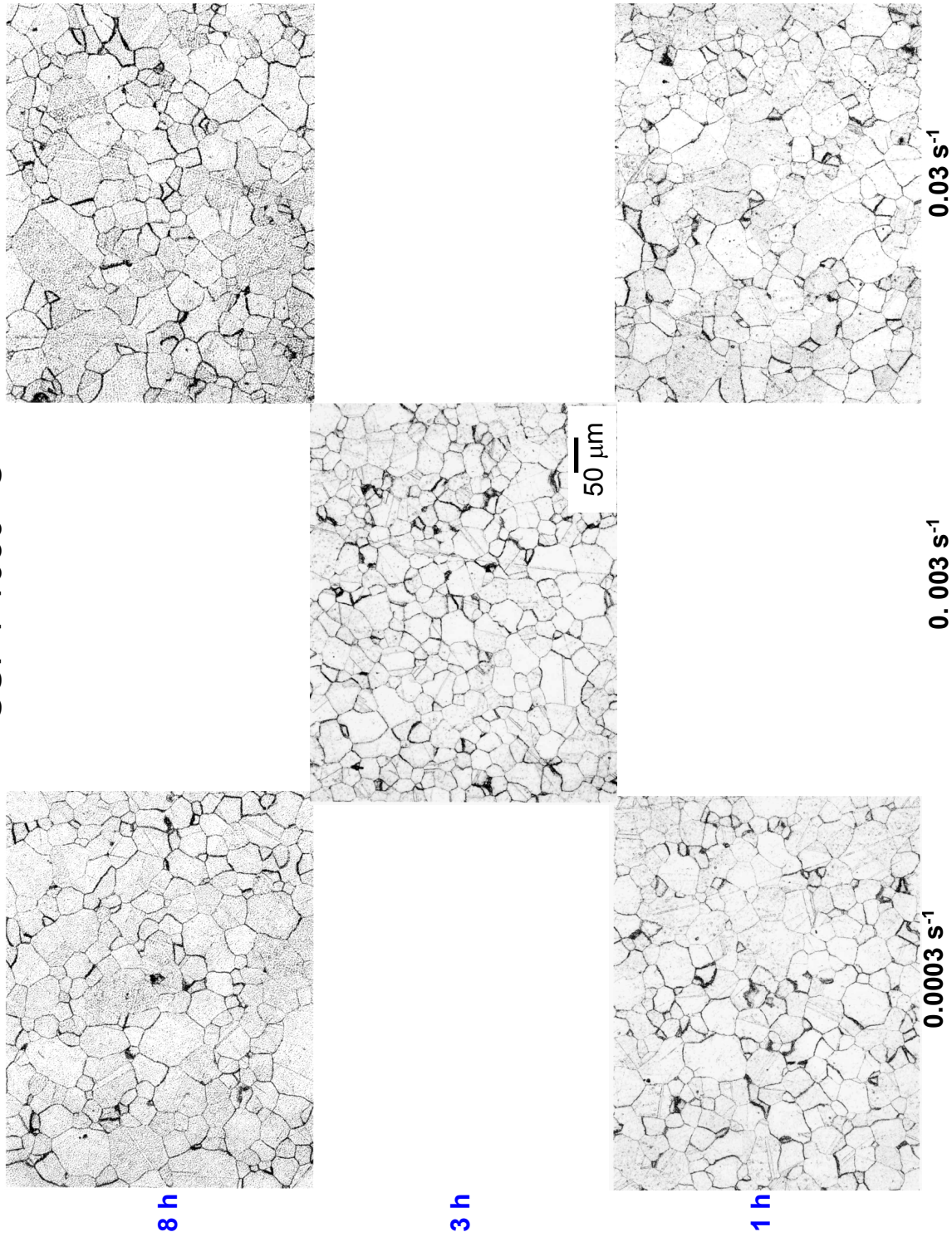
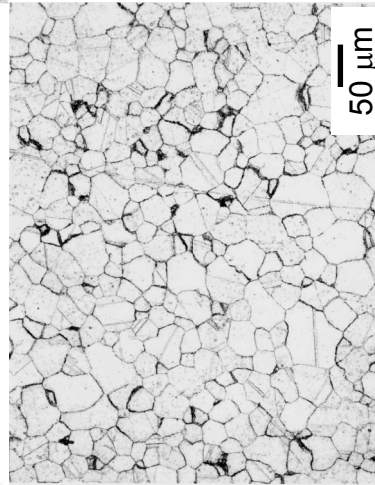
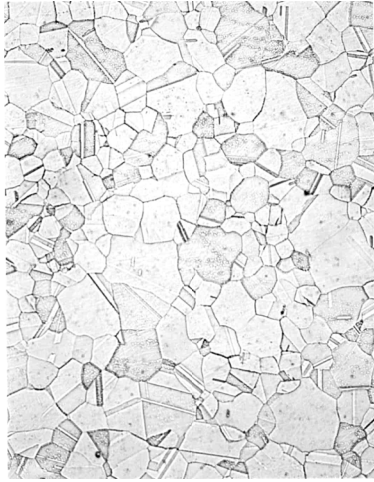
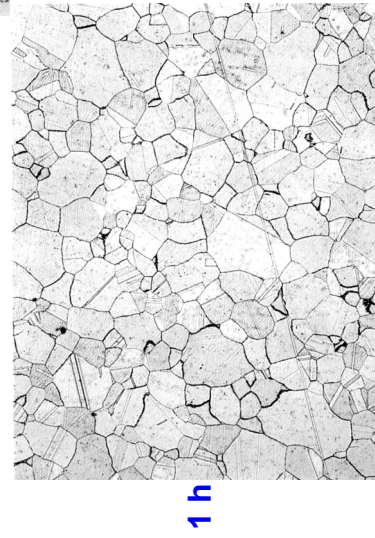


Figure 26.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 1 h.

# SUP4 1050 °C



3 h



0.0003 s<sup>-1</sup>

0.003 s<sup>-1</sup>

0.03 s<sup>-1</sup>

Figure 27.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.



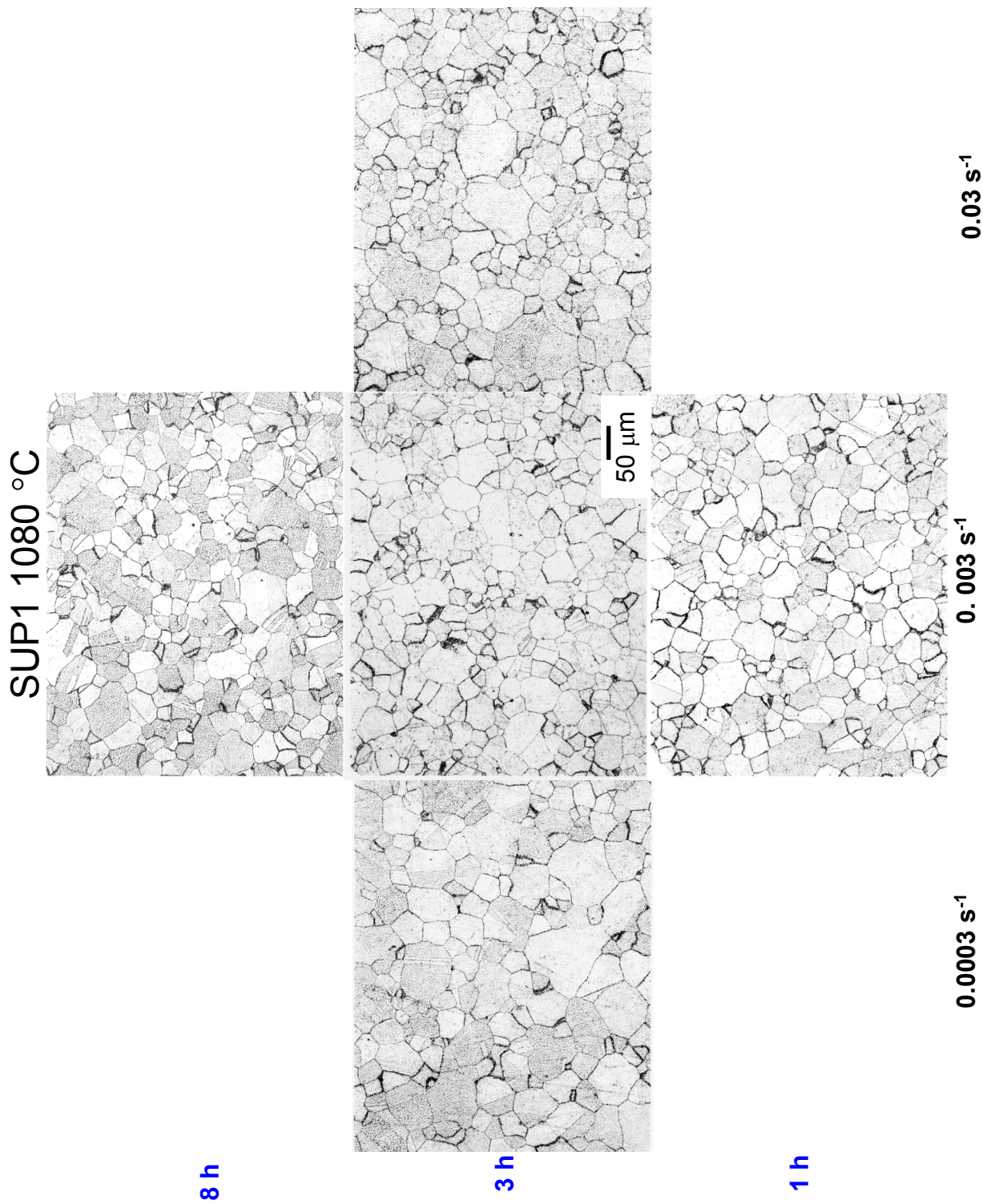


Figure 28.—Typical microstructures of specimens forged at 1080 °C with the indicated pre-soak times and strain rates, then supersolvus solution heat treated 1h.

# SUP4 1080 °C

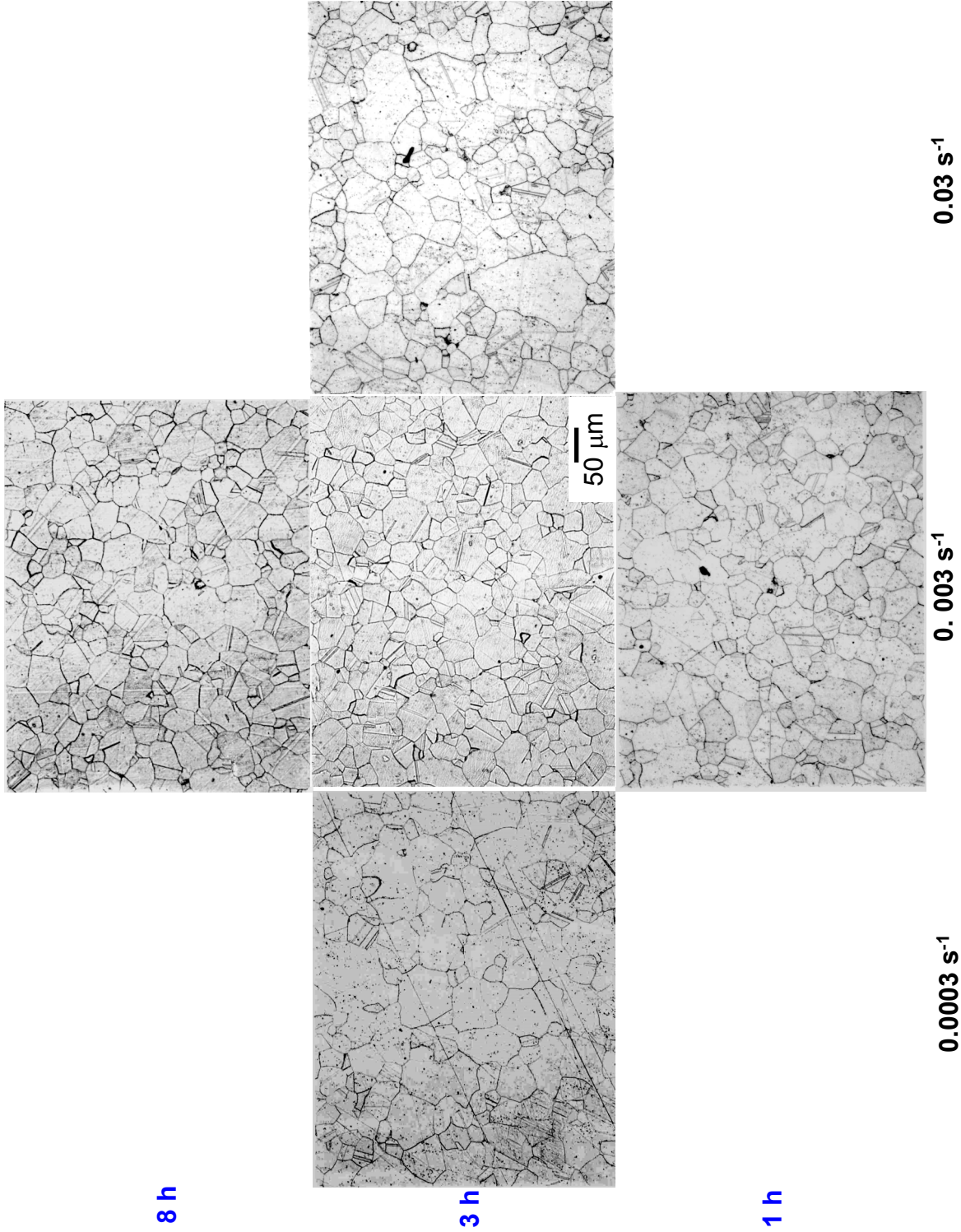


Figure 29.—Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.



# SUP1 1110 °C

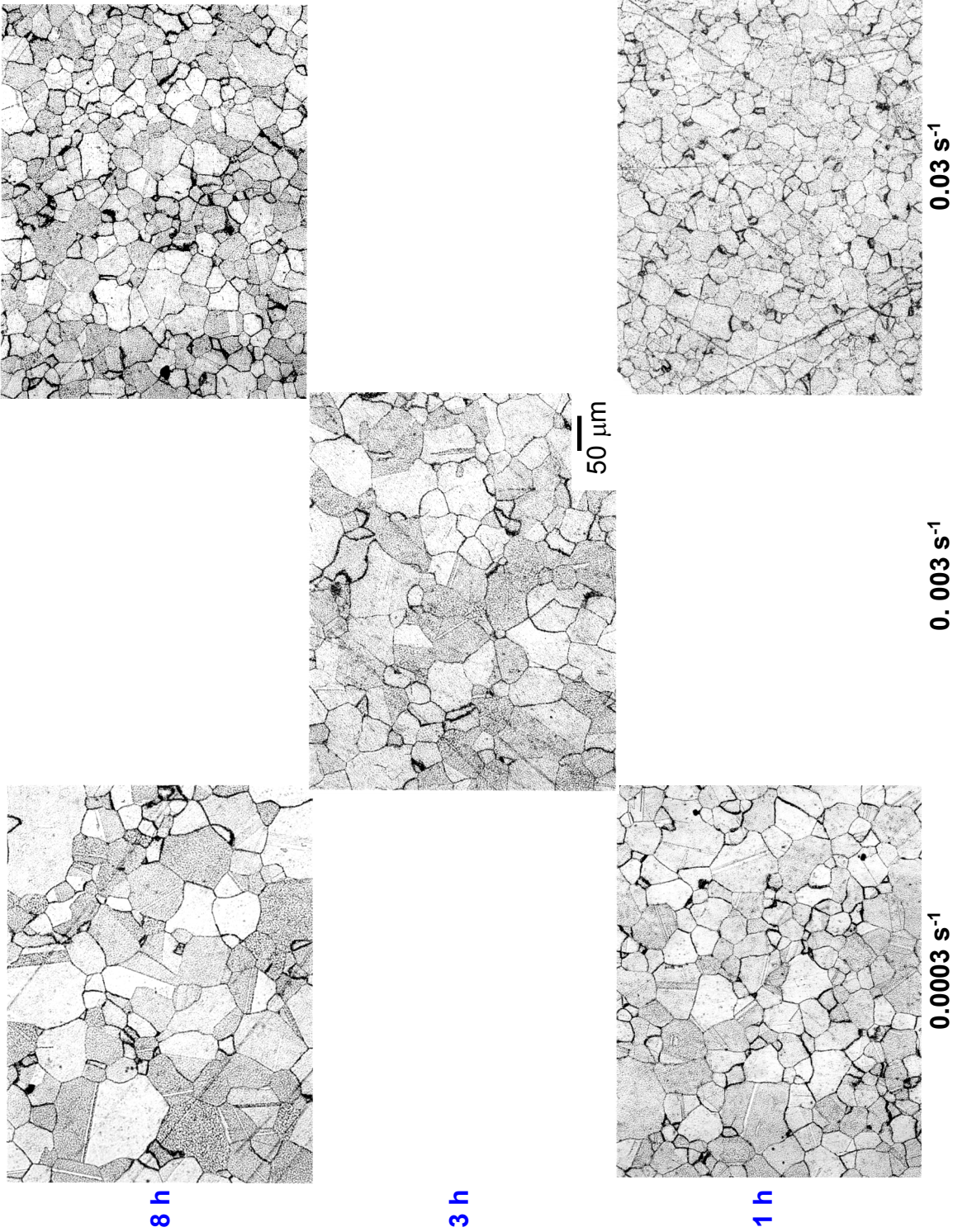


Figure 30.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 1h.

# SUP4 1110 °C

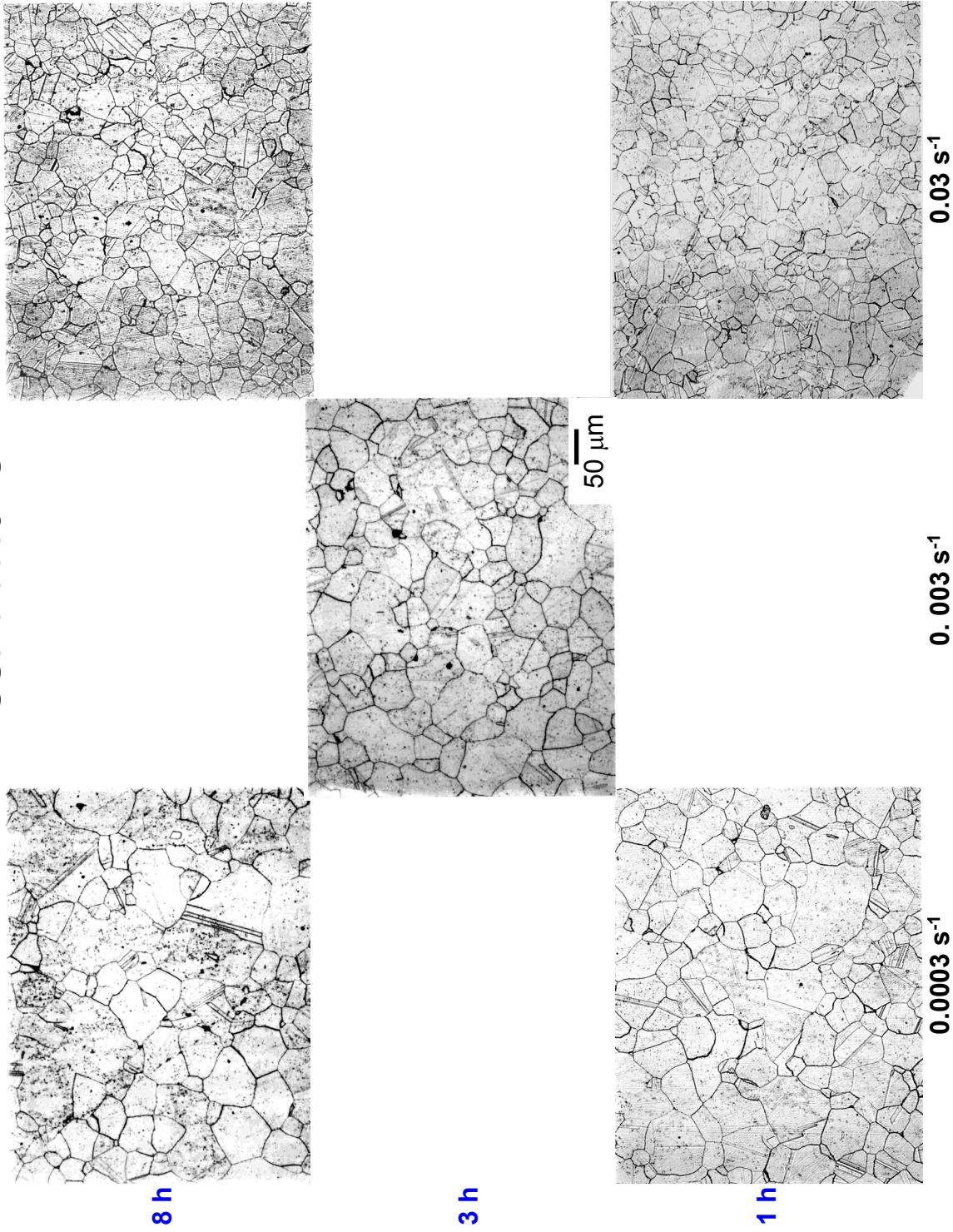


Figure 31.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.



## SUP DC Specimens 1080 °C

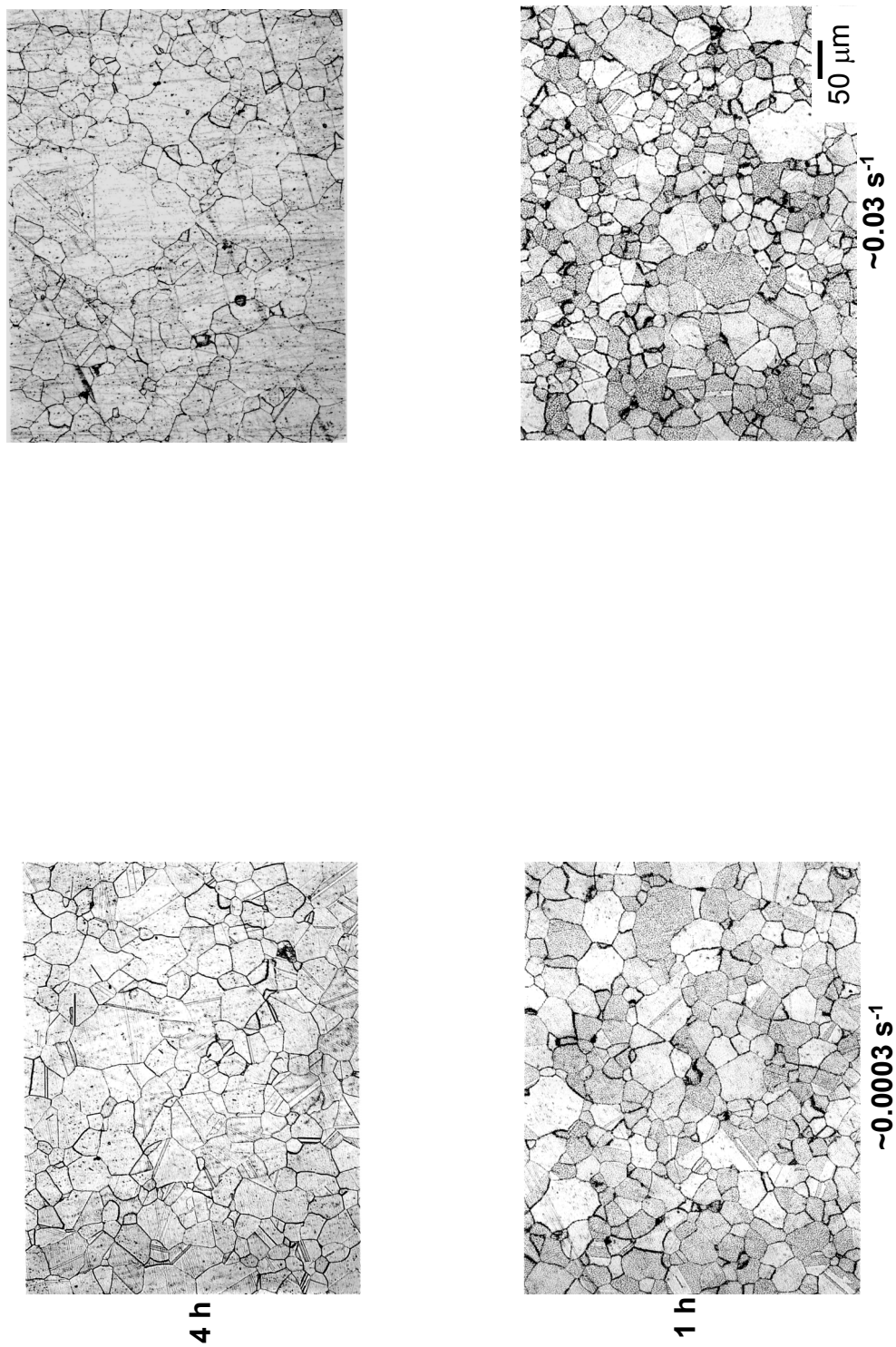


Figure 32.—Typical microstructures of double cone specimens forged at 1080 °C with the indicated approximate average strain rates, then supersolus solution heat treated 1 and 4h.



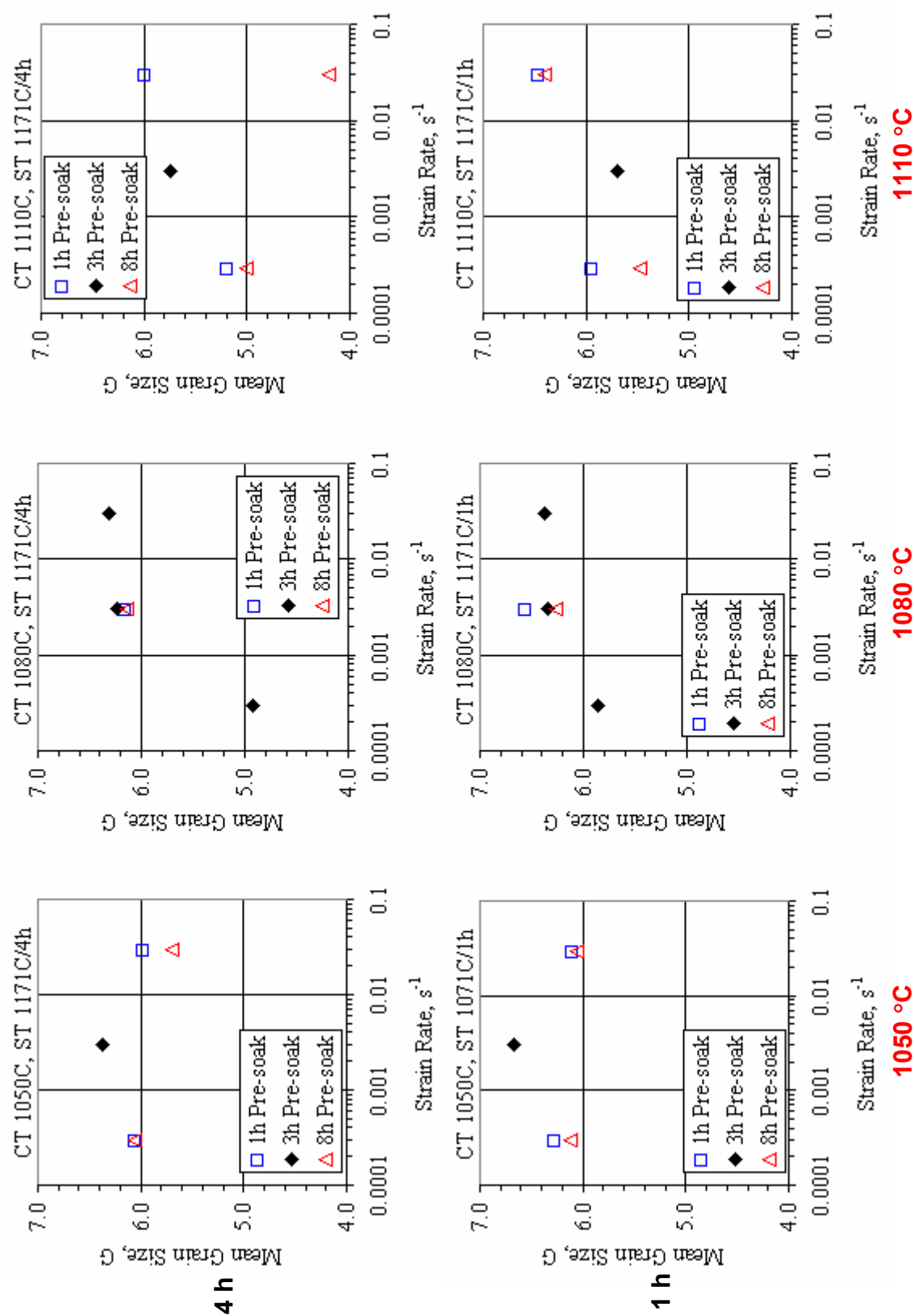
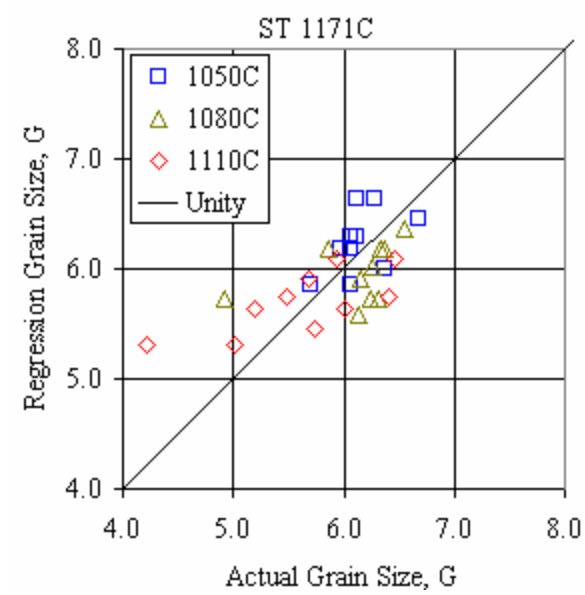


Figure 33.—Mean grain size vs. strain rate for the indicated forging pre-soak times and temperatures, with subsequent 1h and 4h supersolvus solution heat treatments.



# SUP1 1050 °C Macro

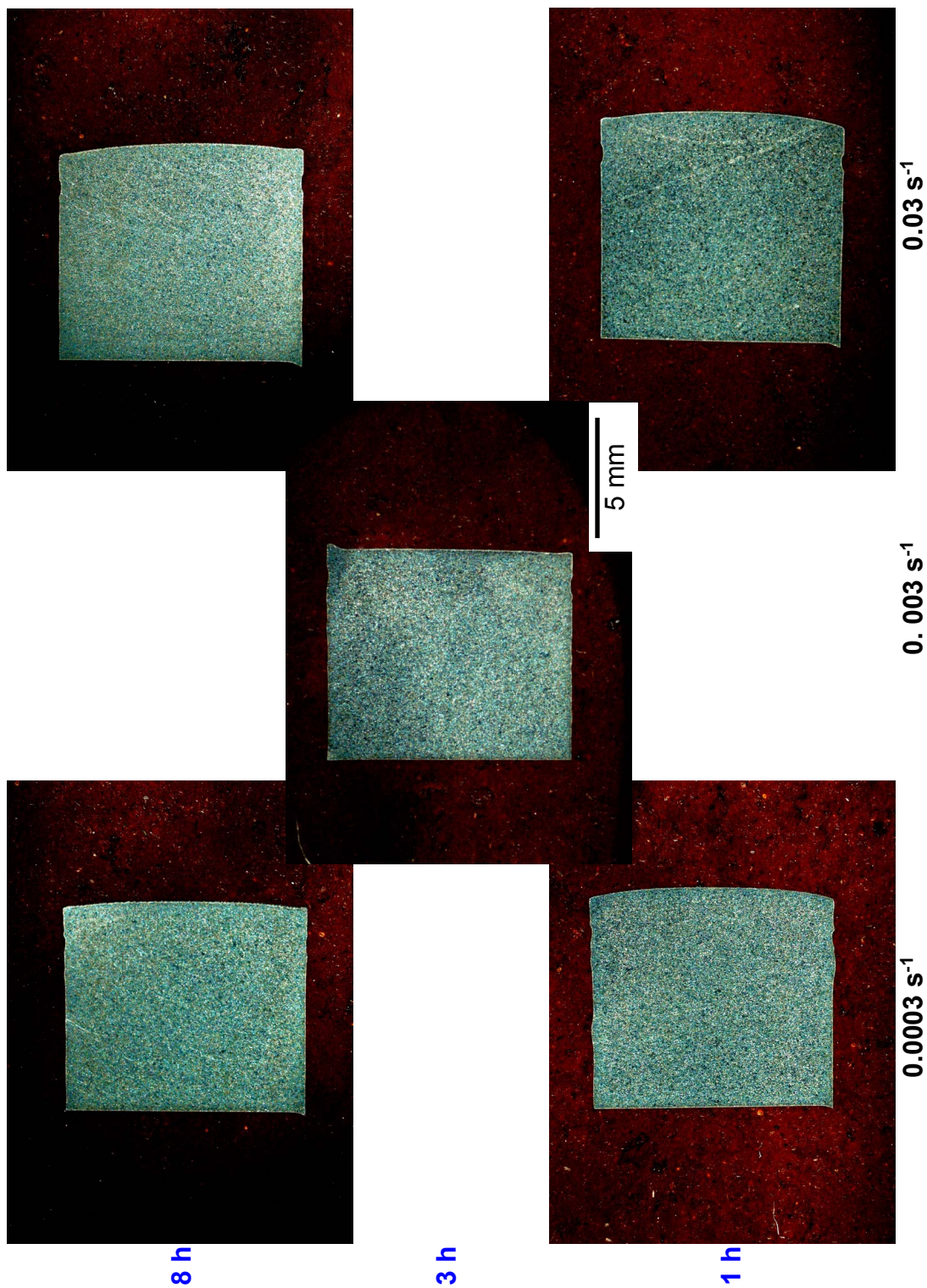


Figure 35.—Typical macrostructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 1 h.



# SUP4 1050 °C Macro

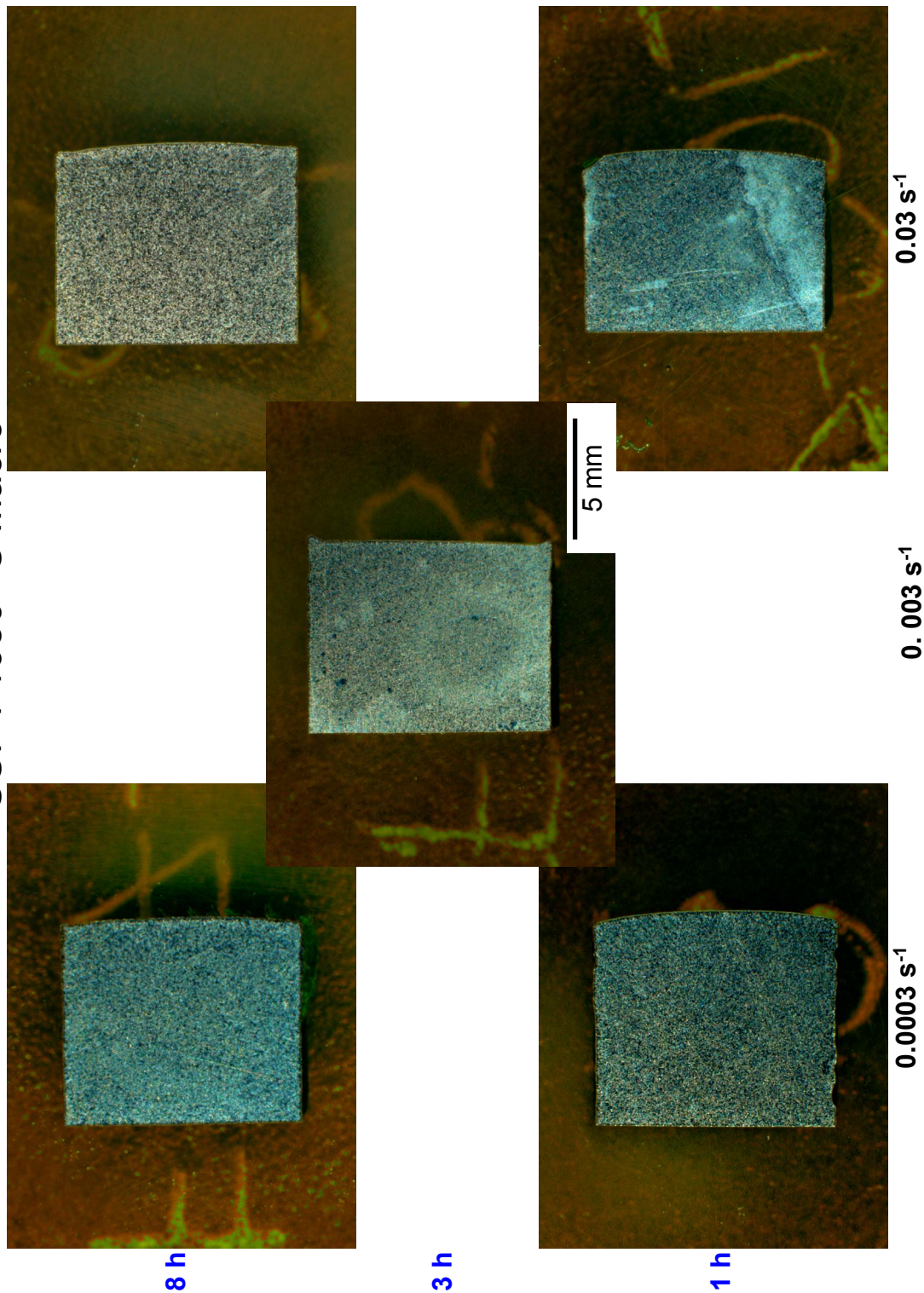


Figure 36.—Typical macrostructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.

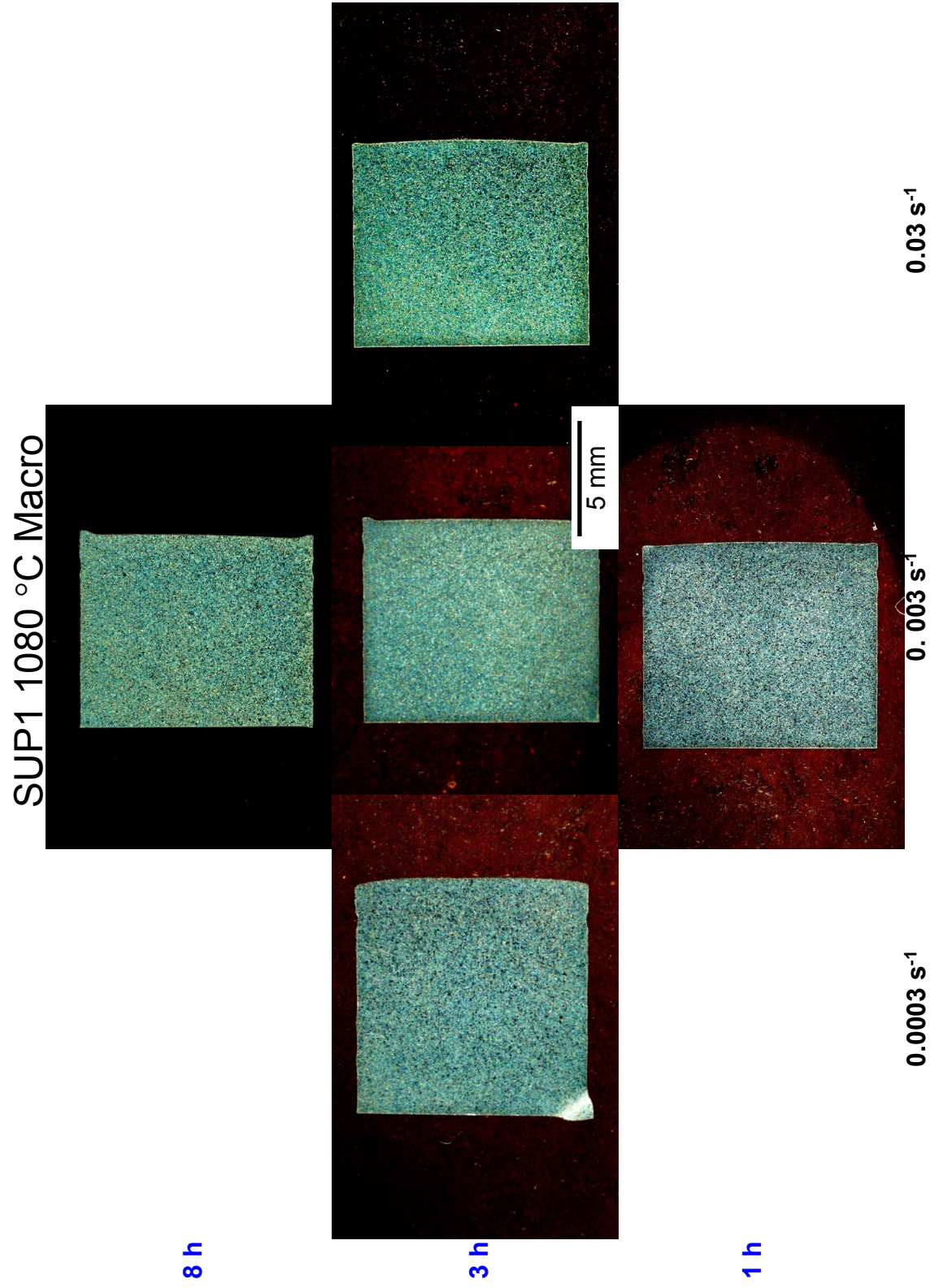


Figure 37.—Typical macrostructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 1h.



# SUP4 1080 °C Macro

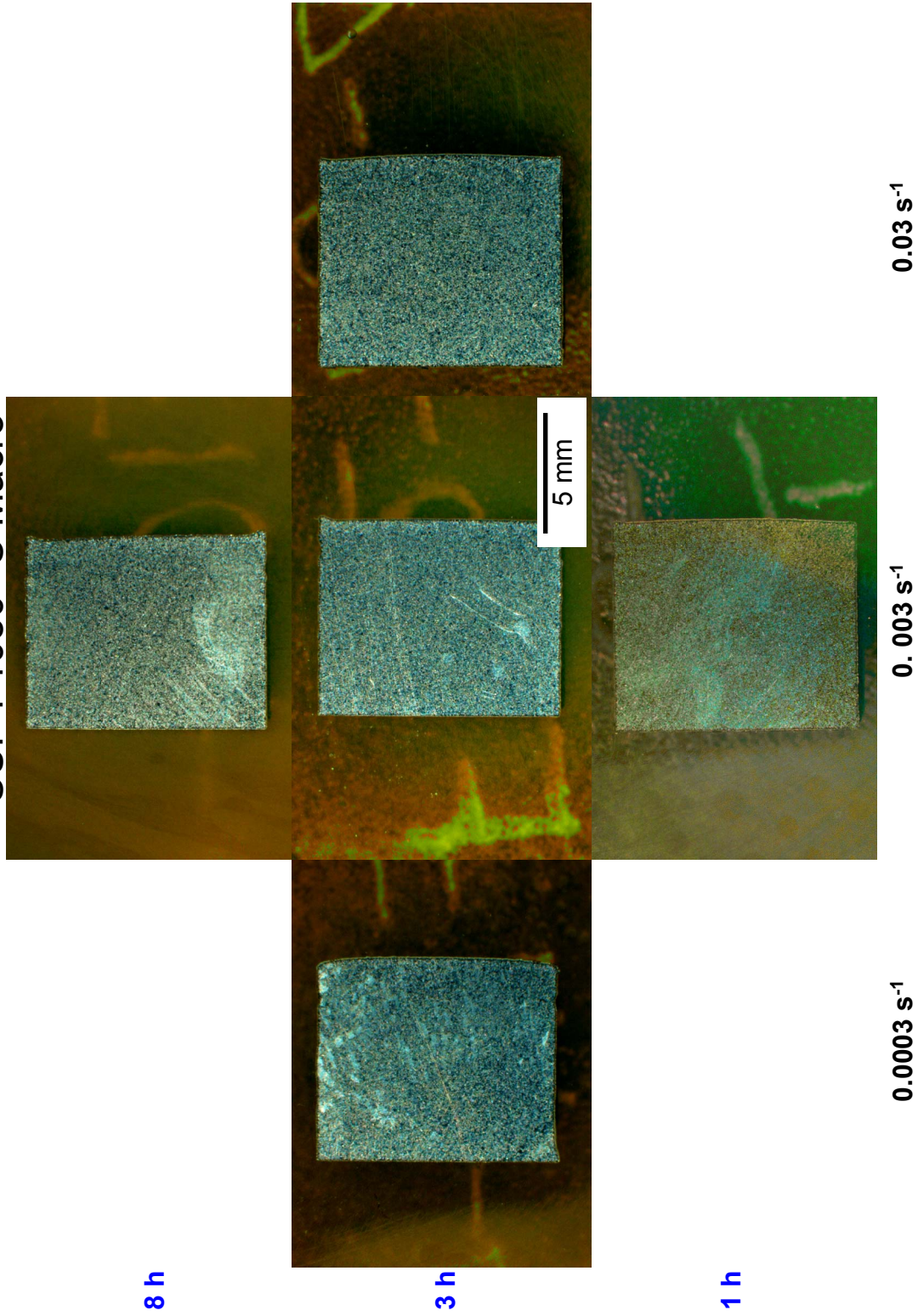


Figure 38.—Typical macrostructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.

# SUP1 1110 °C Macro

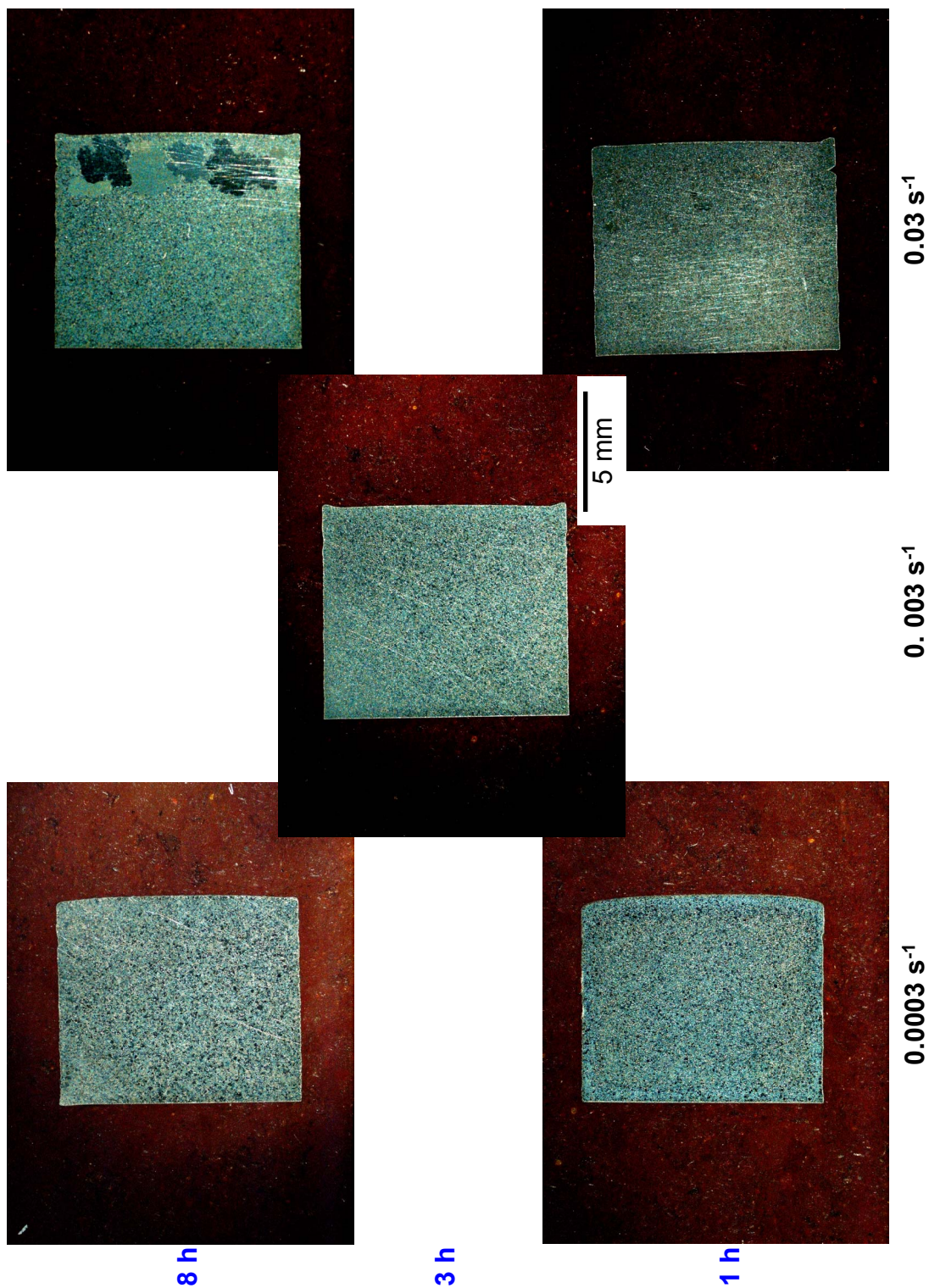


Figure 39.—Typical macrostructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 1h.



# SUP4 1110 °C Macro

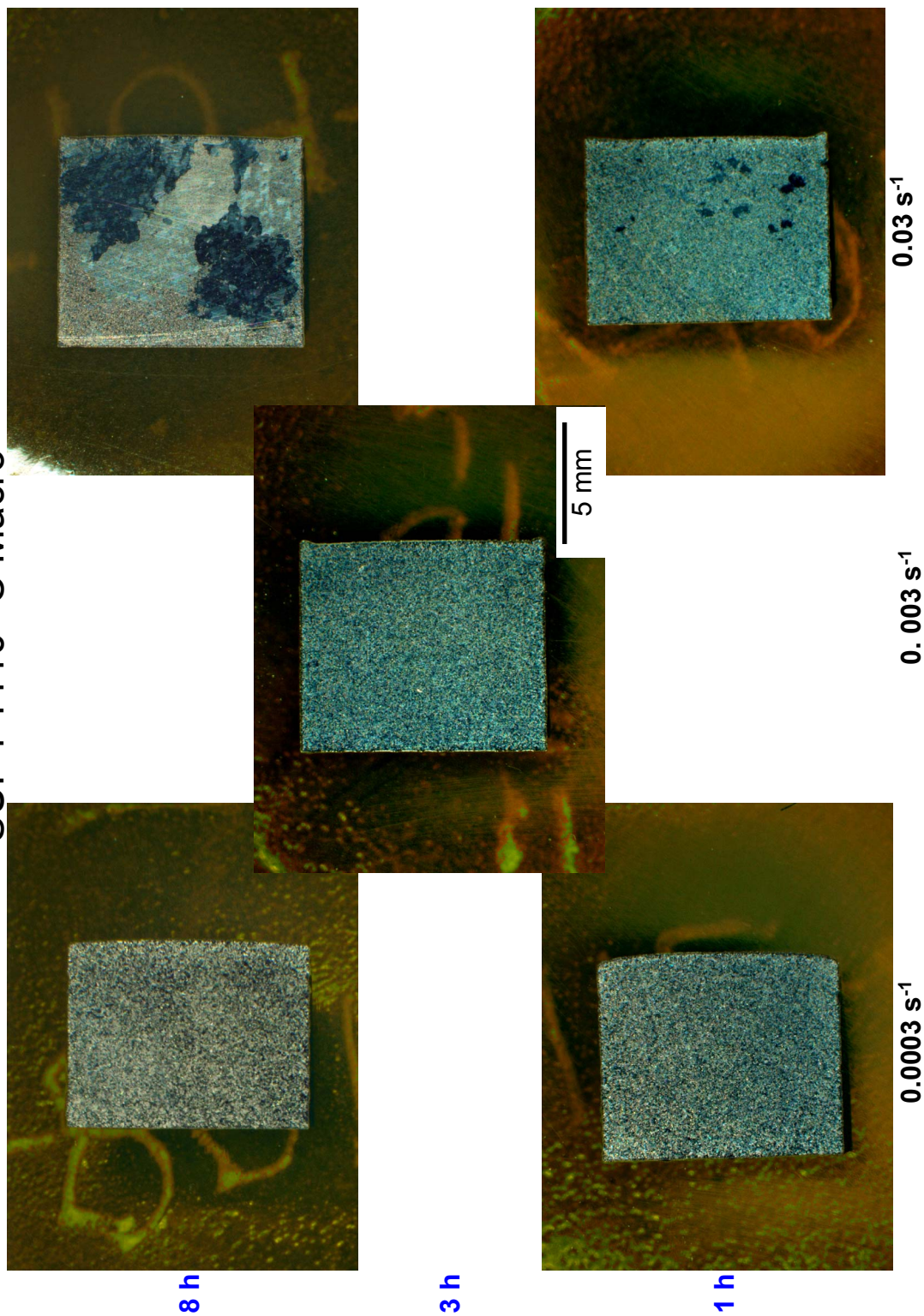


Figure 40.—Typical macrostructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then supersolvus solution heat treated 4h.



## SUP DC Specimens 1080 °C Macro

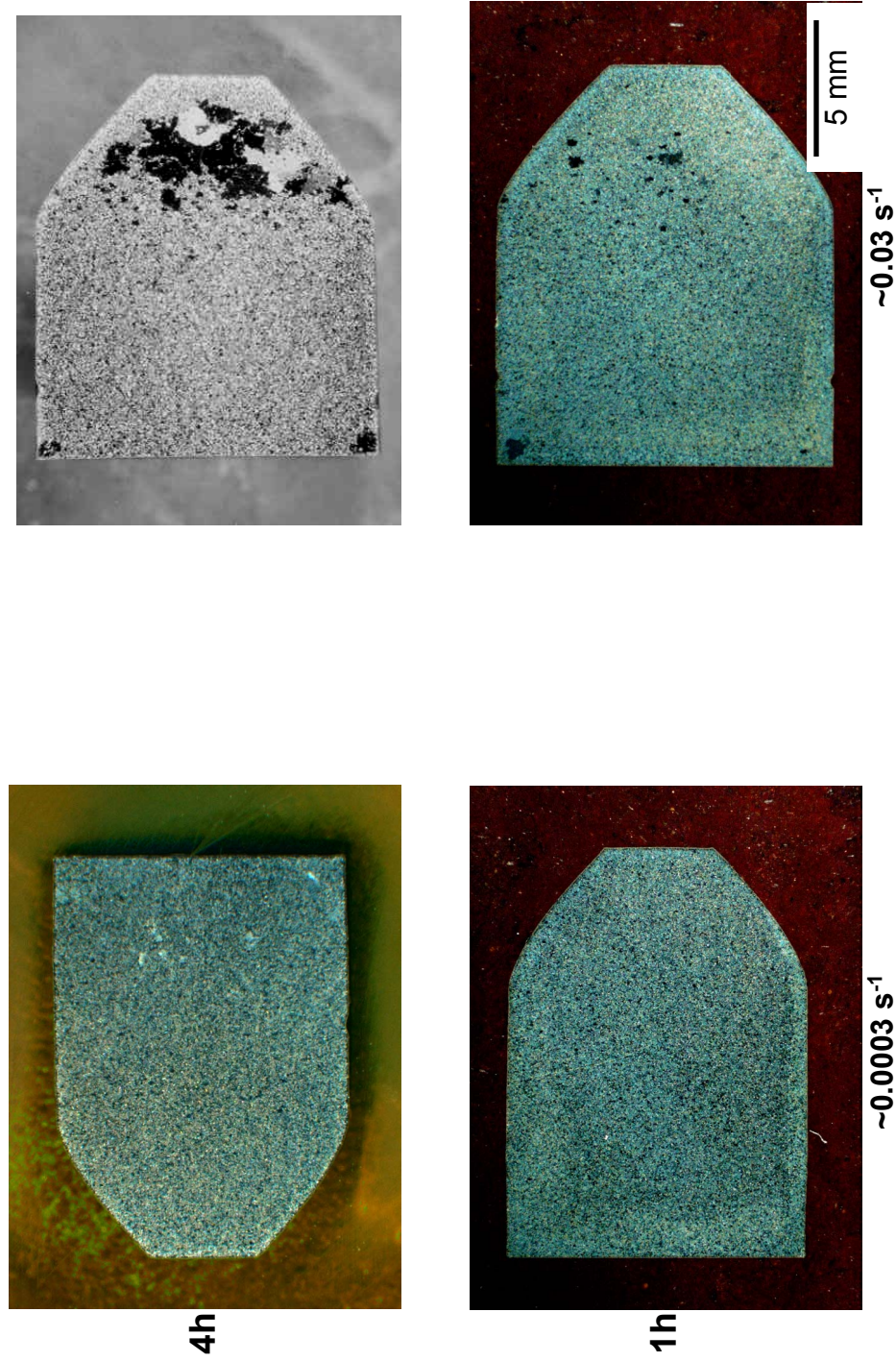


Figure 41.—Typical macrostructures of double cone specimens forged at 1080 °C with the indicated approximate average strain rates, then supersolvus solution heat treated 1 and 4h.

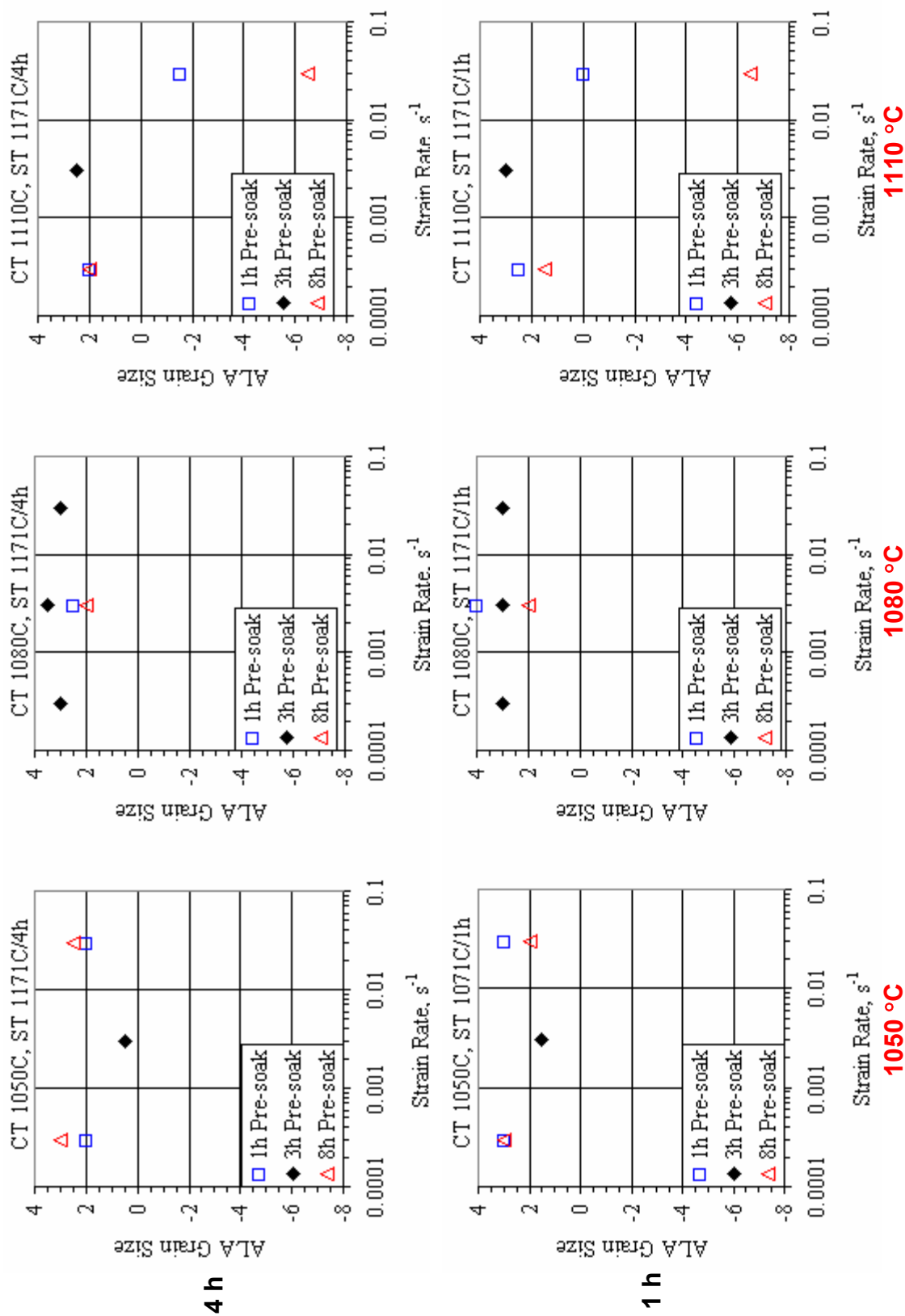


Figure 42.—As-large-as grain size vs. strain rate for the indicated forging pre-soak times and temperatures, with subsequent 1h and 4h supersolvus solution heat treatments.

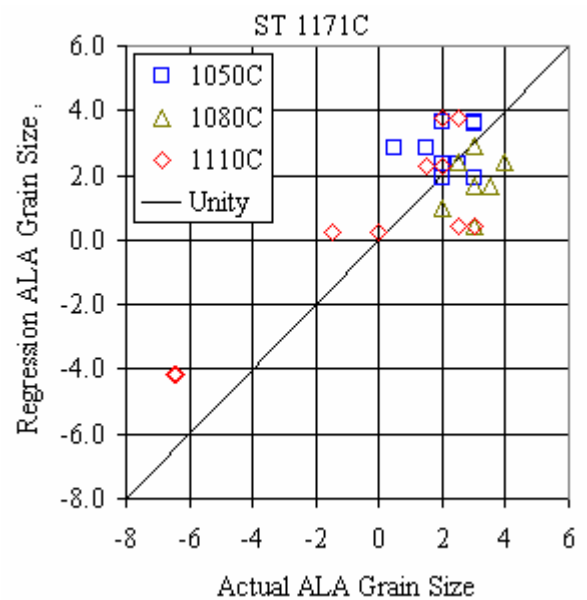


Figure 43.—Comparison of actual vs. regression supersolvus heat treated as-large-as grain sizes.

SUBP1 1050 °C

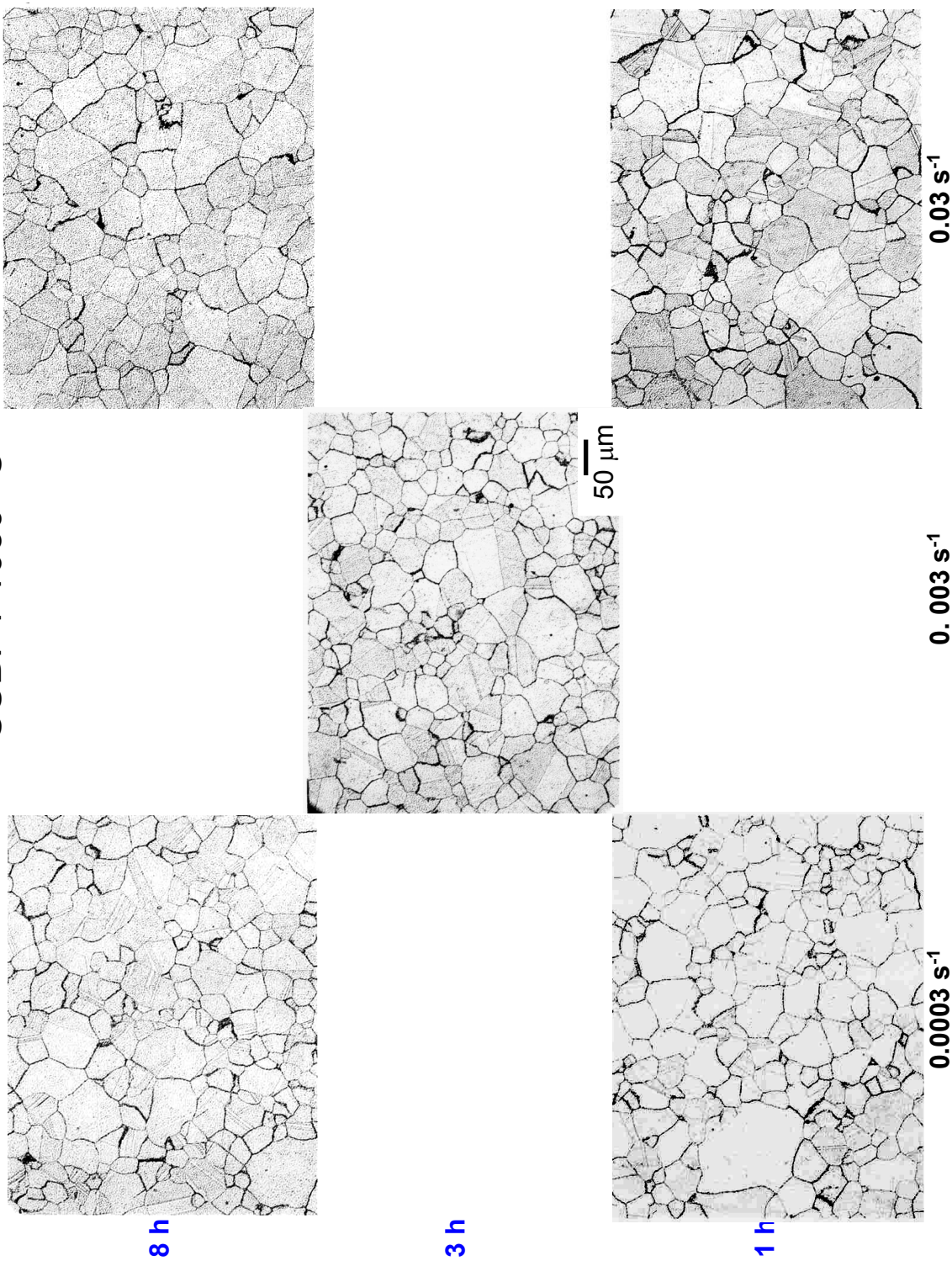


Figure 44.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then 1 h subsolvus plus 1 h supersolvus solution heat treated.



# SUBP4 1050 °C

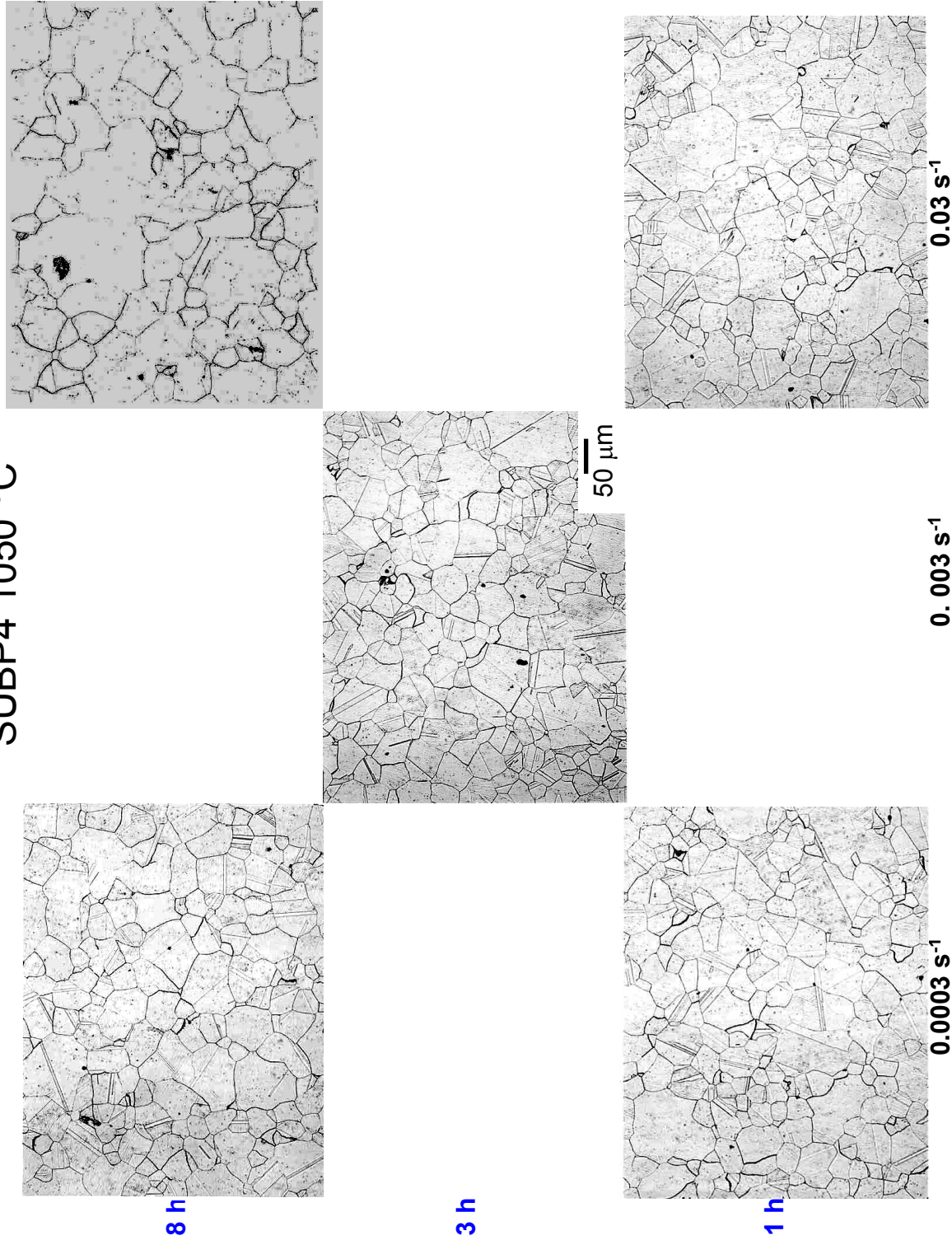


Figure 45.—Typical microstructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then 1 h subsolvus plus 4 h supersolvus solution heat treated.

SUBP1 1080 °C

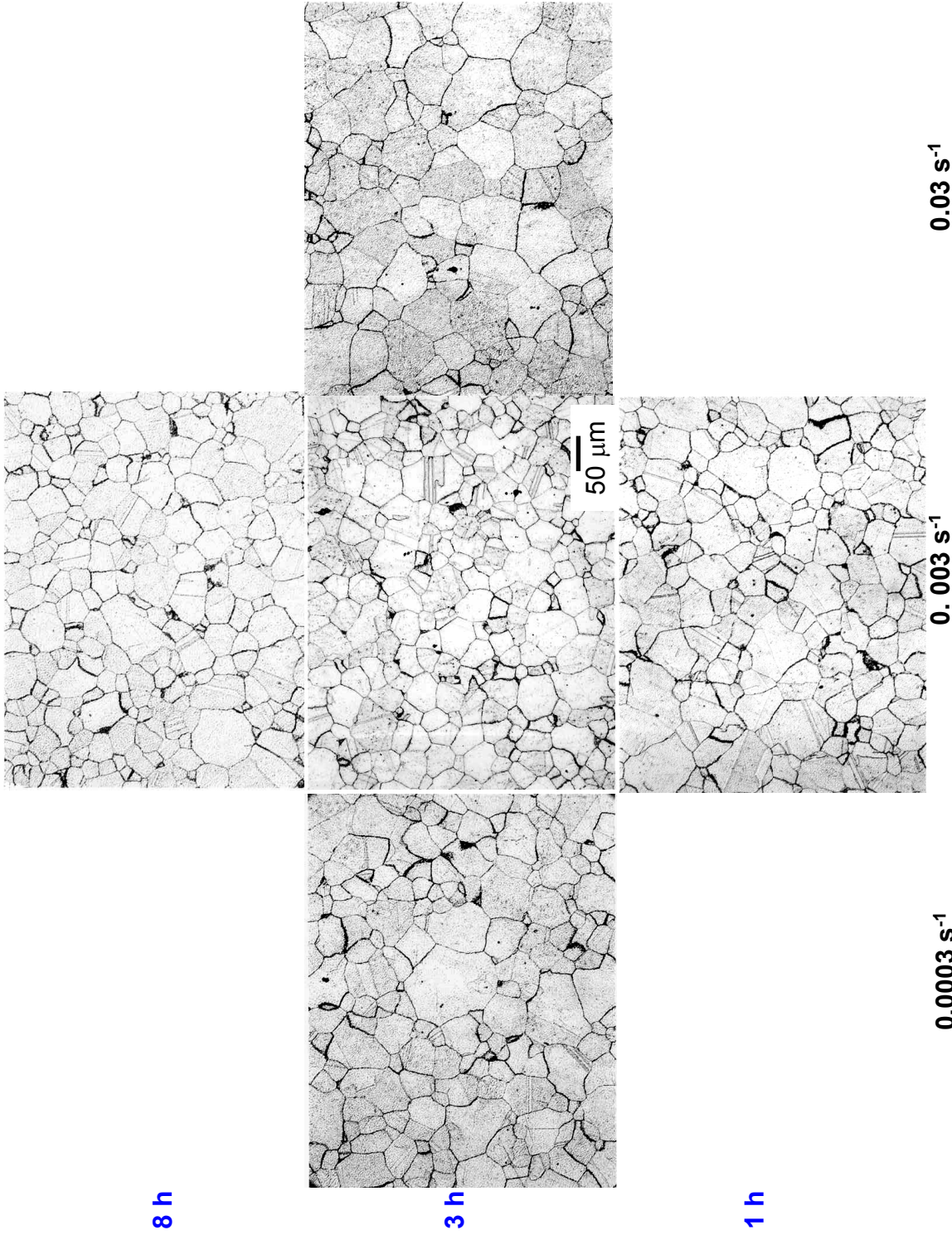


Figure 46.—Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then 1 h subsolvus plus 1 h supersolvus solution heat treated.



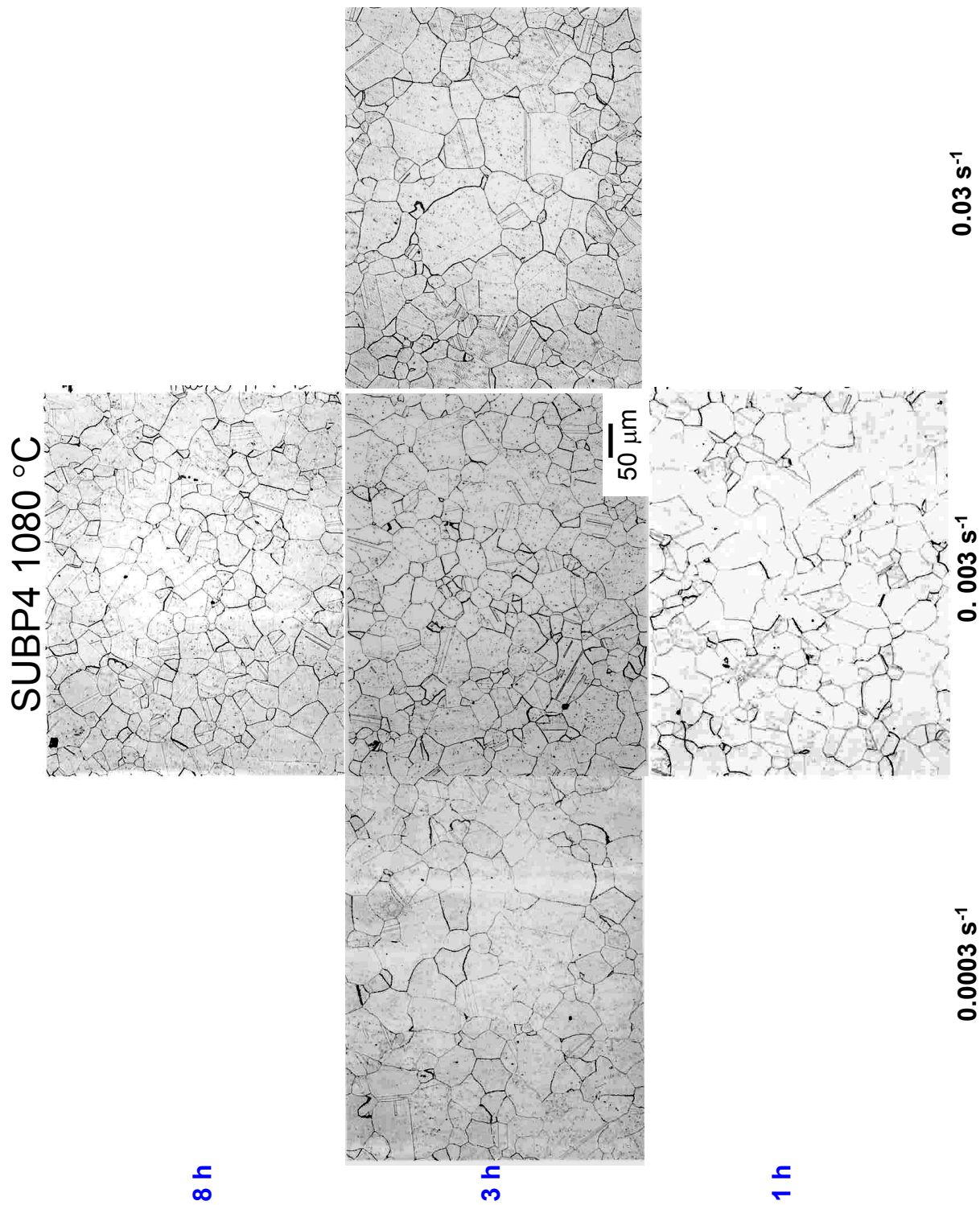


Figure 47.—Typical microstructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then 1 h subsolvus plus 4 h supersolvus solution heat treated.

SUBP1 1110 °C

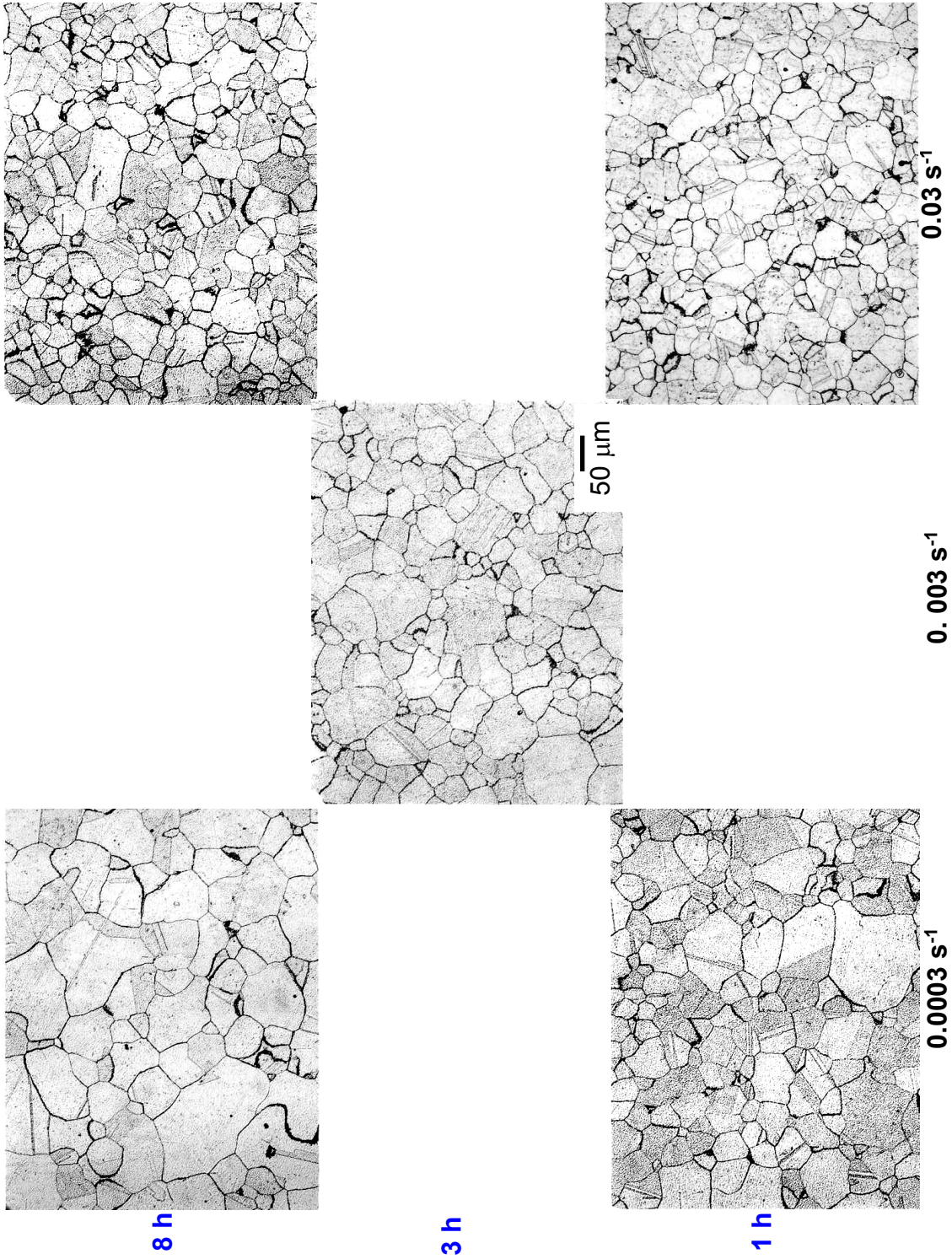


Figure 48.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then 1 h subsolvus plus 1 h supersolvus solution heat treated.



# SUBP4 1110 °C

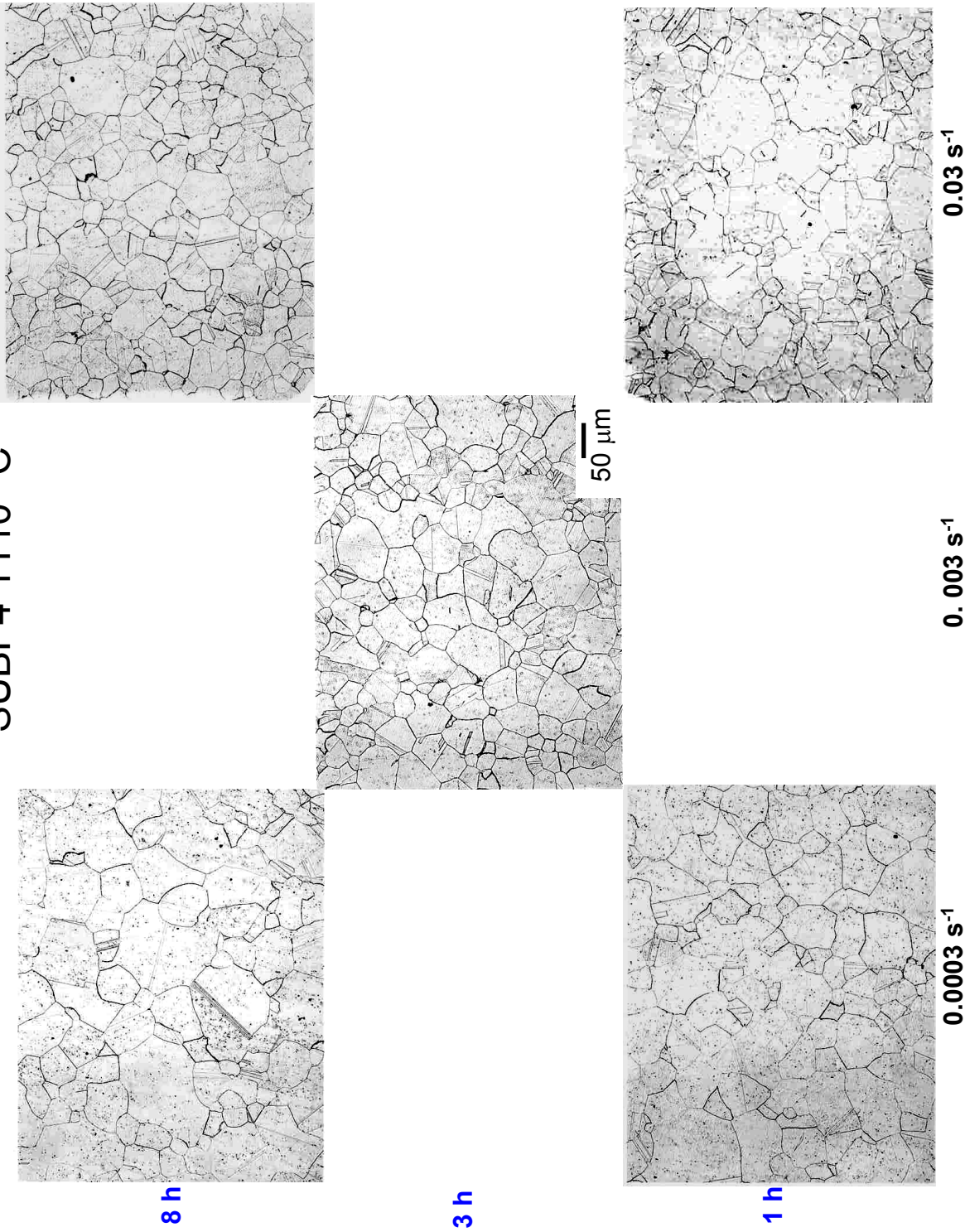


Figure 49.—Typical microstructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 4h supersolvus solution heat treated.

## SUBP DC Specimens 1080 °C

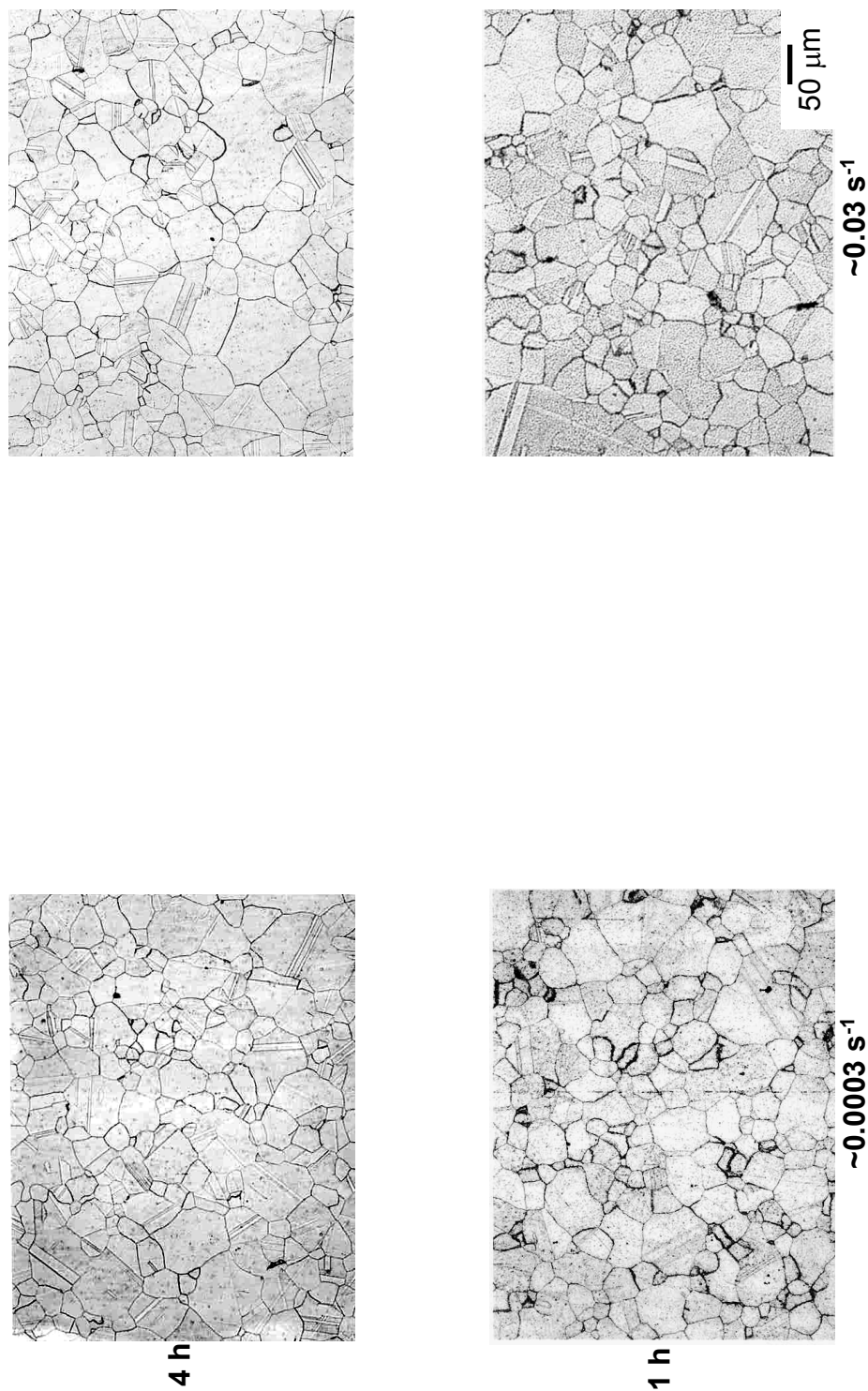


Figure 50.—Typical microstructures of double cone specimens forged at 1080 °C with the indicated approximate average strain rates, then 1h subsolvus plus 1h and 4h supersolvus solution heat treated.

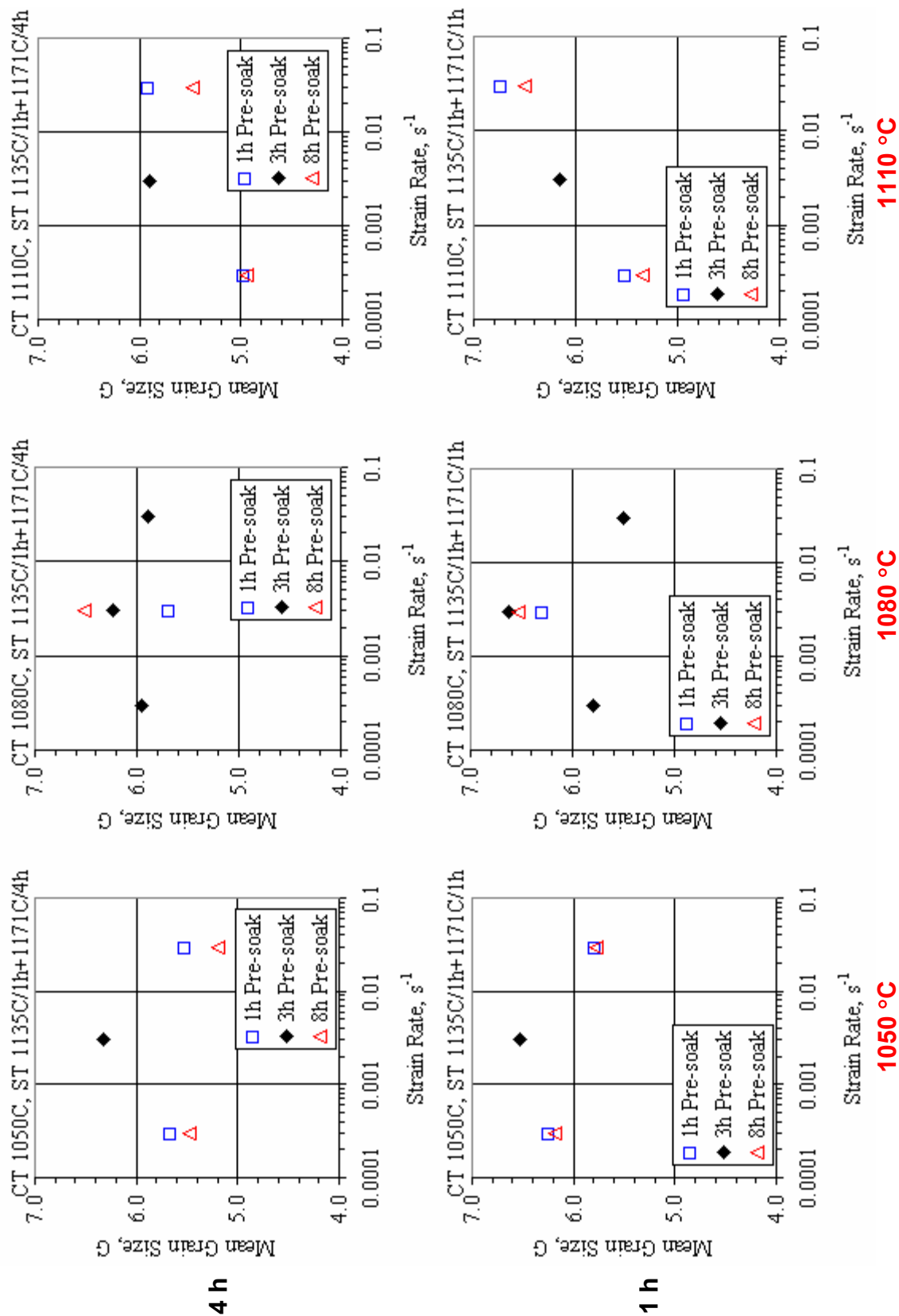


Figure 51.—Mean grain size vs. strain rate for the indicated forging pre-soak times and temperatures, with subsequent 1h subsolvus plus 1h and 4h supersolvus solution heat treatments.

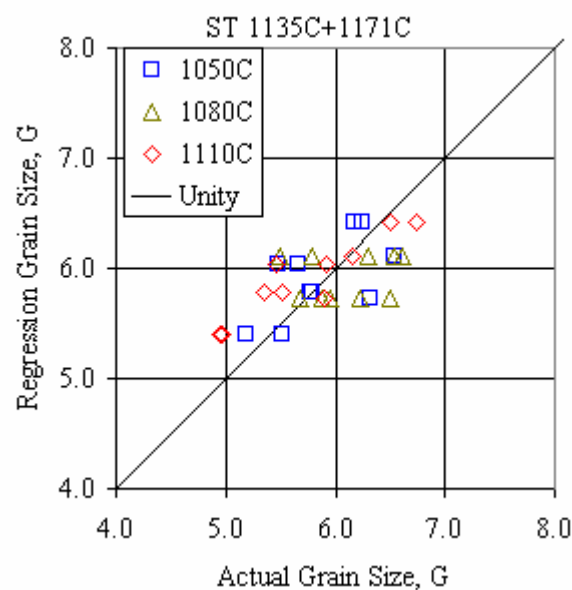


Figure 52.—Comparison of actual vs. regression subsolvus plus supersolvus heat treated mean grain sizes.



# **SUBP1 1050 °C Macro**

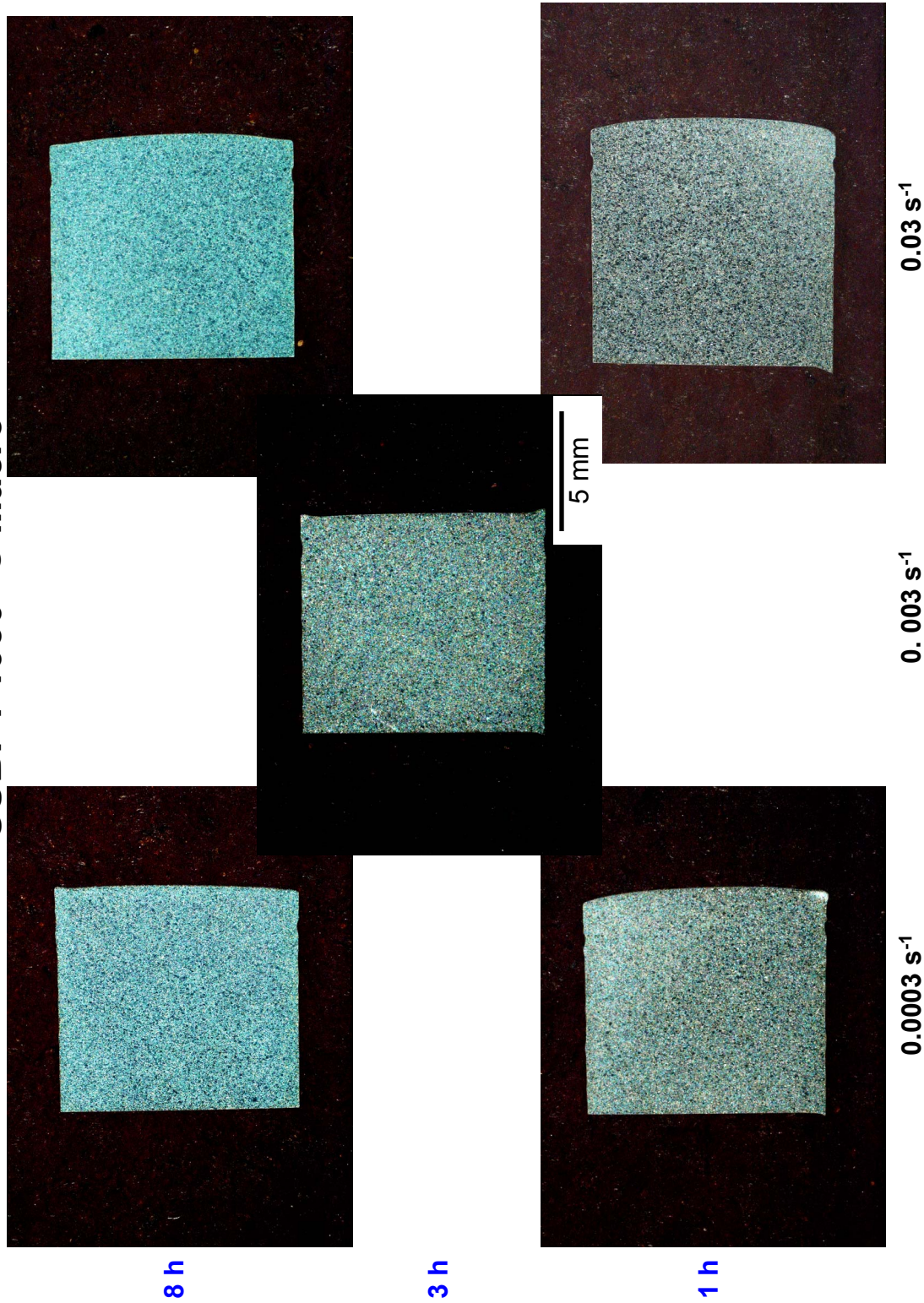


Figure 53.—Typical macrostructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 1h supersolvus solution heat treated.

# **SUBP4 1050 °C Macro**

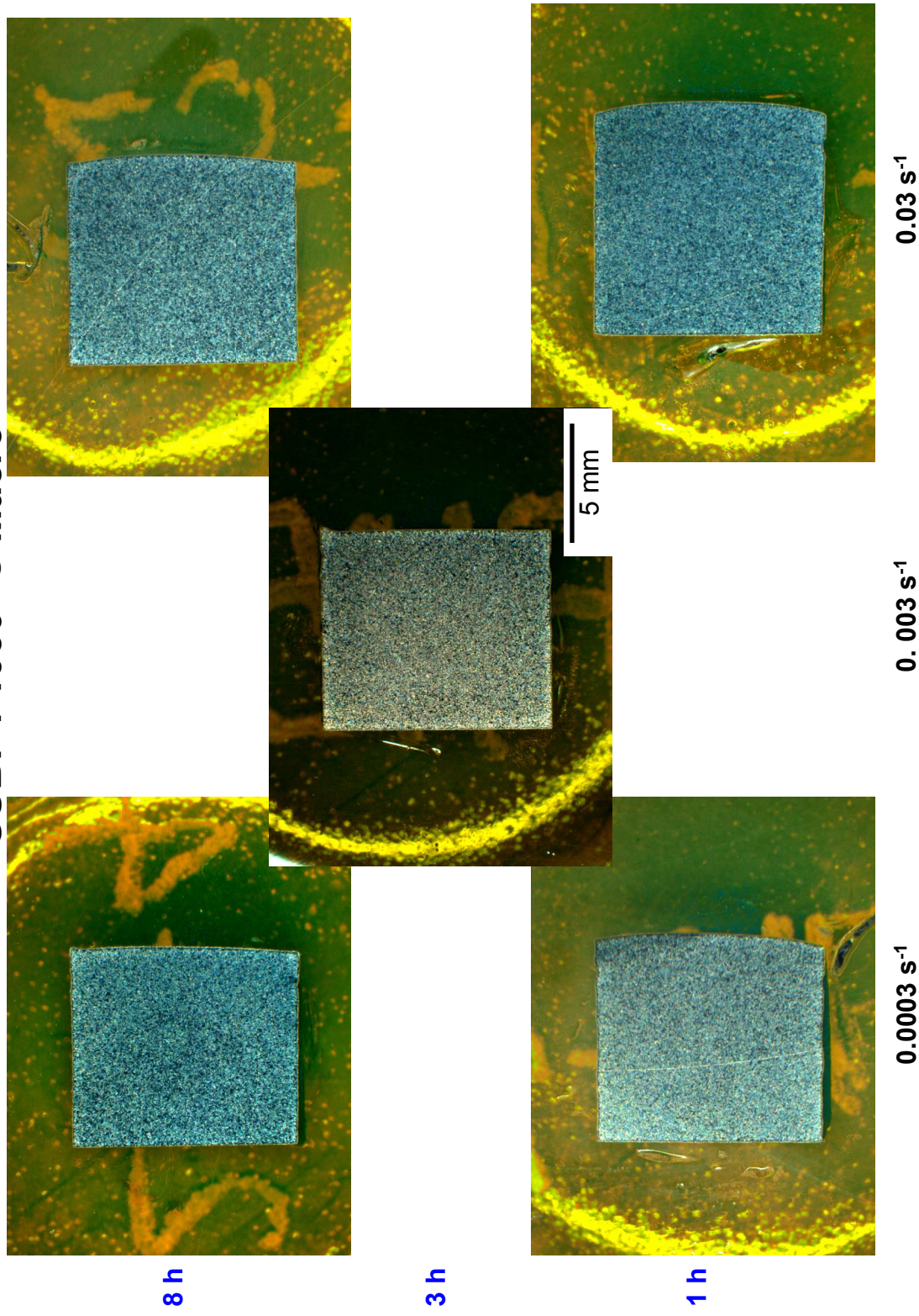


Figure 54.—Typical macrostructures of specimens forged at 1050 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 4h supersolvus solution heat treated.



# **SUBP1 1080 °C Macro**

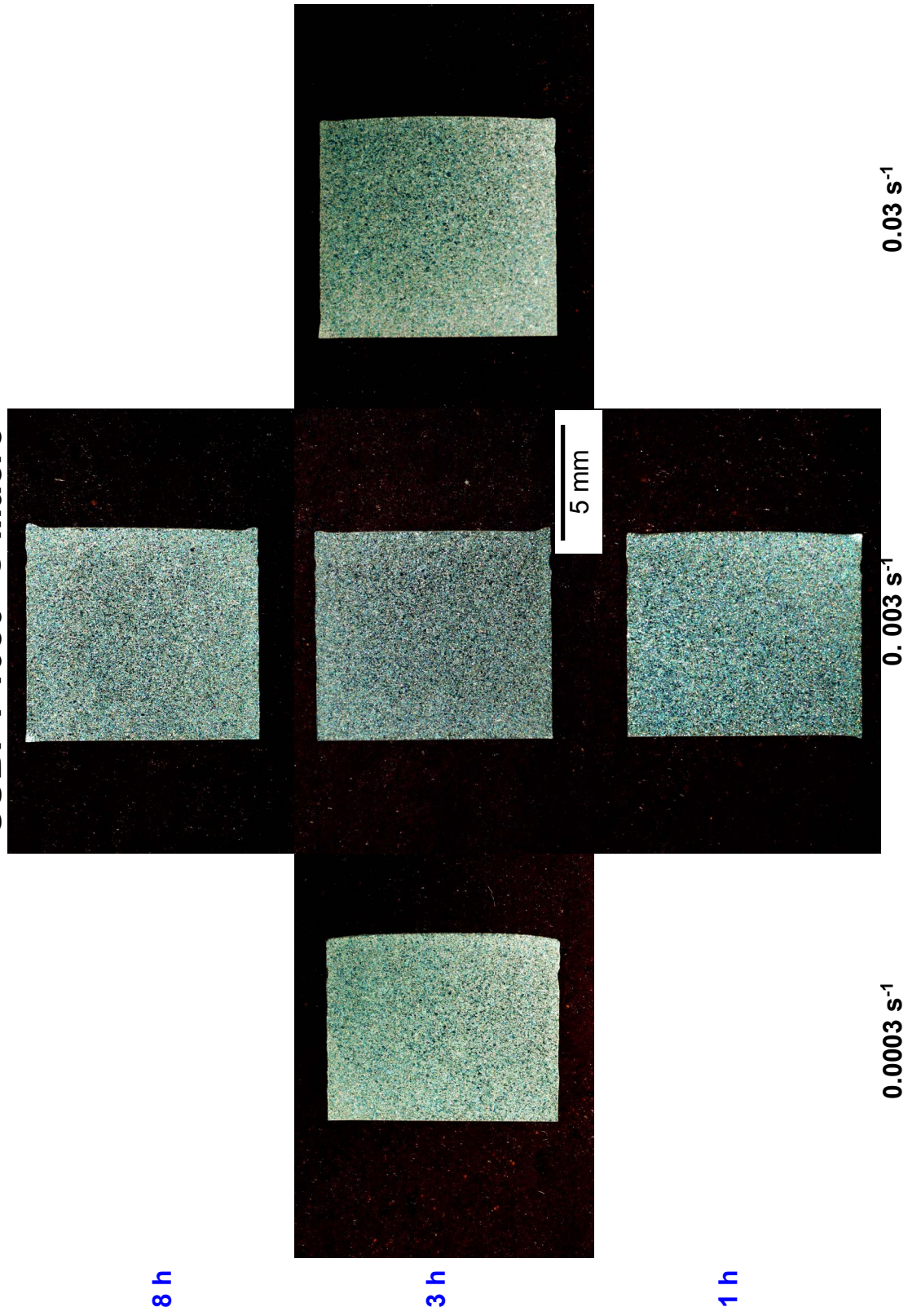


Figure 55.—Typical macrostructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 1h supersolvus solution heat treated.



# **SUBP4 1080 °C Macro**

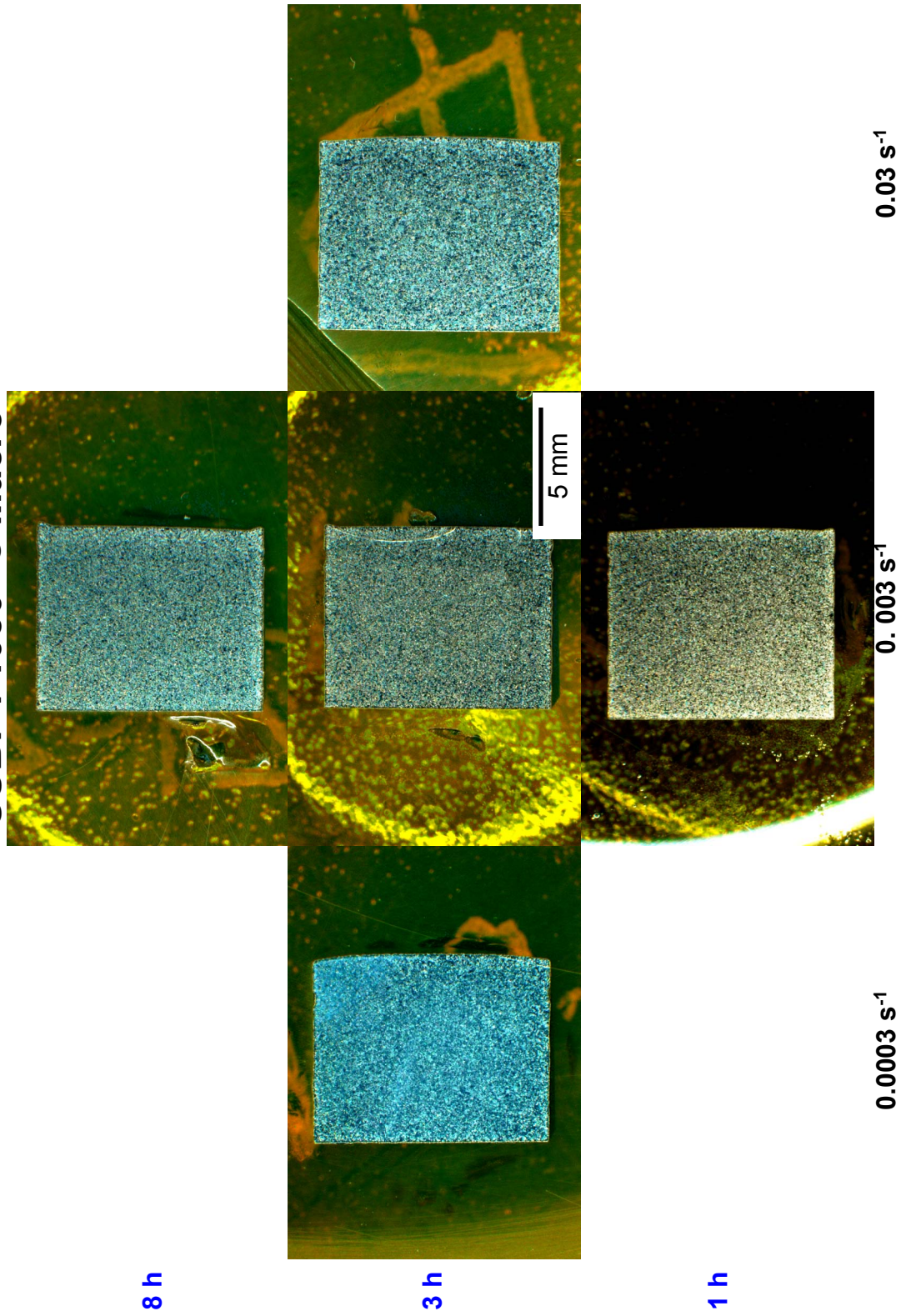


Figure 56.—Typical macrostructures of specimens forged at 1080 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 4h supersolvus solution heat treated.

# SUBP1 1110 °C Macro

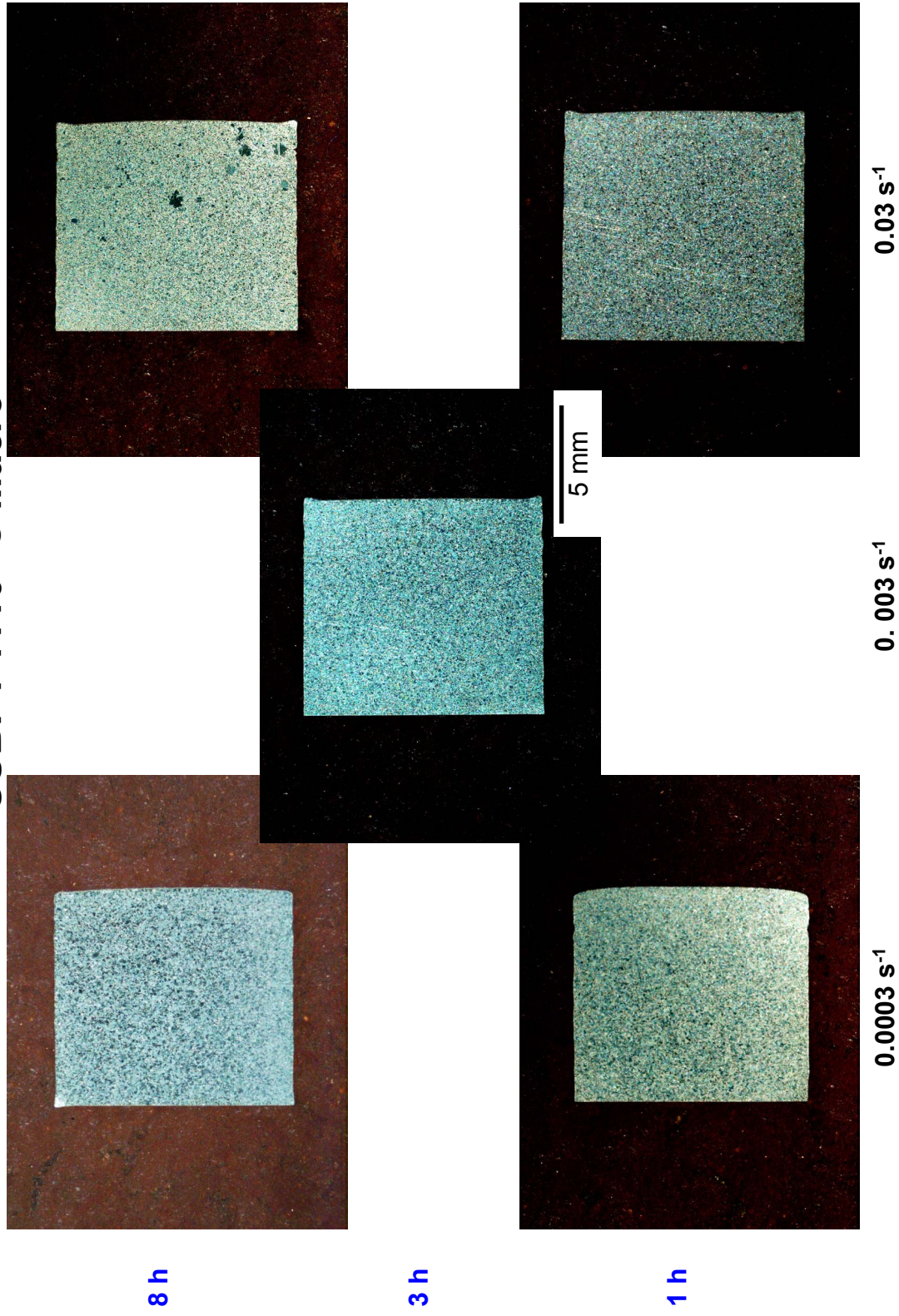


Figure 57.—Typical macrostructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 1h supersolvus solution heat treated.



# **SUBP4 1110 °C Macro**

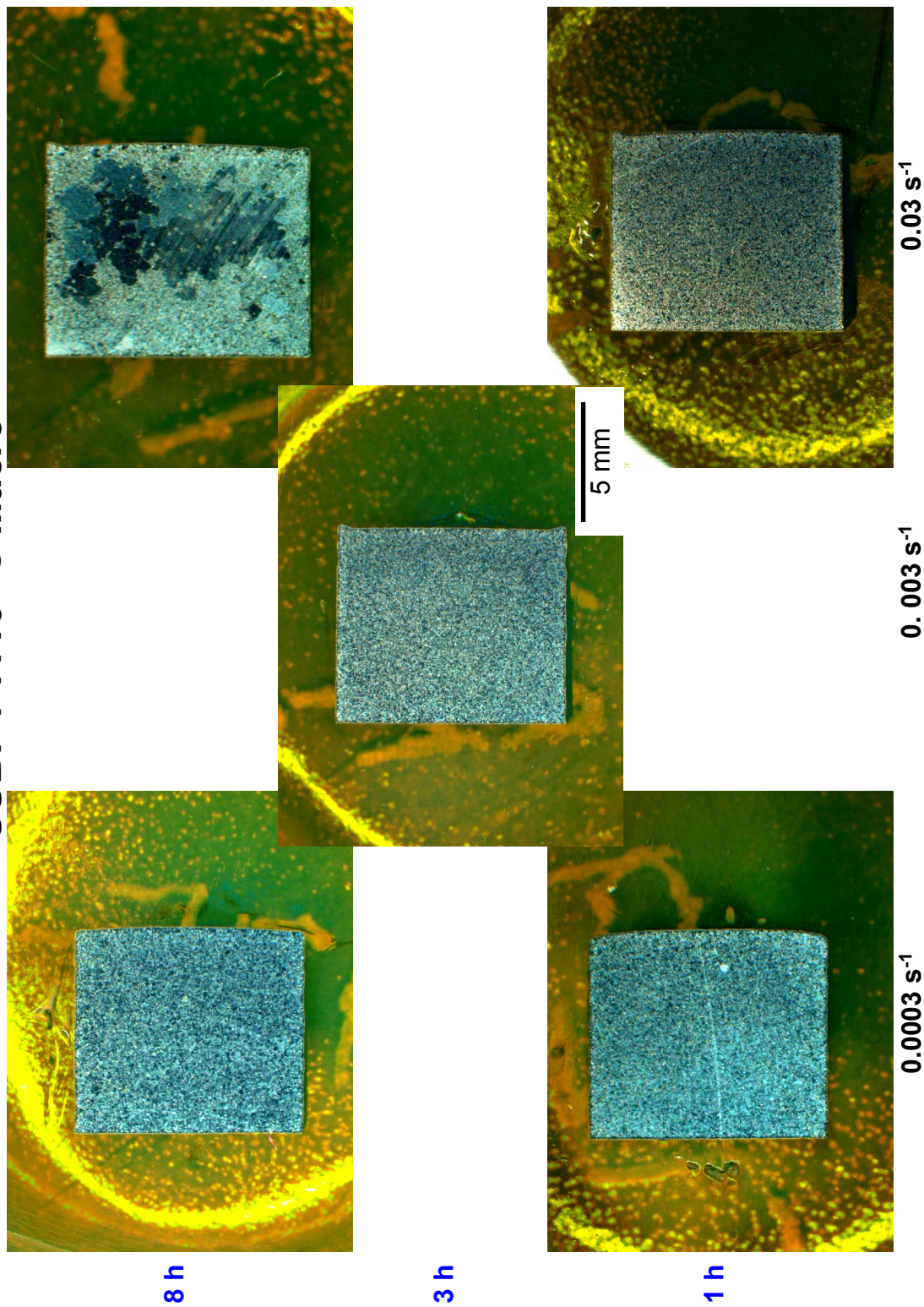


Figure 58.—Typical macrostructures of specimens forged at 1110 °C with the indicated presoak times and strain rates, then 1h subsolvus plus 4h supersolvus solution heat treated.

# SUBP DC Specimens 1080 °C Macro

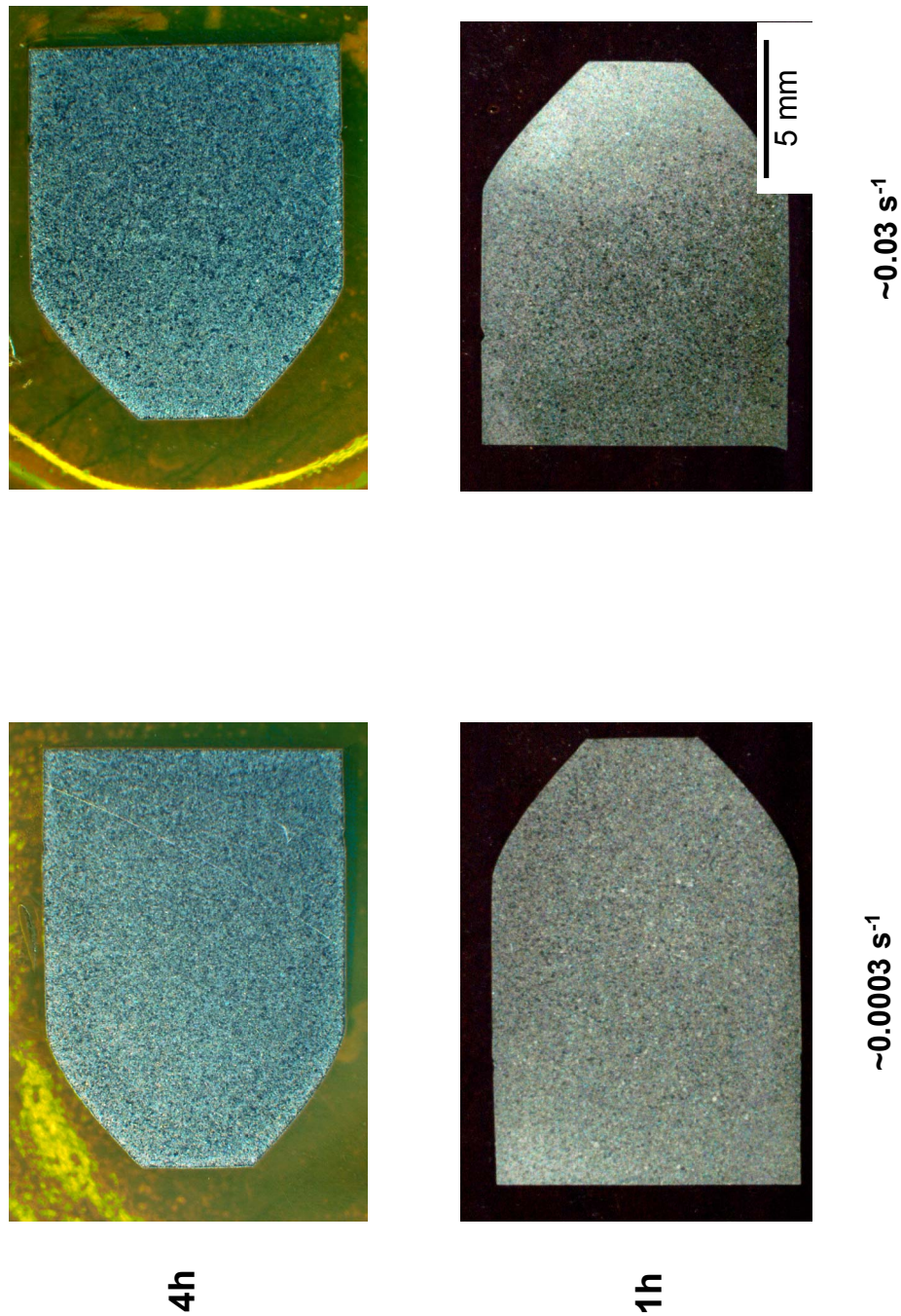


Figure 59.—Typical macrostructures of double cone specimens forged at 1080 °C with the indicated approximate average strain rates, then 1h subsolvus plus 1h and 4h supersolvus solution heat treated.



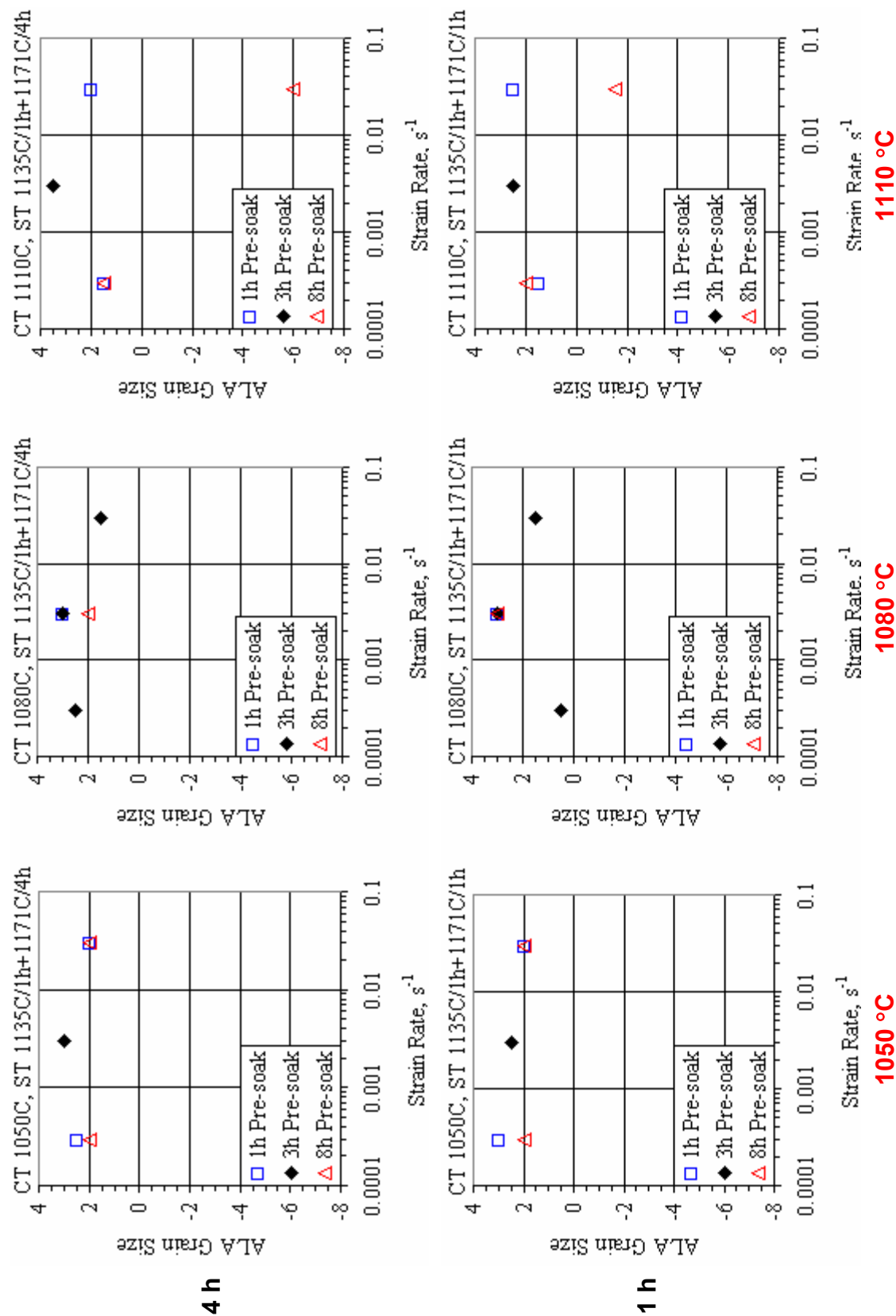


Figure 60.—As-large as grain size vs. strain rate for the indicated forging pre-soak times and temperatures, with subsequent 1h subsolvus plus 1h and 4h supersolvus solution heat treatments.

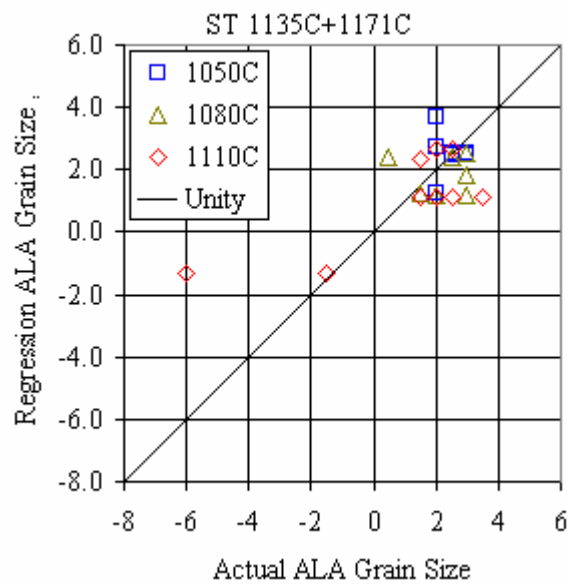


Figure 61.—Comparison of actual vs. regression subsolvus plus supersolvus heat treated as-large-as grain sizes.



## **Appendix A**





**TMPSTRESS (TMPSTRESS) - Experimental Design**

File Edit Define Design Enter Analyze Help

	TEMPERATURE (C) (1050 , 1110)	LOGSTRAINRATE (-3.5229 , -1.5229)	LOGPRESOAK (0 , 0.9031)	LOGSOLNTIME (0 , 0.6021)	LogFlowStress (0 , 100)	AsForgedGS (0 , 100)	SubGS (0 , 100)	SubALA (0 , 100)	SupGS (0 , 100)	SupALA (0 , 100)	SubSupGS (0 , 100)	SubSupALA (0 , 100)
1	1050	-3.5229	0.0000	0	1.1475	12.2	11.5	7.5	6.3	3	6.3	3
2	1050	-3.5229	0.9031	0	1.2732	12.1	11.3	7.5	6.1	3	6.2	2
3	1050	-2.5229	0.4771	0	1.7336	12.6	11.3	8	6.7	1.5	6.5	2.5
4	1050	-1.5229	0.0000	0	2.0852	13.1	11.9	7.5	6.1	3	5.8	2
5	1050	-1.5229	0.9031	0	2.1255	12.5	11.6	8	6.1	2	5.8	2
6	1050	-3.5229	0.4771	0	1.1182	11.7	11.2	9.5	5.9	3	5.8	0.5
7	1080	-2.5229	0.0000	0	1.5643	11.8	11.7	8.5	6.6	4	6.3	3
8	1080	-2.5229	0.4771	0	1.6577	12.3	11.3	8	6.3	3	6.6	3
9	1080	-2.5229	0.9031	0	1.7165	12.9	11.1	7	6.3	2	6.5	3
10	1080	-1.5229	0.4771	0	1.9899	11.7	11.4	7.5	6.4	3	5.5	1.5
11	1110	-3.5229	0.9031	0	1.1682	11.5	11.0	9	5.5	1.5	5.4	2
12	1110	-3.5229	0.0000	0	0.9742	11.5	11.5	8	5.9	2.5	5.5	1.5
13	1110	-2.5229	0.4771	0	1.5985	12.1	11.8	6.5	5.7	3	6.2	2.5
14	1110	-1.5229	0.0000	0	1.8732	11.8	11.2	6	6.5	0	6.7	2.5
15	1110	-1.5229	0.9031	0	1.9175	11.7	10.6	5.5	6.4	-6.5	6.5	-1.5
16	1050	-3.5229	0.0000	0.602059991			10.3	7.5	6.1	2	5.7	2.5
17	1050	-3.5229	0.9031	0.602059991			10.4	9.5	6.1	3	5.5	2
18	1050	-2.5229	0.4771	0.602059991			9.9	7.5	6.4	0.5	6.3	3
19	1050	-1.5229	0.0000	0.602059991			10.3	6.5	6.0	2	5.5	2
20	1050	-1.5229	0.9031	0.602059991			10.5	7	5.7	2.5	5.2	2
21	1080	-3.5229	0.4771	0.602059991			10.7	8	4.9	3	6.0	2.5
22	1080	-2.5229	0.0000	0.602059991			10.7	8.5	6.2	2.5	5.7	3
23	1080	-2.5229	0.4771	0.602059991			10.4	8.5	6.2	3.5	6.2	3
24	1080	-2.5229	0.9031	0.602059991			10.0	8	6.1	2	6.5	2
25	1080	-1.5229	0.4771	0.602059991			9.9	8.5	6.3	3	5.9	1.5
26	1110	-3.5229	0.9031	0.602059991			10.4	7.5	5.0	2	5.0	1.5
27	1110	-3.5229	0.0000	0.602059991			10.8	7.5	5.2	2	5.0	1.5
28	1110	-2.5229	0.4771	0.602059991			10.0	6.5	5.7	2.5	5.9	3.5
29	1110	-1.5229	0.0000	0.602059991			9.8	7.5	6.0	-1.5	5.9	2
30	1110	-1.5229	0.9031	0.602059991			9.5	7	4.2	-6.5	5.5	-6

Define  
Design  
Enter Data  
Analyze

Factors: Responses: 8 Terms: 11 Ready

A-1.—Input data table used for flow stress regression.

Least Squares Coefficients, Response LFS, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	1.595152	0.015225			
2 ~T	-0.083445	0.018643			((T-1.08e+03)/3e+01)
3 ~LSR	0.431332	0.018643			(LSR+2.5229)
4 ~LP	0.056251	0.018632			((LP-4.5155e-01)/4.5155e
5 ~T*LSR	-0.017712	0.020842	-0.85	0.4201	((T-1.08e+03)/3e+01)*(LS
6 ~T*LP	0.009255	0.020836	0.44	0.6687	((T-1.08e+03)/3e+01)*(L
7 ~LSR*LP	-0.029300	0.020836	-1.41	0.1973	(LSR+2.5229)*((LP-4.5155
No. cases = 15 R-sq. = 0.9861 RMS Error = 0.05895					
Resid. df = 8 R-sq-adj. = 0.9756 Cond. No. = 1.023					
~ indicates factors are transformed.					

## All Terms

## FORWARD AND REVERSE STEPWISE SELECTION

MuIreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response LFS MuIreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response LFS

Term	df	P-Remove	P-Enter	Term	df	P-Remove	P-Enter
1 1	1	0.000		1 1	1	0.000	
2 T	1	0.002		2 T	1	0.001	
3 LSR	1	0.000		3 LSR	1	0.000	
4 LP	1	0.017		4 LP	1	0.011	
5 T*LSR	1	0.420		5 T*LSR	1	0.419	
6 T*LP	1	0.669		6 T*LP	1	0.677	
7 LSR*LP	1	0.197		7 LSR*LP	1	0.167	
No. cases = 15		R-sq. = 0.9861		No. cases = 15		R-sq. = 0.9810	
Resid. df = 8		R-sq-adj. = 0.9756		Resid. df = 11		R-sq-adj. = 0.9759	
Obey Hierarchy: no				Obey Hierarchy: no			
RMS Error = 0.05895				RMS Error = 0.05867			

A-1.—Log flow stress regression results.

## MODEL TMLPLSTRESS

Least Squares Coefficients, Response LFS, Model TMLPLSTRESS					
Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	1.595152	0.015154	105.27	0.0001	
2 ~T	-0.083340	0.018554	-4.49	0.0009	((T-1.08e+03)/3e+01)
3 ~LSR	0.431000	0.018554	23.23	0.0001	(LSR+2.5229)
4 ~LP	0.056251	0.018545	3.03	0.0114	((LP-4.5155e-01)/4.5155e
No. cases = 15      R-sq. = 0.9810      RMS Error = 0.05867					
Resid. df = 11      R-sq-adj. = 0.9759      Cond. No. = 1.023					
~ indicates factors are transformed.					

## ANOVA

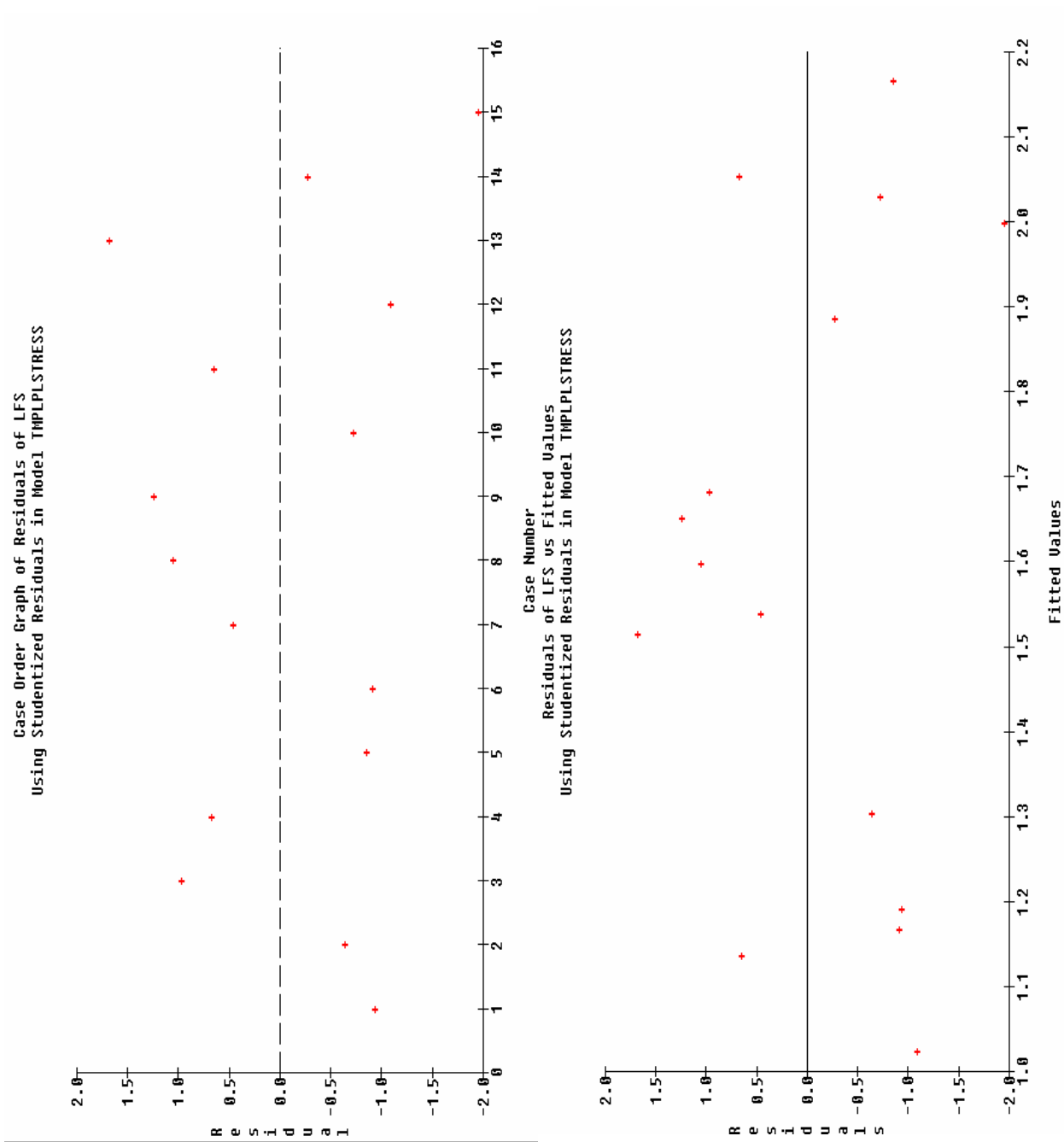
Least Squares Summary ANOVA, Response LFS Model TMLPLSTRESS

Least Squares Components ANOVA, Response LFS Model TMLPLSTRESS

Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Transformed Term
1 Total(Corr.)	14	1.996611				1 Constant	1	38.147333				
2 Regression	3	1.958741	0.652914	189.70	0.0000	2 ~T	1	0.069456	0.069456	20.17	0.0009	((T-1.08e+03)/3e+01)
3 Residual	11	0.037869	0.003443			3 ~LSR	1	1.857610	1.857610	539.60	0.0000	(LSR+2.5229)
						4 ~LP	1	0.031676	0.031676	9.20	0.0114	((LP-4.5155e-01)/4.5155e
						5 Residual	11	0.037869	0.003443			
						~ indicates factors are transformed. R-sq. = 0.9810						
						R-sq-adj. = 0.9759						
						Type 3 sum of squares.						

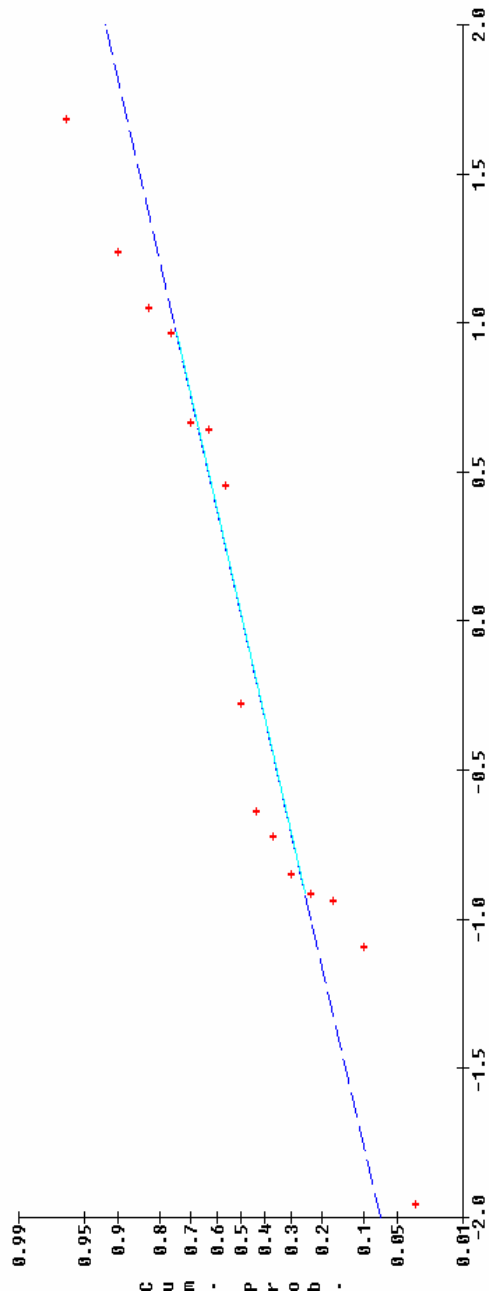
A-1.—Log flow stress regression results.



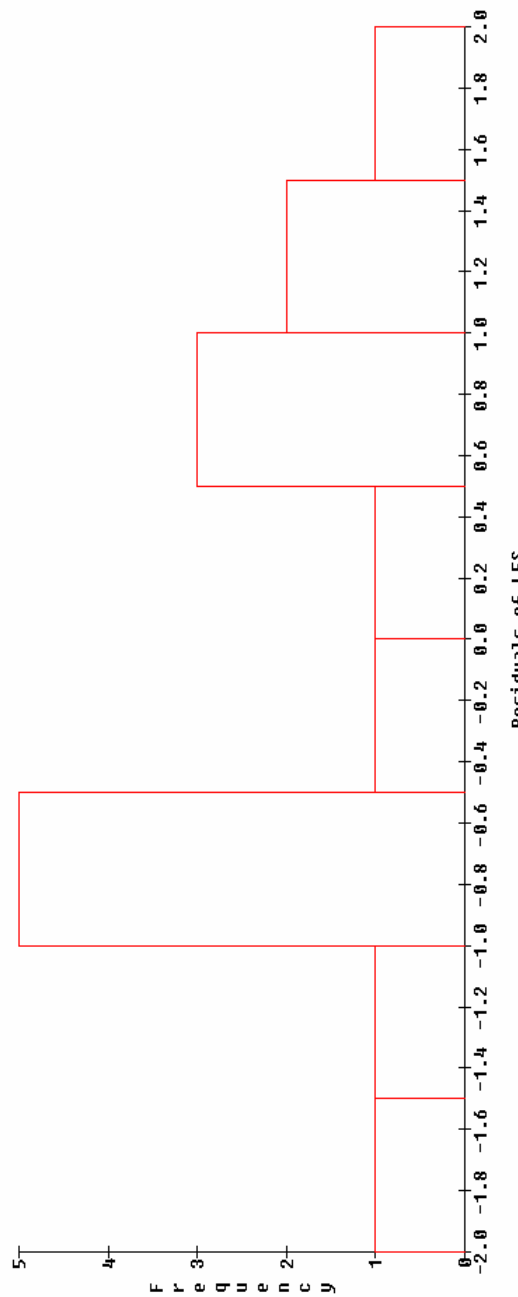


A-1.—Log flow stress regression results.

Normal Probability Plot of Residuals of LFS  
Using Studentized Residuals in Model TMPLPLSTRESS  
(Sample size = 15)

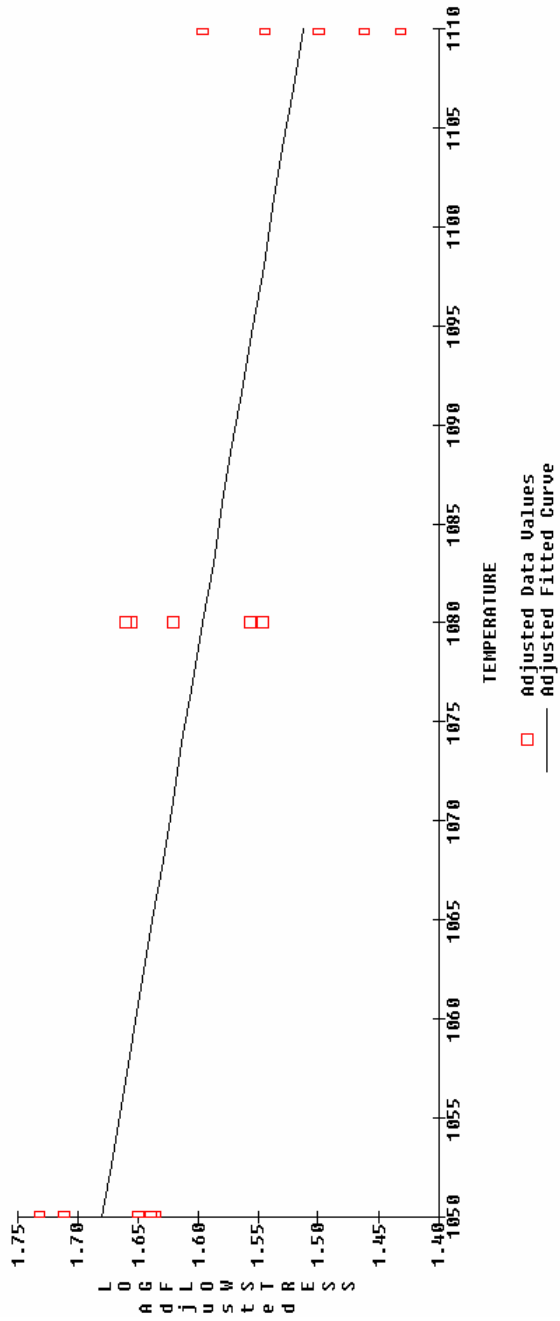


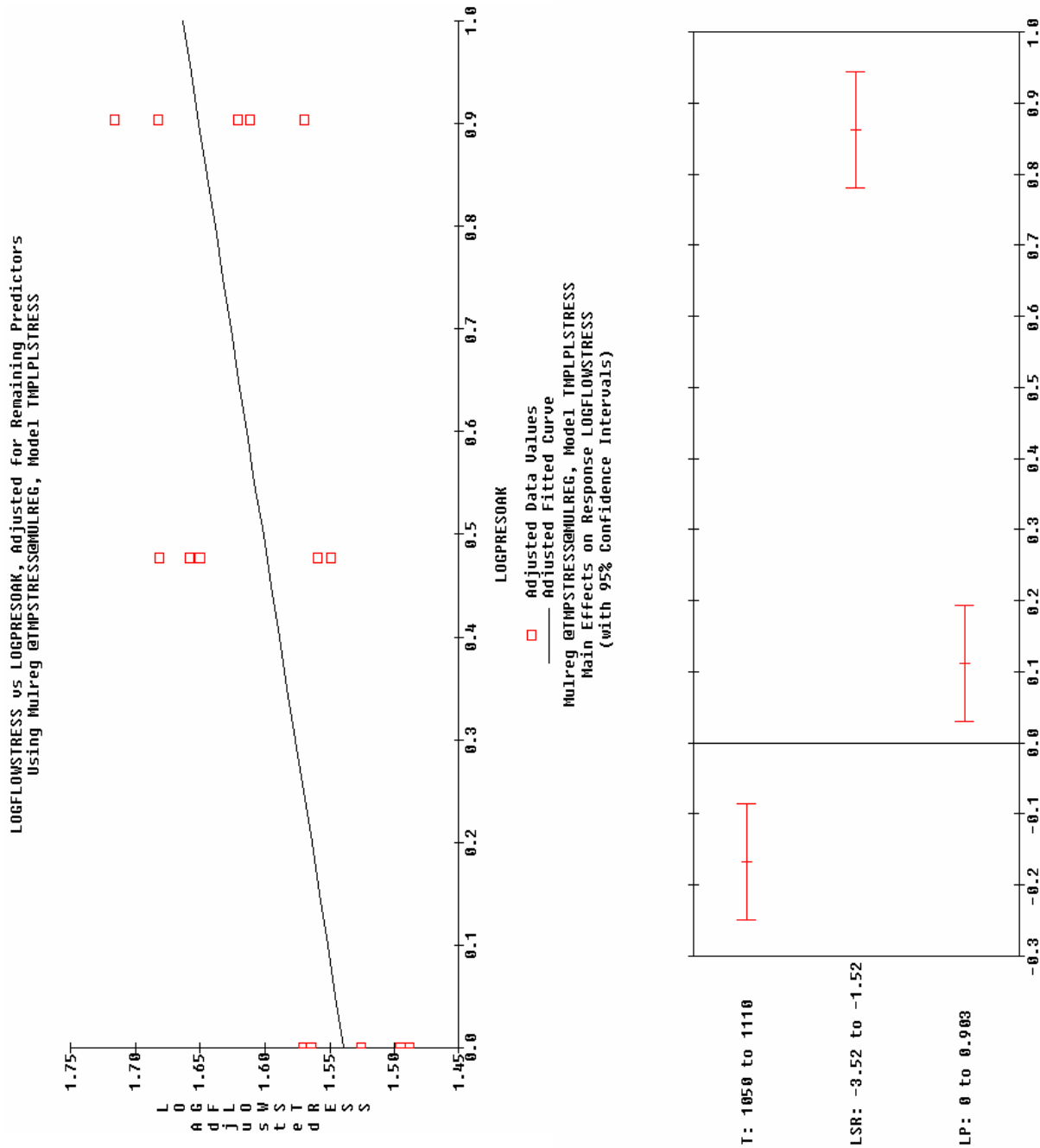
Histogram of Residuals of LFS  
Using Studentized Residuals in Model TMPLPLSTRESS  
(Sample size = 15)



A-1.—Log flow stress regression results.

LOGFLOWSTRESS vs TEMPERATURE, Adjusted for Remaining Predictors  
Using Muireg @TMPSTRESS@MULREG, Model TMPLPLSTRESS





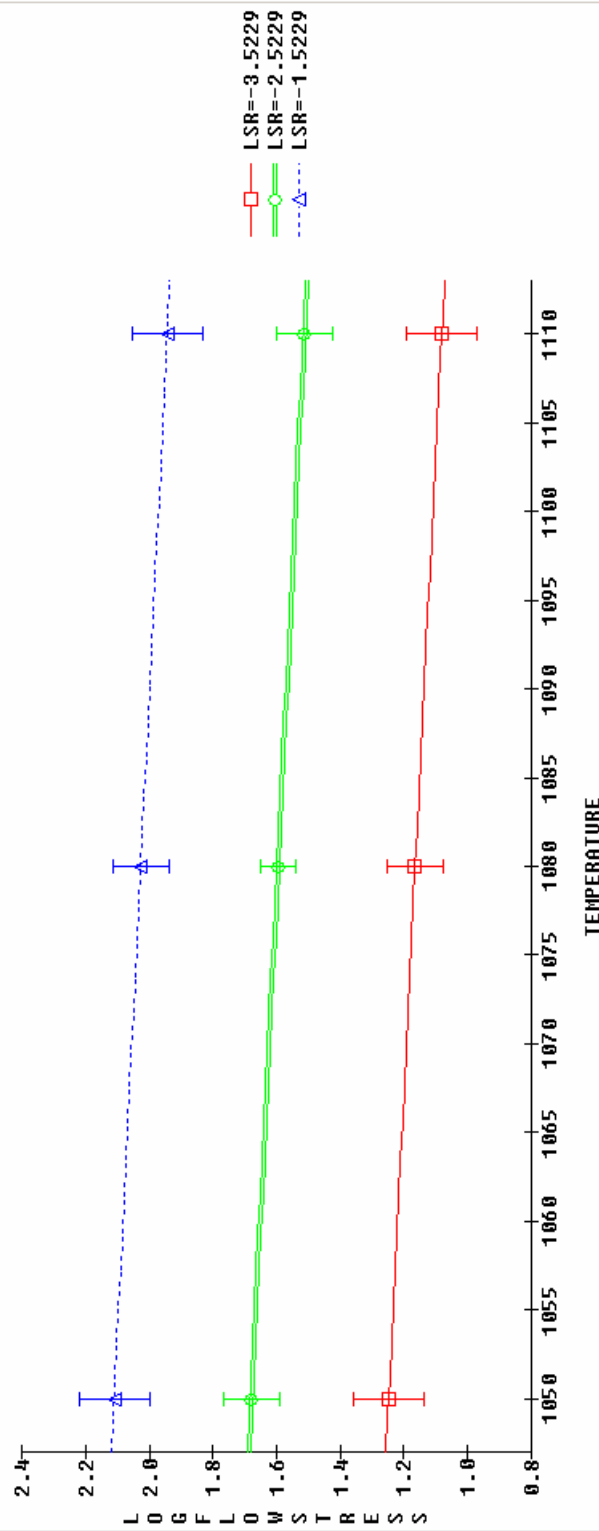
A-1.—Log flow stress regression results.



Predictions and 95% simultaneous confidence intervals  
for mean responses of LOGFLOWSTRESS using model TMLPSTRESS  
LP = 0.45771

LSR		T=1050	T=1080	T=1110
	</			

Predictions and 95% simultaneous confidence intervals  
for mean responses of LOGFLOWSTRESS using model TMLPSTRESS  
LP = 0.45771



A-1.—Log flow stress regression results.

## Least Squares Coefficients, Response AFG, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	12.099445	0.109987	110.01	0.0001	
2 ~T	-0.390871	0.134681	-2.90	0.0198	((T-1.08e+03)/3e+01)
3 ~LSR	0.180877	0.134681	1.34	0.2161	(LSR+2.5229)
4 ~LP	0.029403	0.134599	0.22	0.8325	(LP-4.5155e-01)/4.5155e
5 ~T*LSR	-0.100000	0.150566	-0.66	0.5253	((T-1.08e+03)/3e+01)*(LS
6 ~T*LP	0.076931	0.150518	0.51	0.6231	((T-1.08e+03)/3e+01)*(L
7 ~LSR*LP	-0.077497	0.150518	-0.51	0.6206	(LSR+2.5229)*(LP-4.5155

No. cases = 15      R-sq. = 0.5831      RMS Error = 0.4259  
 Resid. df = 8      R-sq-adj. = 0.2704      Cond. No. = 1.023  
 ~ indicates factors are transformed.

All  
Terms

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMP@HULREG, Model DESIGN\_COPY, Response AFG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.020	
3 LSR	1	0.216	
4 LP	1	0.833	
5 T*LSR	1	0.525	
6 T*LP	1	0.623	
7 LSR*LP	1	0.621	

No. cases = 15      R-sq. = 0.5831      RMS Error = 0.4259  
 Resid. df = 8      R-sq-adj. = 0.2704      Obey Hierarchy: no

Mulreg @TMP@HULREG, Model DESIGN\_COPY, Response AFG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.007	
3 LSR	1		0.149
4 LP	1		0.821
5 T*LSR	1		0.488
6 T*LP	1		0.595
7 LSR*LP	1		0.605

No. cases = 15      R-sq. = 0.4371      RMS Error = 0.3882  
 Resid. df = 13      R-sq-adj. = 0.3938      Obey Hierarchy: no

A-2.—As-Forged grain size regression results.

MODEL TMPAFG

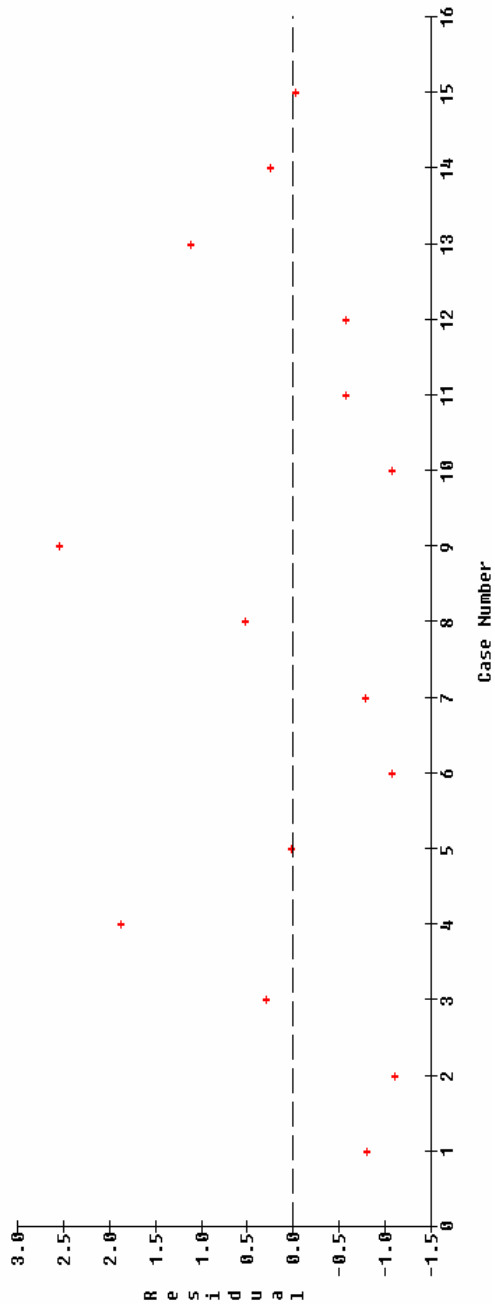
Least Squares Coefficients, Response AFG, Model TMPAFG				
Term	Coeff.	Std. Error	T-value	Signif. Transformed Term
1 1	12.100000	0.100231	120.72	0.0001
2 ~T	-0.390000	0.122757	-3.18	0.0073 ((T-1.08e+03)/3e+01)
No. cases = 15 R-sq. = 0.4371 RMS Error = 0.3882				
Resid. df = 13 R-sq-adj. = 0.3938 Cond. No. = 1				
~ indicates factors are transformed.				

ANOVA

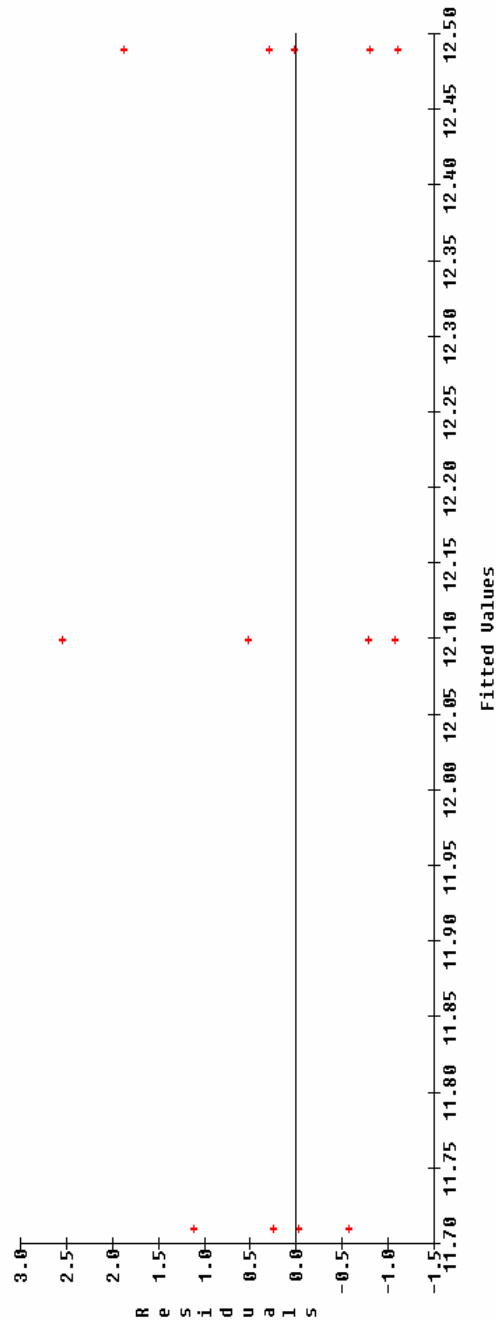
Least Squares Summary ANOVA, Response AFG Model TMPAFG				
Source	df	Sum Sq.	Mean Sq.	F-Ratio Signif.
1 Total(Corr.)	14	3.480000		
2 Regression	1	1.521000	1.521000	10.09 0.0073
3 Residual	13	1.959000	0.150692	
R-sq. = 0.4371				
R-sq-adj. = 0.3938				
Least Squares Components ANOVA, Response AFG Model TMPAFG				
Source	df	Sum Sq.	Mean Sq.	F-Ratio Signif. Transformed Term
1 Constant	1	2196		
2 ~T	1	1.521000	1.521000	10.09 0.0073 ((T-1.08e+03)/3e+01)
3 Residual	13	1.959000	0.150692	
~ indicates factors are transformed. R-sq. = 0.4371				
are transformed. R-sq-adj. = 0.3938				
Type 3 sum of squares.				

A-2.—As-Forged grain size regression results.

Case Order Graph of Residuals of AFG  
Using Studentized Residuals in Model TMPAFG

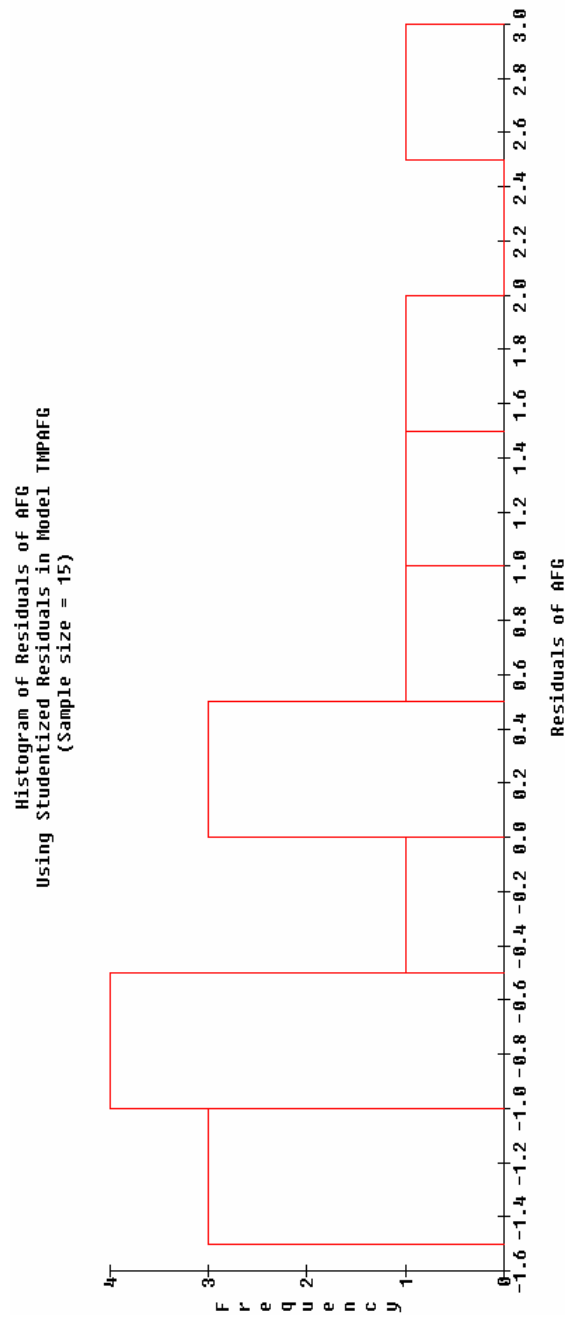
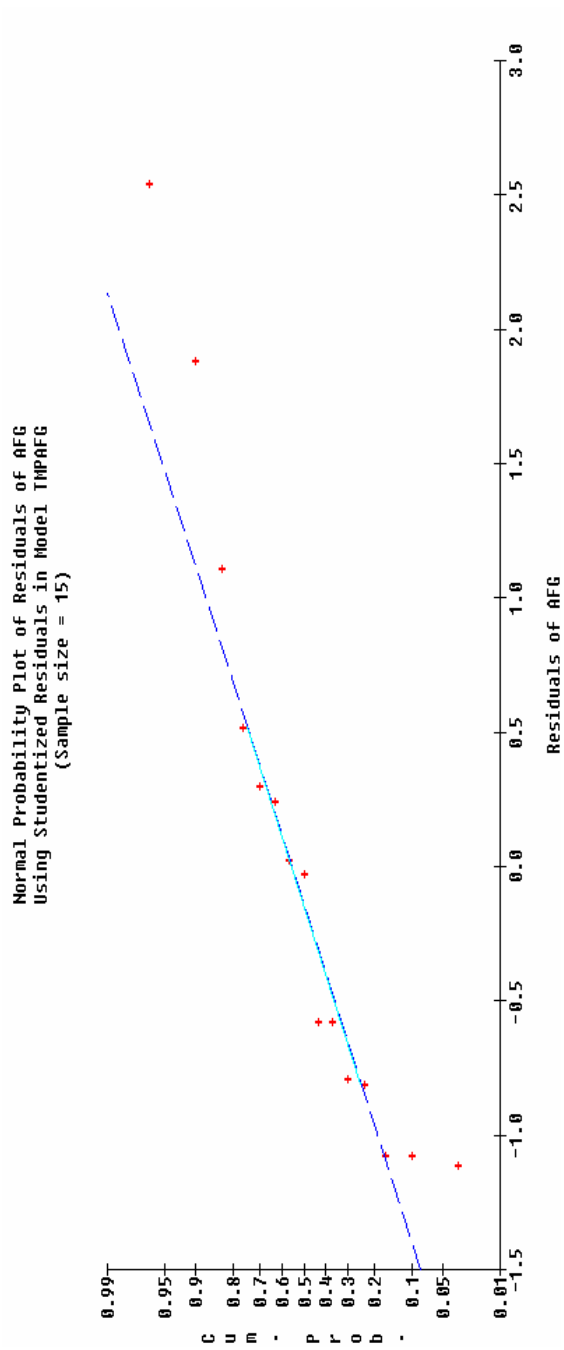


Residuals of AFG vs Fitted Values  
Using Studentized Residuals in Model TMPAFG



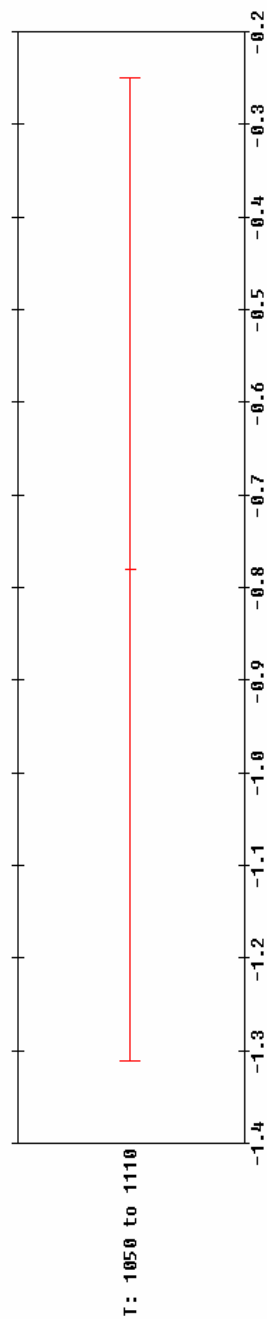
A-2.—As-Forged grain size regression results.



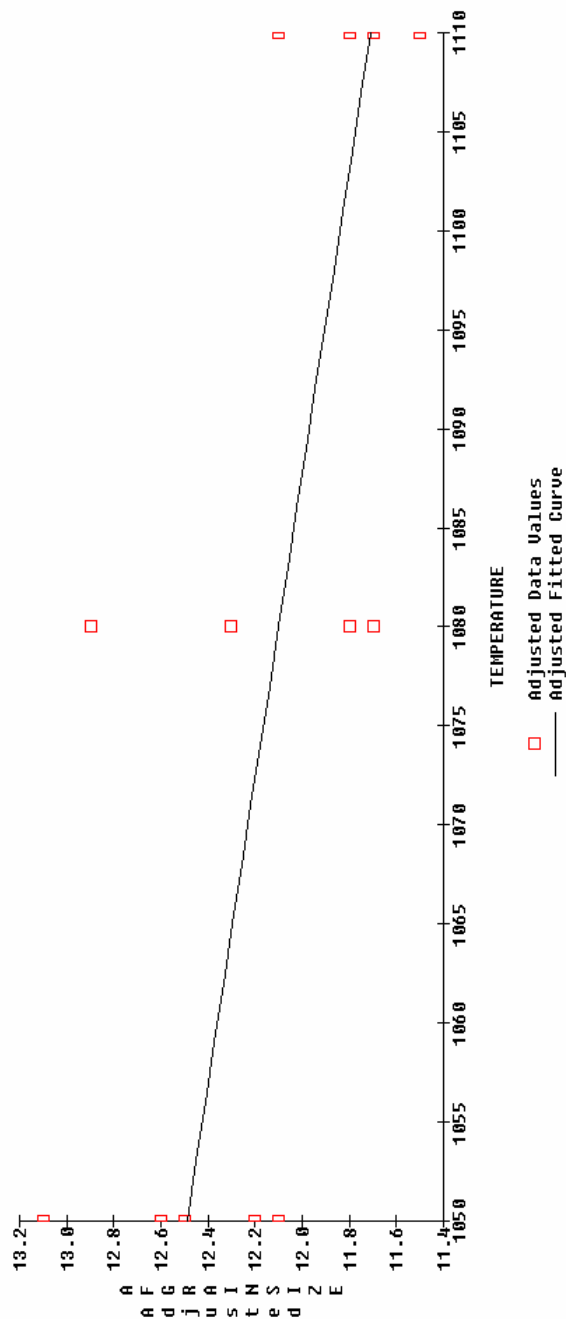


A-2.—As-Forged grain size regression results.

Multreg @TMPSTRESS@MULREG, Model TMPAFG  
Main Effects on Response, AFGRAINSIZE  
(with 95% Confidence Intervals)



AFGRAINSIZE vs TEMPERATURE, Adjusted for Remaining Predictors  
Using Multreg @TMPSTRESS@MULREG, Model TMPAFG

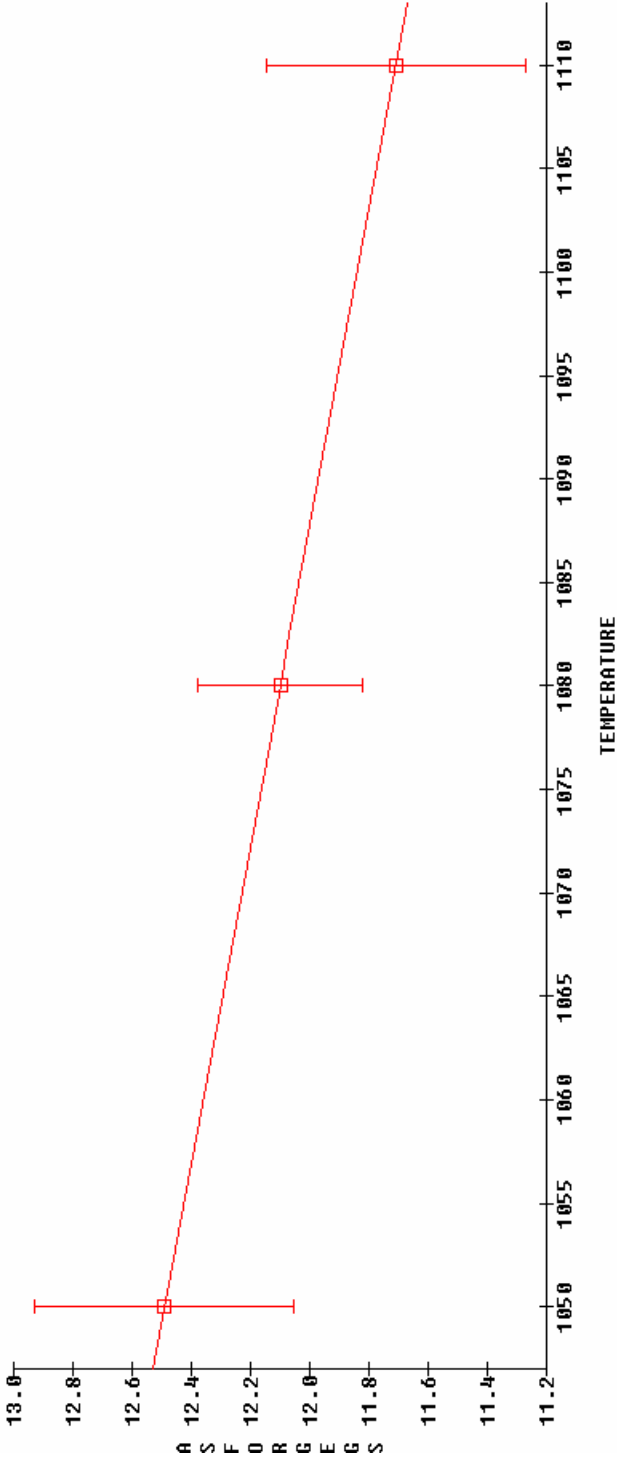


A-2.—As-Forged grain size regression results.

Predictions and 95% simultaneous confidence intervals  
for mean responses of ASFORGEES using model TMPAFG

T:	1050	1080	1110
Lower	12.052786	11.823481	11.272786
Predicted	12.490000	12.100000	11.710000
Upper	12.927214	12.376519	12.147214

Predictions and 95% simultaneous confidence intervals  
for mean responses of ASFORGEES using model TMPAFG



A-2.—As-Forged grain size regression results.

TMPSTRESS (TMPSGALA) - Experimental Design													
File Edit Define Design Enter Analyze Help													
TEMPERATURE (1050, 1110) [C]	LOGSTRAINRATE (-3.5229, -1.5229)	LOGPRESOAK (0, 0.9031)	LogSolnTime (0, 0.6021)	SubGS (0, 100)	SupGS (0, 100)	Sub+SupGS (0, 100)	SubALA (0, 100)	SupALA (0, 100)	Sub+SupALA (0, 100)				
1 1050	-3.5229	0.0000	0	11.5	6.3	6.3	7.5	3	3				
2 1050	-3.5229	0.9031	0	11.3	6.1	6.2	7.5	3	2				
3 1050	-2.5229	0.4771	0	11.3	6.7	6.5	8	1.5	2.5				
4 1050	-1.5229	0.0000	0	11.9	6.1	5.8	7.5	3	2				
5 1050	-1.5229	0.9031	0	11.6	6.1	5.8	8	2	2				
6 1080	-3.5229	0.4771	0	11.2	5.9	5.8	9.5	3	0.5				
7 1080	-2.5229	0.0000	0	11.7	6.6	6.3	8.5	4	3				
8 1080	-2.5229	0.4771	0	11.3	6.3	6.6	8	3	3				
9 1080	-2.5229	0.9031	0	11.1	6.3	6.5	7	2	3				
10 1080	-1.5229	0.4771	0	11.4	6.4	5.5	7.5	3	1.5				
11 1110	-3.5229	0.9031	0	11.0	5.5	5.4	9	1.5	2				
12 1110	-3.5229	0.0000	0	11.5	5.9	5.5	8	2.5	1.5				
13 1110	-2.5229	0.4771	0	11.8	5.7	6.2	6.5	3	2.5				
14 1110	-1.5229	0.0000	0	11.2	6.5	6.7	6	0	2.5				
15 1110	-1.5229	0.9031	0	10.6	6.4	6.5	5.5	-6.5	-1.5				
16 1050	-3.5229	0.0000	0.602059991	10.3	6.1	5.7	7.5	2	2.5				
17 1050	-3.5229	0.9031	0.602059991	10.4	6.1	5.5	9.5	3	2				
18 1050	-2.5229	0.4771	0.602059991	9.9	6.4	6.3	7.5	0.5	3				
19 1050	-1.5229	0.0000	0.602059991	10.3	6.0	5.5	6.5	2	2				
20 1050	-1.5229	0.9031	0.602059991	10.5	5.7	5.2	7	2.5	2				
21 1080	-3.5229	0.4771	0.602059991	10.7	4.9	6.0	8	3	2.5				
22 1080	-2.5229	0.0000	0.602059991	10.7	6.2	5.7	8.5	2.5	3				
23 1080	-2.5229	0.4771	0.602059991	10.4	6.2	6.2	8.5	3.5	3				
24 1080	-2.5229	0.9031	0.602059991	10.0	6.1	6.5	8	2	2				
25 1080	-1.5229	0.4771	0.602059991	9.9	6.3	5.9	8.5	3	1.5				
26 1110	-3.5229	0.9031	0.602059991	10.4	5.0	5.0	7.5	2	1.5				
27 1110	-3.5229	0.0000	0.602059991	10.8	5.2	5.0	7.5	2	1.5				
28 1110	-2.5229	0.4771	0.602059991	10.0	5.7	5.9	6.5	2.5	3.5				
29 1110	-1.5229	0.0000	0.602059991	9.8	6.0	5.9	7.5	-1.5	2				
30 1110	-1.5229	0.9031	0.602059991	9.5	4.2	5.5	7	-6.5	-6				
31													

A-3.—Subsolvus mean grain size regression results.



## All Terms

Least Squares Coefficients, Response SBG, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	10.003077	0.042981			
2 ~T	-0.118910	0.052631			((T-1.08e+03)/3e+01)
3 ~LSR	-0.120005	0.052631			(LSR+2.5229)
4 ~LP	-0.165103	0.052598			((LP-4.5155e-01)/4.5155e
5 ~LST	-0.561047	0.042984			((LST-3.0105e-01)/3.0105
6 ~T*LSR	-0.212500	0.058838	-3.61	0.0019	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.096119	0.058819	-1.63	0.1187	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	0.030002	0.052630	0.57	0.5753	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.000424	0.058819	-0.01	0.9943	(LSR+2.5229)*(LP-4.5155
10 ~LSR*LST	-0.140009	0.052630	-2.66	0.0155	(LSR+2.5229)*(LST-3.010
11 ~LP*LST	0.053532	0.052602	1.02	0.3216	((LP-4.5155e-01)/4.5155e

No. cases = 30    R-sq. = 0.9185    RMS Error = 0.2354  
 Resid. df = 19    R-sq-adj. = 0.8757    Cond. No. = 1.023  
 ~ indicates factors are transformed.

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response SBG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.036	
3 LSR	1	0.034	
4 LP	1	0.005	
5 LST	1	0.000	
6 T*LSR	1	0.002	
7 T*LP	1	0.119	
8 T*LST	1	0.575	
9 LSR*LP	1	0.994	
10 LSR*LST	1	0.015	
11 LP*LST	1	0.322	

No. cases = 30    R-sq. = 0.9185  
 Resid. df = 19    R-sq-adj. = 0.8757

RMS Error = 0.2354  
 Obey Hierarchy: no

Mulreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response SBG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.032	
3 LSR	1	0.032	
4 LP	1	0.005	
5 LST	1	0.000	
6 T*LSR	1	0.001	
7 T*LP	1		0.104
8 T*LST	1		0.580
9 LSR*LP	1		0.994
10 LSR*LST	1	0.014	
11 LP*LST	1		0.320

No. cases = 30    R-sq. = 0.9013    RMS Error = 0.2355  
 Resid. df = 23    R-sq-adj. = 0.8755    Obey Hierarchy: no

A-3.—Subsolvus mean grain size regression results.

## MODEL TMPSUBGS

Least Squares Coefficients, Response SBG, Model TMPSUBGS						
Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term	
1 1	10.803077	0.043010	251.18	0.0001		
2 ~T	-0.120000	0.052662	-2.28	0.0323	((T-1.08e+03)/3e+01)	
3 ~LSR	-0.120009	0.052662	-2.28	0.0323	(LSR+2.5229)	
4 ~LP	-0.165107	0.052634	-3.14	0.0046	((LP-4.5155e-01)/4.5155e-01)	
5 ~LST	-0.560037	0.043001	-13.02	0.0001	(LST-3.0105e-01)/3.0105e-01	
6 ~T*LSR	-0.212500	0.058878	-3.61	0.0015	((T-1.08e+03)/3e+01)*(LSR+2.5229)	
7 ~LSR*LST	-0.140009	0.052666	-2.66	0.0140		
No. cases = 30				R-sq. = 0.9013	RMS Error = 0.2355	
Resid. df = 23				R-sq-adj. = 0.8755	Cond. No. = 1.023	
~ indicates factors are transformed.						

## ANOVA

Least Squares Summary ANOVA, Response SBG Model TMPSUBGS

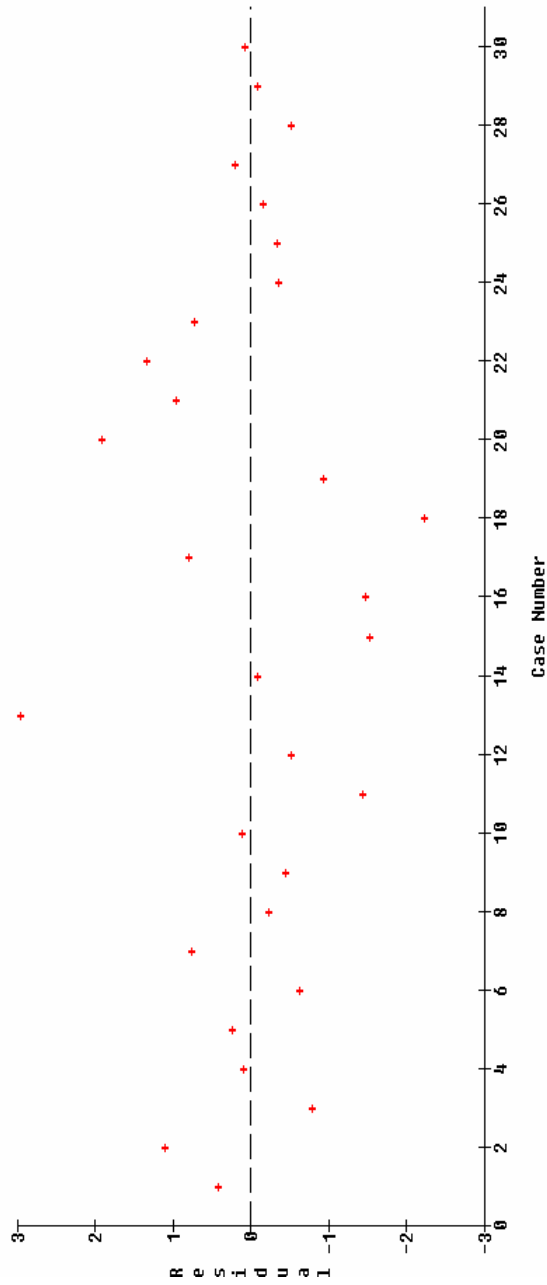
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.
1 Total(Corr.)	29	12.92000			
2 Regression	6	11.64429	1.94071	34.99	0.0000
3 Linear	4	10.52983	2.63246	47.46	0.0000
4 Non-Linear	2	1.11450	0.55725	10.05	0.0007
5 Residual	23	1.27571	0.05547		
R-sq. = 0.9013					
R-sq-adj. = 0.8755					

Least Squares Components ANOVA, Response SBG Model TMPSUBGS

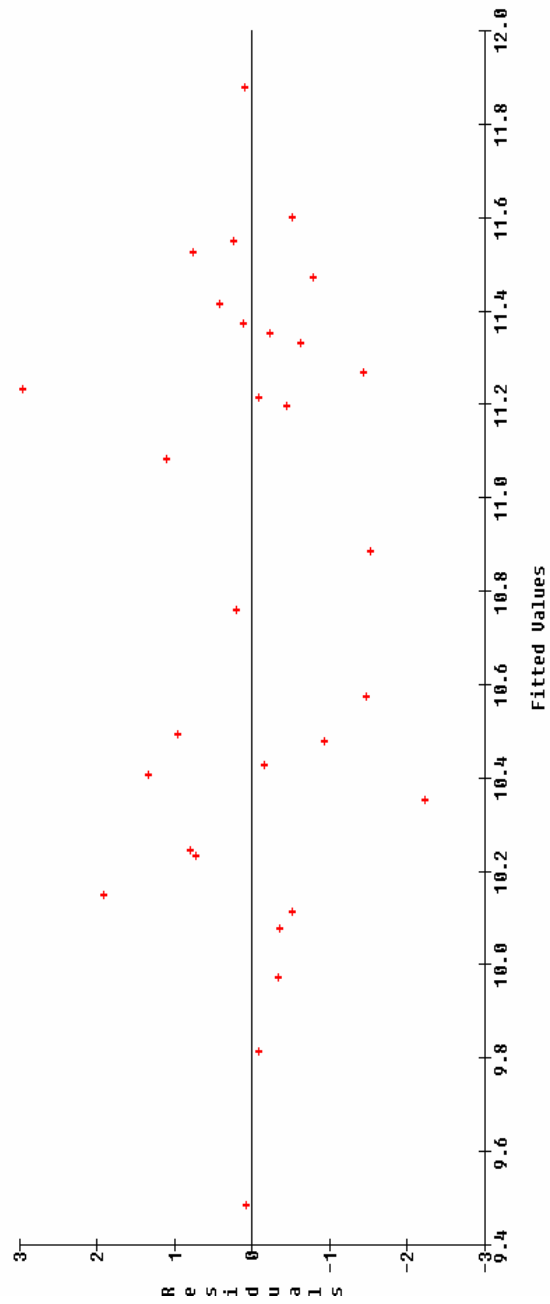
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Transformed Term
1 Constant	1	3499				
2 ~T	1	0.28800	0.28800	5.19	0.0323	$((T-1.08e+03)/3e+01)$
3 ~LSR	1	0.28804	0.28804	5.19	0.0323	$(LSR+2.5229)$
4 ~LP	1	0.54579	0.54579	9.84	0.0046	$((LP-4.5155e-01)/4.5155e-01)$
5 ~LST	1	9.40800	9.40800	169.60	0.0000	$(LST-3.0105e-01)/3.0105e-01$
6 ~T*LSR	1	0.72250	0.72250	13.03	0.0015	$((T-1.08e+03)/3e+01)*(LSR+2.5229)$
7 ~LSR*LST	1	0.39200	0.39200	7.07	0.0140	$(LSR+2.5229)*((LST-3.0105e-01)/3.0105e-01)$
8 Residual	23	1.27571	0.05547			
~ indicates factors are transformed. R-sq. = 0.9013						
Type 3 sum of squares. R-sq-adj. = 0.8755						

A-3.—Subsolvus mean grain size regression results.

Case Order Graph of Residuals of SBG  
Using Studentized Residuals in Model TMPSUBGS

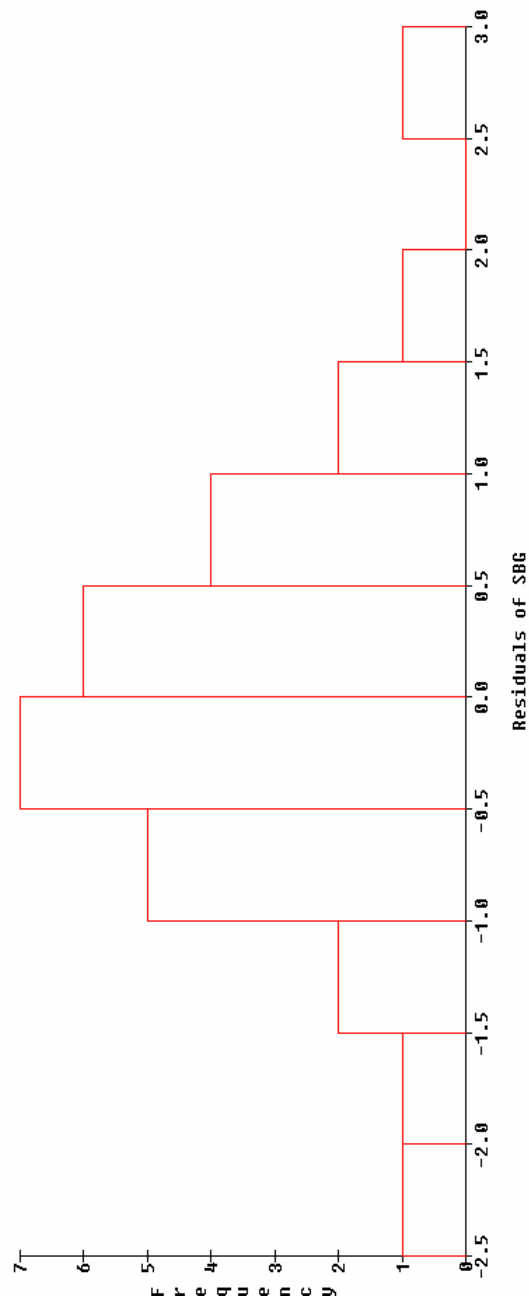
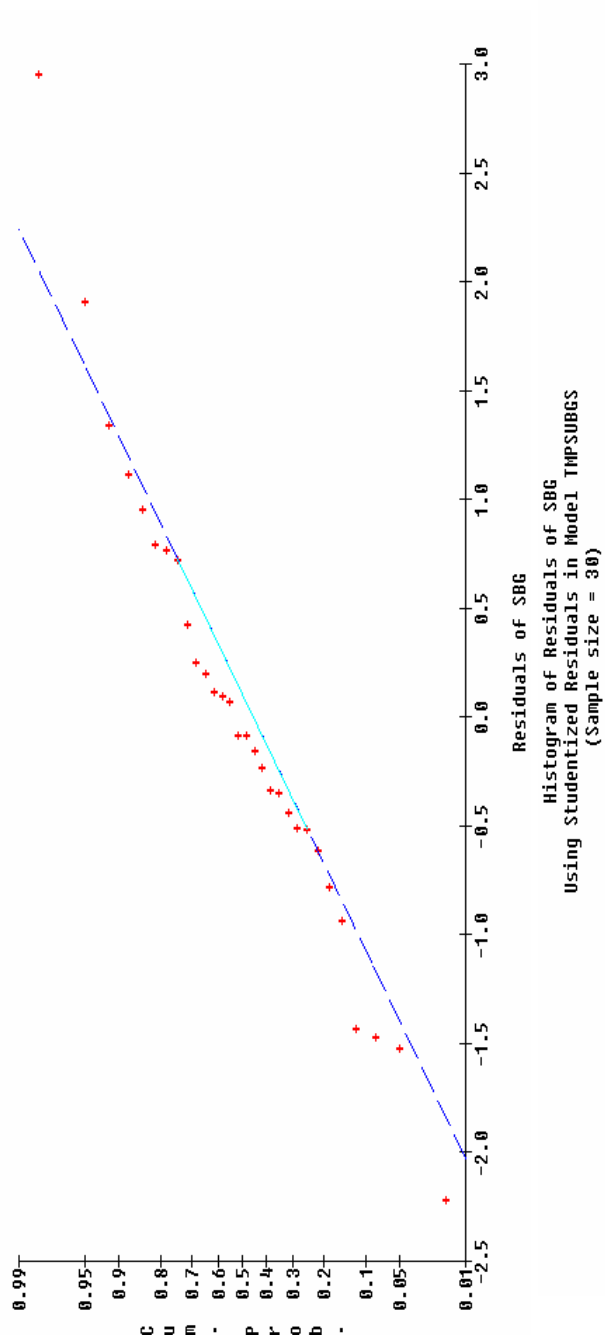


Residuals of SBG vs Fitted Values  
Using Studentized Residuals in Model TMPSUBGS



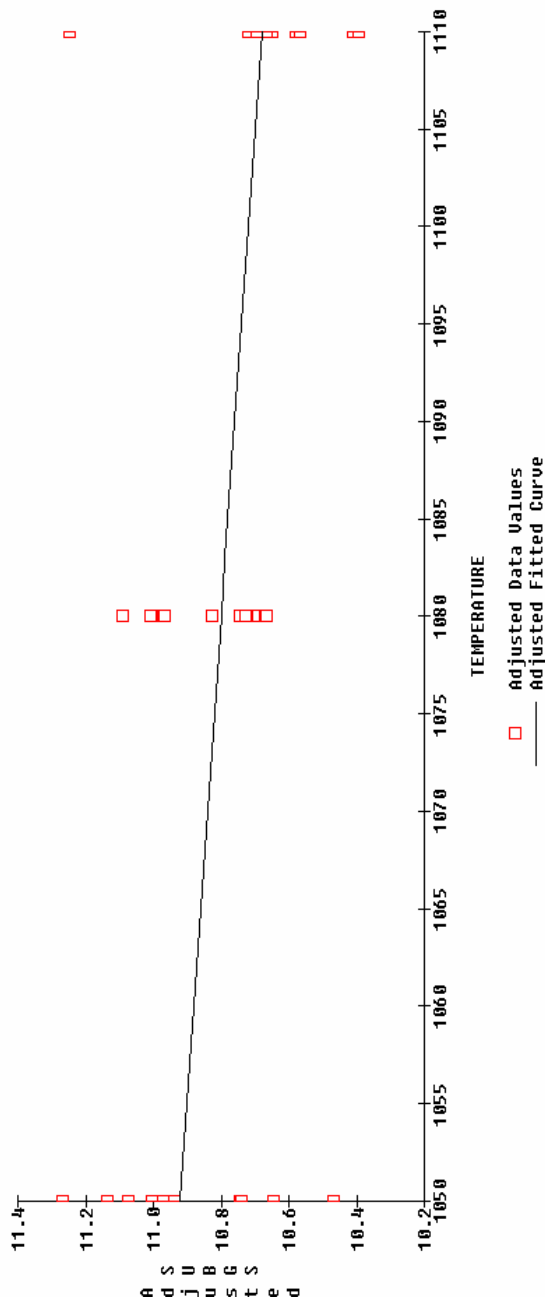
A-3.—Subsolvus mean grain size regression results.

Normal Probability Plot of Residuals of SBG  
Using Studentized Residuals in Model TmpSUBGS  
(Sample size = 30)

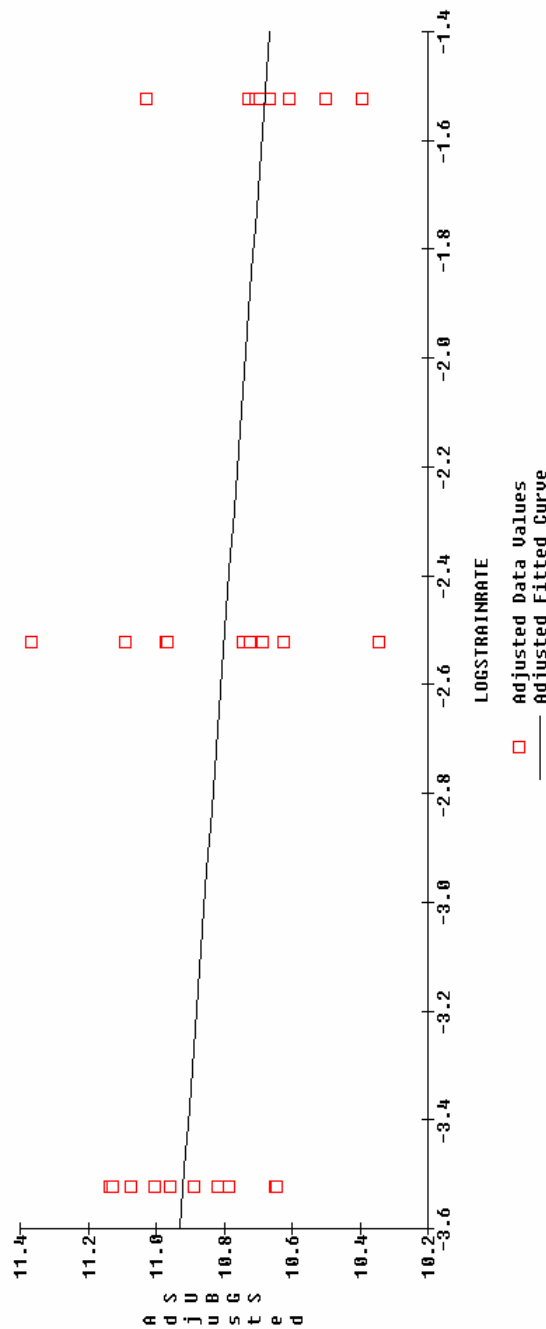


A-3.—Subsolvus mean grain size regression results.

SUBGS vs TEMPERATURE, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS



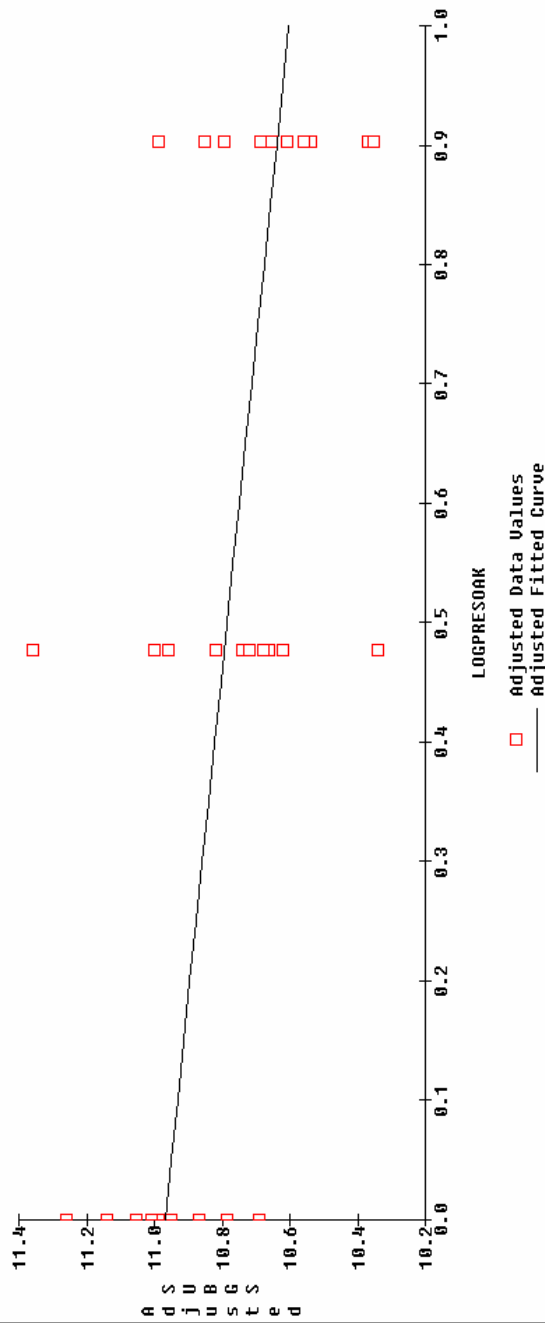
SUBGS vs LOGSTRAINRATE, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS



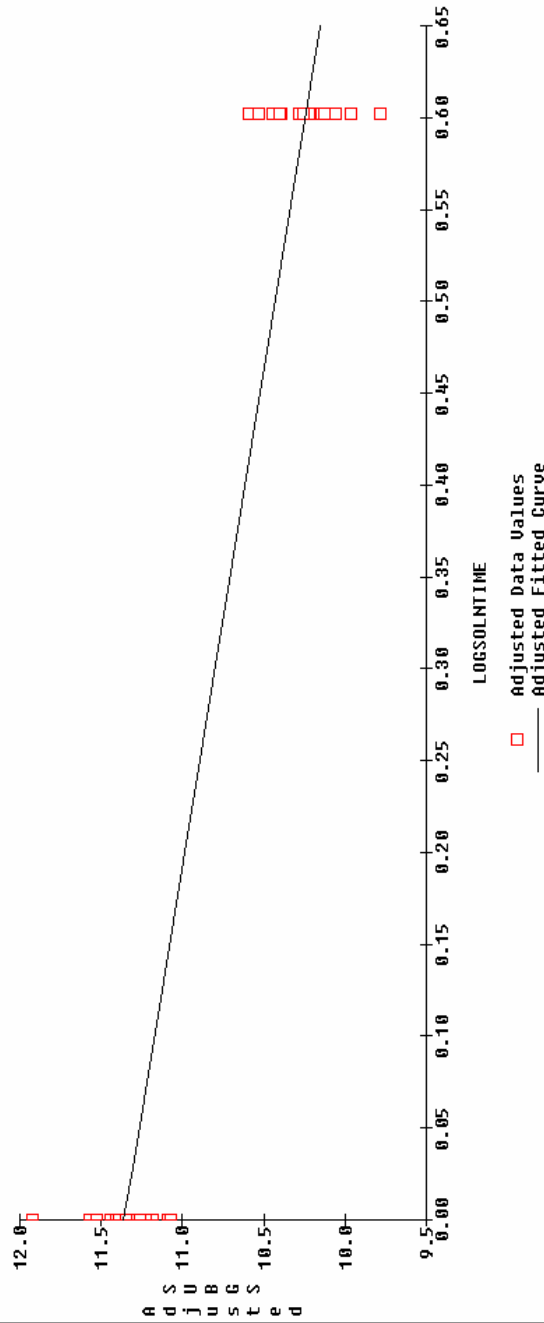
A-3.—Subsolvus mean grain size regression results.



SUBGS vs LOGPRESOAK, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS

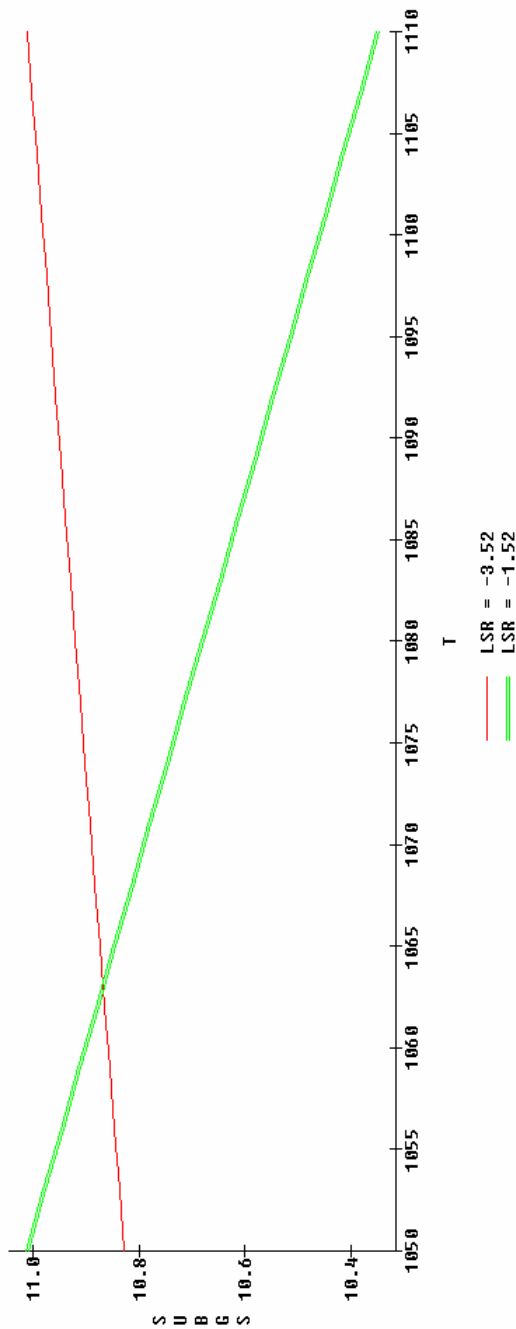


SUBGS vs LOGSOLNTIME, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS

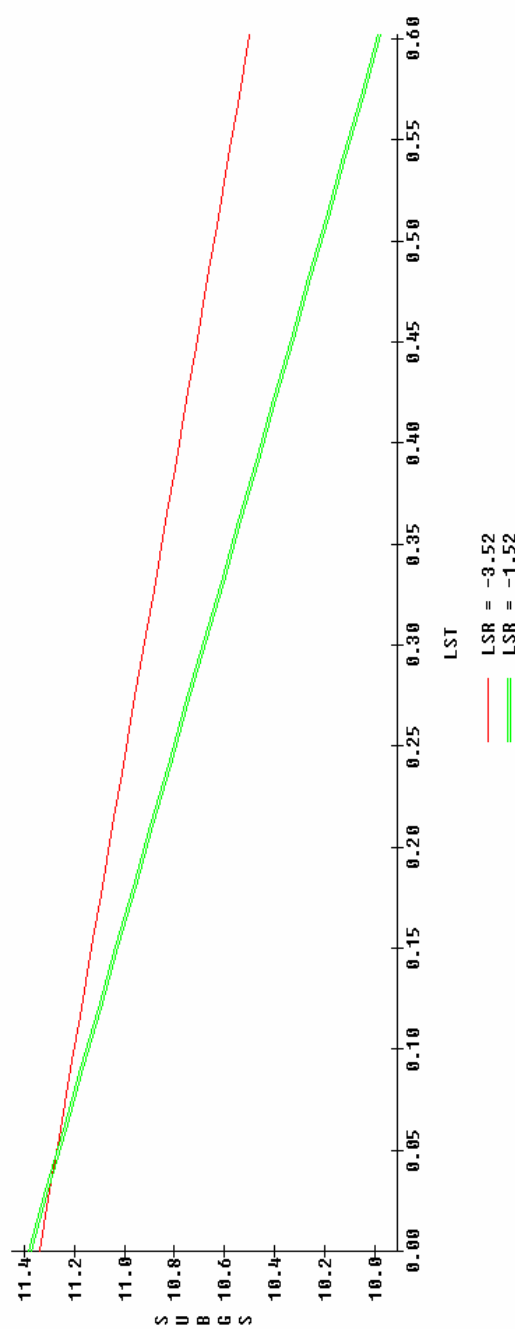


A-3.—Subsolvus mean grain size regression results.

Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS  
Interaction Effects of TEMPERATURE with LOGSTRAINRATE  
On Response SUBGS

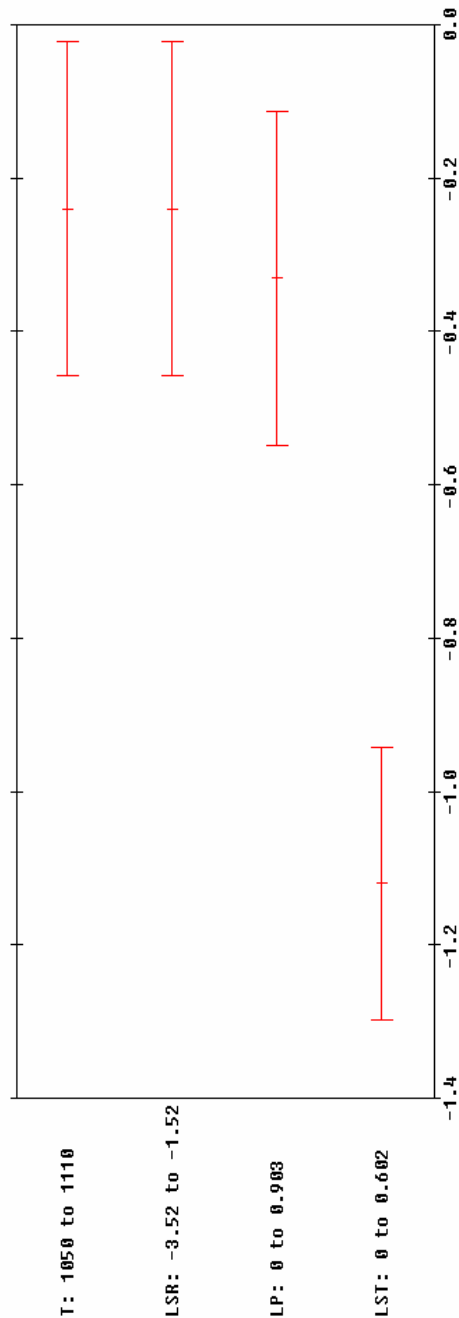


Mulreg @TMPSTRESS@MULREG, Model TMPSUBGS  
Interaction Effects of LOGSOLTIME with LOGSTRAINRATE  
On Response SUBGS



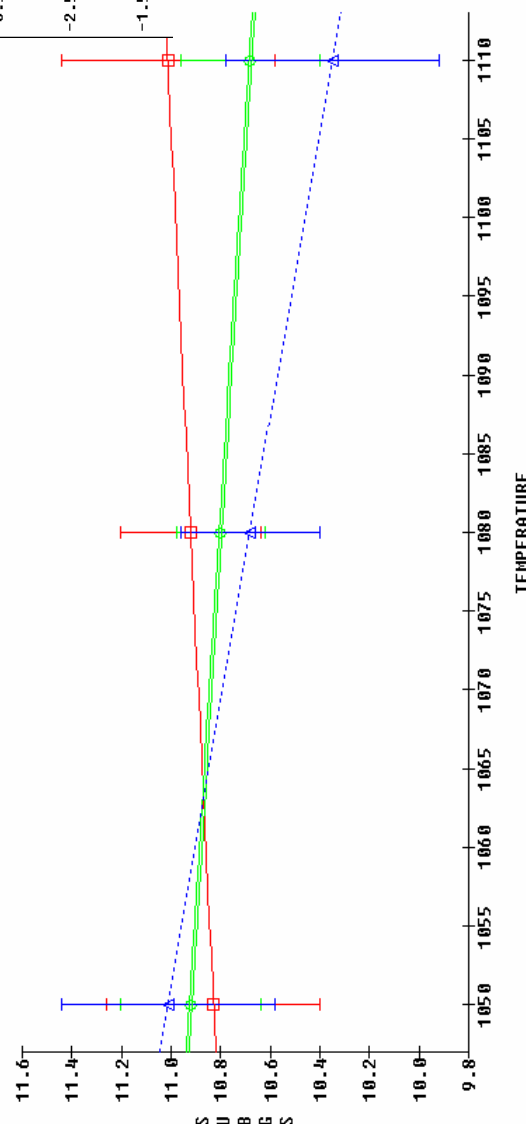
A-3.—Subsolvus mean grain size regression results.

Mulreg @IMPSTRESS@MULREG, Model TMPSUBGS  
Main Effects on Response SUBGS  
(with 95% Confidence Intervals)



Predictions and 95% simultaneous confidence intervals  
for mean responses of SUBGS using model TMPSUBGS  
LP = 0.45771, LST = 0.30103

Predictions and 95% simultaneous confidence intervals  
for mean responses of SUBGS using model TMPSUBGS  
LP = 0.45771, LST = 0.30103



A-3.—Subsolvus mean grain size regression results.

## All Terms

Least Squares Coefficients, Response SBA, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	7.648955	0.163854	46.68	0.0001	
2 ~T	-0.272819	0.200642	-1.36	0.1898	((T-1.08e+03)/3e+01)
3 ~LSR	-0.522892	0.200642	-2.61	0.0174	(LSR+2.5229)
4 ~LP	0.055605	0.200519	0.28	0.7845	((LP-4.5155e-01)/4.5155e
5 ~LST	0.048172	0.163865	0.29	0.7720	(LST-3.0105e-01)/3.0105
6 ~T*LSR	-0.187500	0.224306	-0.84	0.4136	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.192328	0.224235	-0.86	0.4017	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	0.075005	0.200639	0.37	0.7127	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.185260	0.224235	-0.83	0.4190	(LSR+2.5229)*((LP-4.5155
10 ~LSR*LST	0.175012	0.200639	0.87	0.3940	(LSR+2.5229)*((LST-3.010
11 ~LP*LST	0.097074	0.200532	0.48	0.6339	((LP-4.5155e-01)/4.5155e
No. cases = 30 R-sq. = 0.3900 RMS Error = 0.8972					
Resid. df = 19 R-sq-adj. = 0.0690 Cond. No. = 1.023					
~ indicates factors are transformed.					

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMPSTRESS@MULREG, Model DESIGN_COPY, Response SBA					Mulreg @TMPSTRESS@MULREG, Model DESIGN_COPY, Response SBA				
Term	df	P-Remove	P-Enter		Term	df	P-Remove	P-Enter	
1 1	1	0.000			1 1	1	0.000		
2 T	1	0.190			2 T	1		0.144	
3 LSR	1	0.017			3 LSR	1	0.009		
4 LP	1	0.785			4 LP	1		0.772	
5 LST	1	0.772			5 LST	1		0.750	
6 T*LSR	1	0.414			6 T*LSR	1		0.379	
7 T*LP	1	0.402			7 T*LP	1		0.357	
8 T*LST	1	0.713			8 T*LST	1		0.696	
9 LSR*LP	1	0.419			9 LSR*LP	1		0.385	
10 LSR*LST	1	0.394			10 LSR*LST	1		0.359	
11 LP*LST	1	0.634			11 LP*LST	1		0.607	
No. cases = 30 R-sq. = 0.3900 RMS Error = 0.8972					No. cases = 30 R-sq. = 0.2198				
Resid. df = 19 R-sq-adj. = 0.0690					Resid. df = 28 R-sq-adj. = 0.1920				
Obey Hierarchy: no					Obey Hierarchy: no				

A-4.—Subsolvus as-large-as grain size regression results.

## MODEL TMPSUBALA

Least Squares Coefficients, Response SBA, Model TMPSUBALA					
Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	7.650000	0.152606	50.13	0.0001	
2 ~LSR	-0.525000	0.186904	-2.81	0.0090	(LSR+2.5229)
No. cases = 30    R-sq. = 0.2198    RMS Error = 0.8359					
Resid. df = 28    R-sq-adj. = 0.1920    Cond. No. = 1					
~ indicates factors are transformed.					

## ANOVA

Least Squares Summary ANOVA, Response SBA Model TMPSUBALA					
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.
1 Total(Corr.)	29	25.07500			
2 Regression	1	5.51250	5.51250	7.89	0.0090
3 Residual	28	19.56250	0.69866		
R-sq. = 0.2198					
R-sq-adj. = 0.1920					

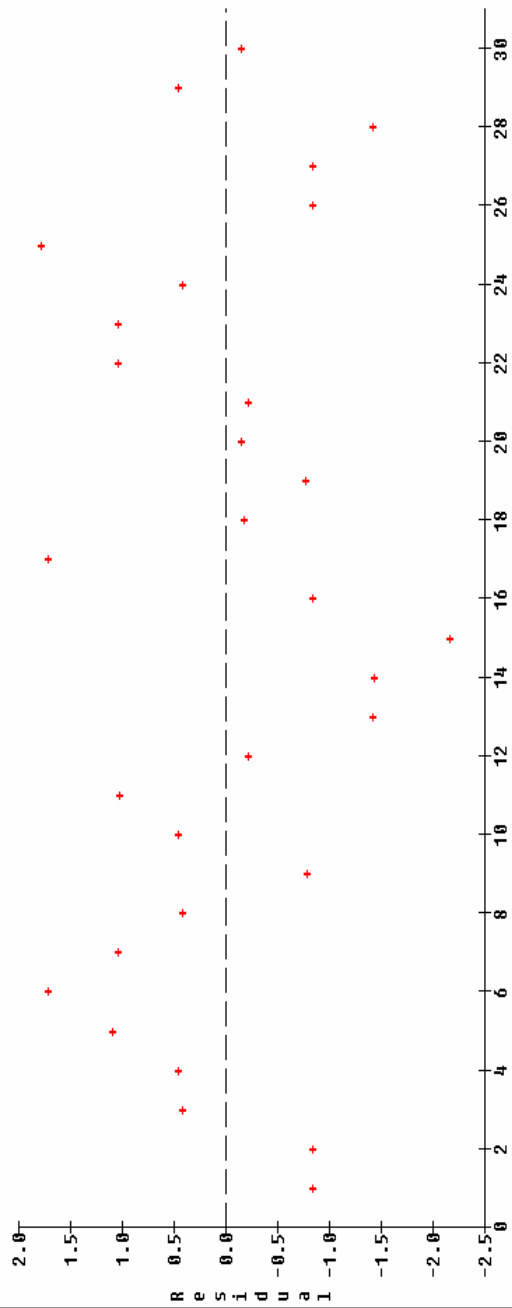
  

Least Squares Components ANOVA, Response SBA Model TMPSUBALA					
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.
1 Constant	1	1756			
2 ~LSR	1	5.51250	5.51250	7.89	0.0090
3 Residual	28	19.56250	0.69866		
~ indicates factors are transformed. R-sq. = 0.2198					
are transformed. R-sq-adj. = 0.1920					
Type 3 sum of squares.					

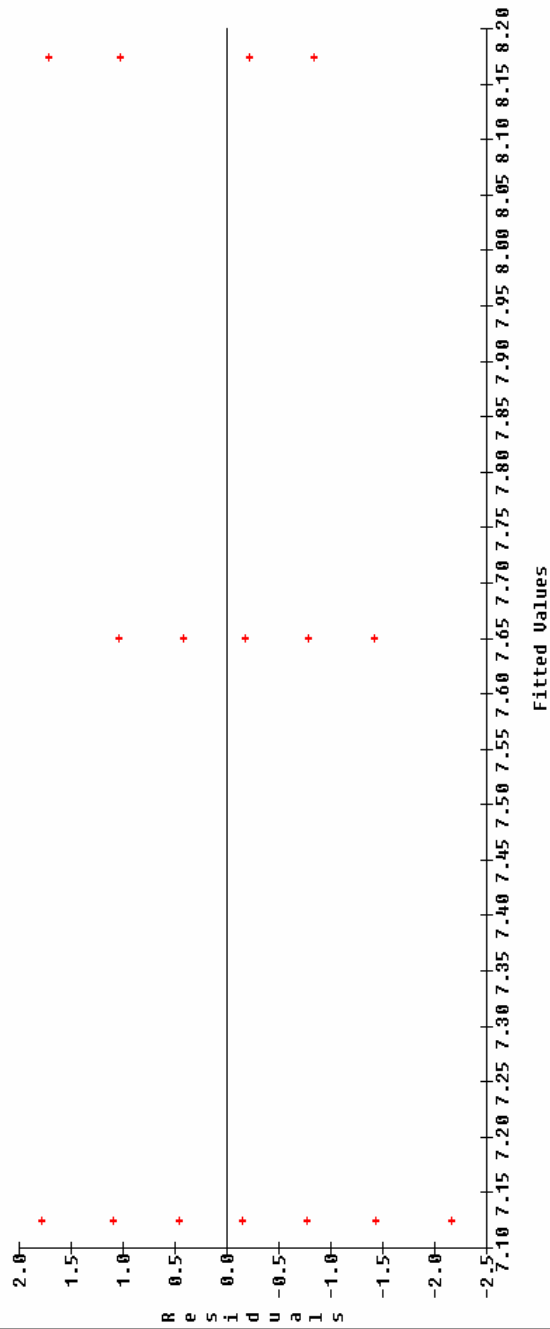
A-4.—Subsolvus as-large-as grain size regression results.



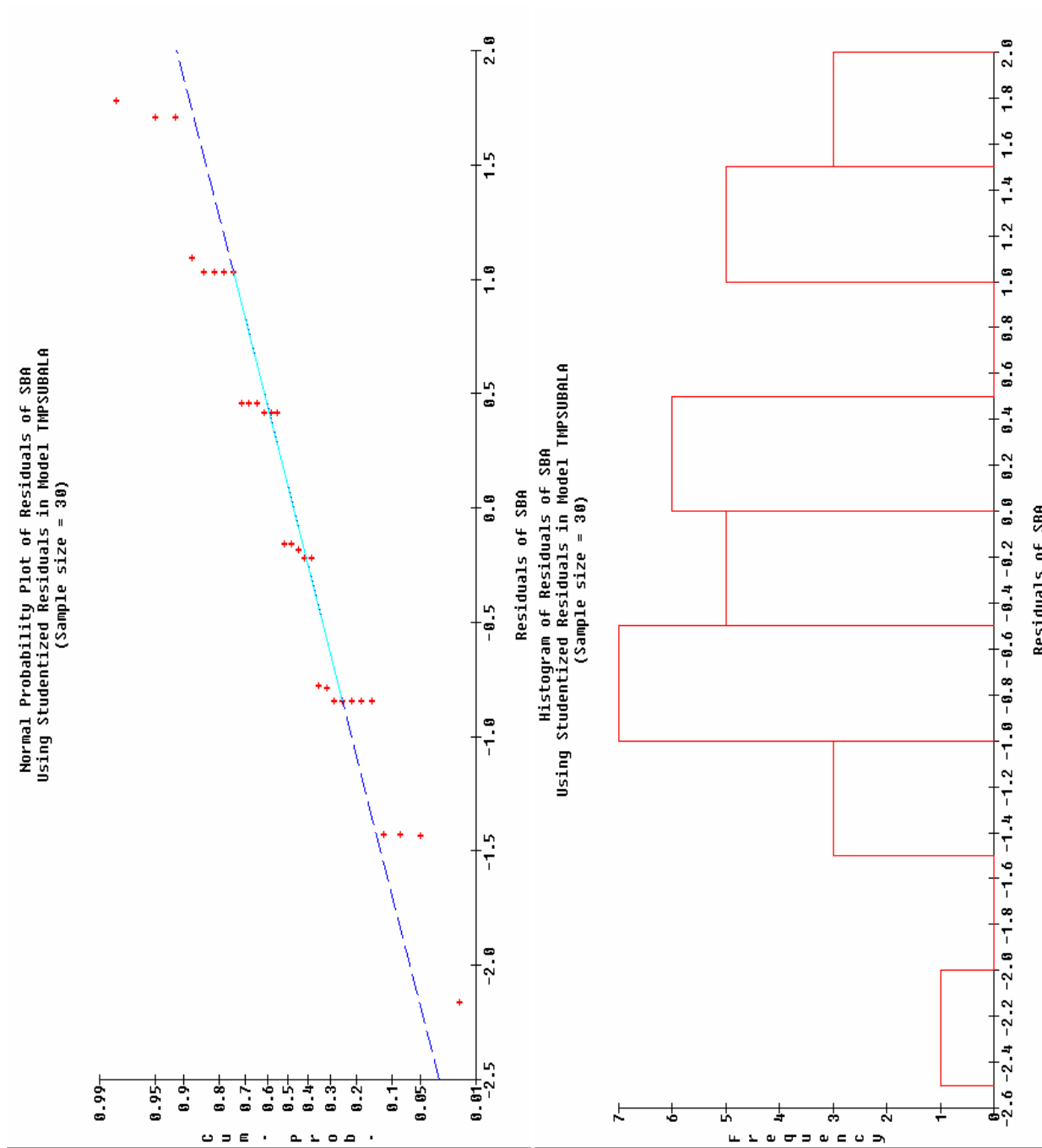
Case Order Graph of Residuals of SBA  
Using Studentized Residuals in Model THPSUBALA



Case Number  
Residuals of SBA vs Fitted Values  
Using Studentized Residuals in Model THPSUBALA

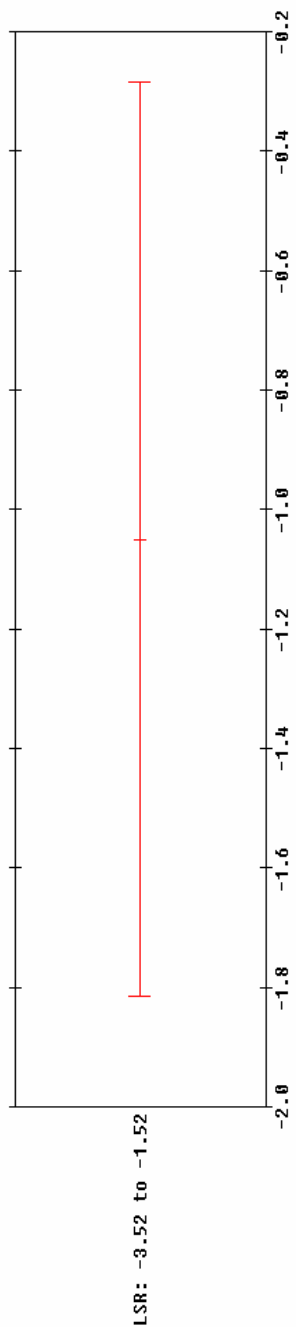


A-4.—Subsolvus as-large-as grain size regression results.

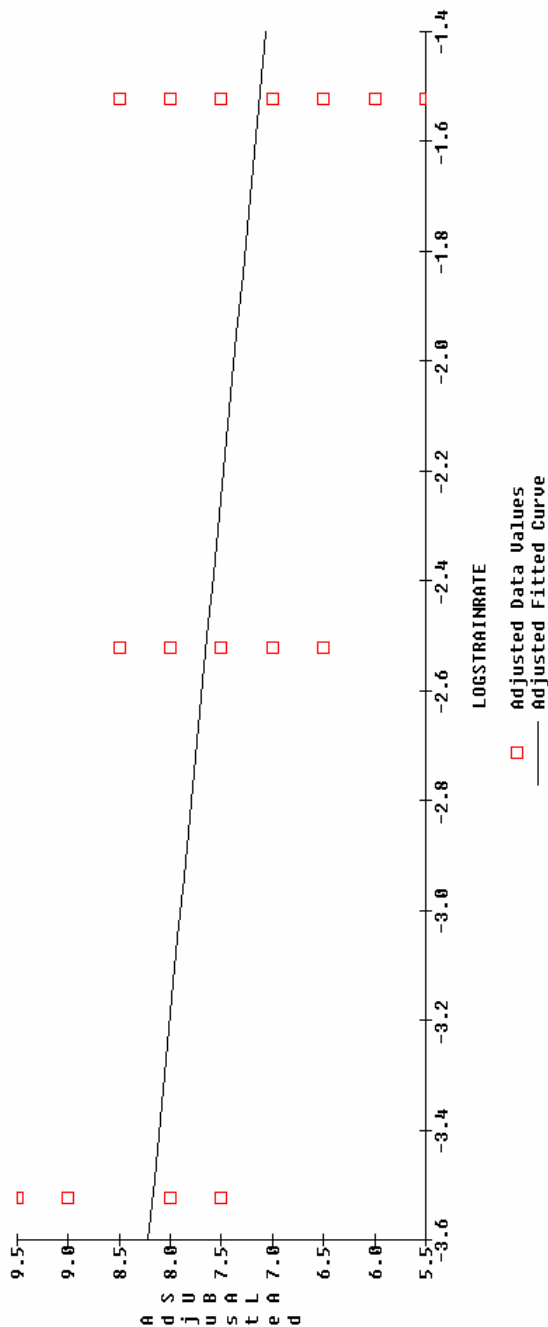


A-4.—Subsolvus as-large-as grain size regression results.

MuIreg @TMPSTRESS@MULREG, Model TMPSUBALA  
Main Effects on Response SUBALA  
(with 95% Confidence Intervals)

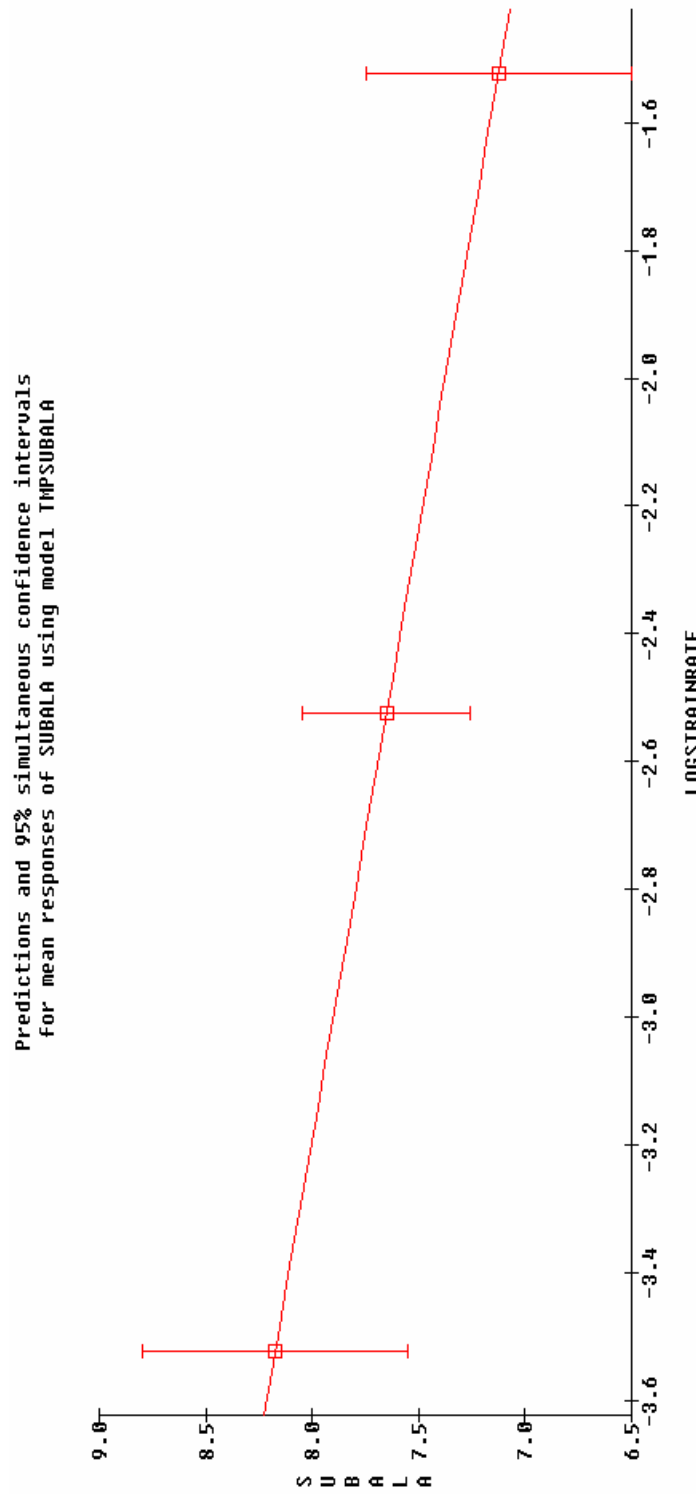


SUBALA vs LOGSTRAINRATE, Adjusted for Remaining Predictors  
Using MuIreg @TMPSTRESS@MULREG, Model TMPSUBALA



A-4.—Subsolvus as-large-as grain size regression results.

Predictions and 95% simultaneous confidence intervals for mean responses of SUBALA using model TMPSUBALA				
LSR:	-3.5229	-2.5229	-1.5229	
<hr/>				
Lower	7.551329	7.255556	6.501329	
Predicted	8.175000	7.650000	7.125000	
Upper	8.798671	8.044444	7.748671	



A-4.—Subsolvus as-large-as grain size regression results.

# All Terms

Least Squares Coefficients, Response SPG, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	5.966475	0.078516	75.99	0.0001	
2 ~T	-0.273572	0.096145	-2.85	0.0103	((T-1.08e+03)/3e+01)
3 ~LSR	0.135932	0.096145	1.41	0.1736	(LSR+2.5229)
4 ~LP	-0.167374	0.096086	-1.74	0.0977	((LP-4.5155e-01)/4.5155e
5 ~LST	-0.222068	0.078522	-2.83	0.0107	((LST-3.0105e-01)/3.0105
6 ~T*LSR	0.137500	0.107484	1.28	0.2162	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.127041	0.107450	-1.18	0.2517	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	-0.145010	0.096143	-1.51	0.1479	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.082638	0.107450	-0.77	0.4513	(LSR+2.5229)*((LP-4.5155
10 ~LSR*LST	-0.045003	0.096143	-0.47	0.6451	(LSR+2.5229)*((LST-3.010
11 ~LP*LST	-0.067857	0.096092	-0.71	0.4887	((LP-4.5155e-01)/4.5155e
No. cases = 30 R-sq. = 0.5949 RMS Error = 0.4299					
Resid. df = 19 R-sq-adj. = 0.3817 Cond. No. = 1.023					
~ indicates factors are transformed.					

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response SPG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.010	
3 LSR	1	0.174	
4 LP	1	0.098	
5 LST	1	0.011	
6 T*LSR	1	0.216	
7 T*LP	1	0.252	
8 T*LST	1	0.148	
9 LSR*LP	1	0.451	
10 LSR*LST	1	0.645	
11 LP*LST	1	0.489	

No. cases = 30 R-sq. = 0.5949 RMS Error = 0.4299  
 Resid. df = 19 R-sq-adj. = 0.3817 Obey Hierarchy: no

Mulreg @TMPSTRESS@MULREG, Model DESIGN\_COPY, Response SPG

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.010	
3 LSR	1		0.178
4 LP	1		0.103
5 LST	1		0.010
6 T*LSR	1		0.221
7 T*LP	1		0.259
8 T*LST	1		0.146
9 LSR*LP	1		0.477
10 LSR*LST	1		0.658
11 LP*LST	1		0.504

No. cases = 30 R-sq. = 0.4117  
 Resid. df = 26 R-sq-adj. = 0.3439  
 Obey Hierarchy: no

## MODEL TMPSPUGS

Least Squares Coefficients, Response SPG, Model TMPSPUGS

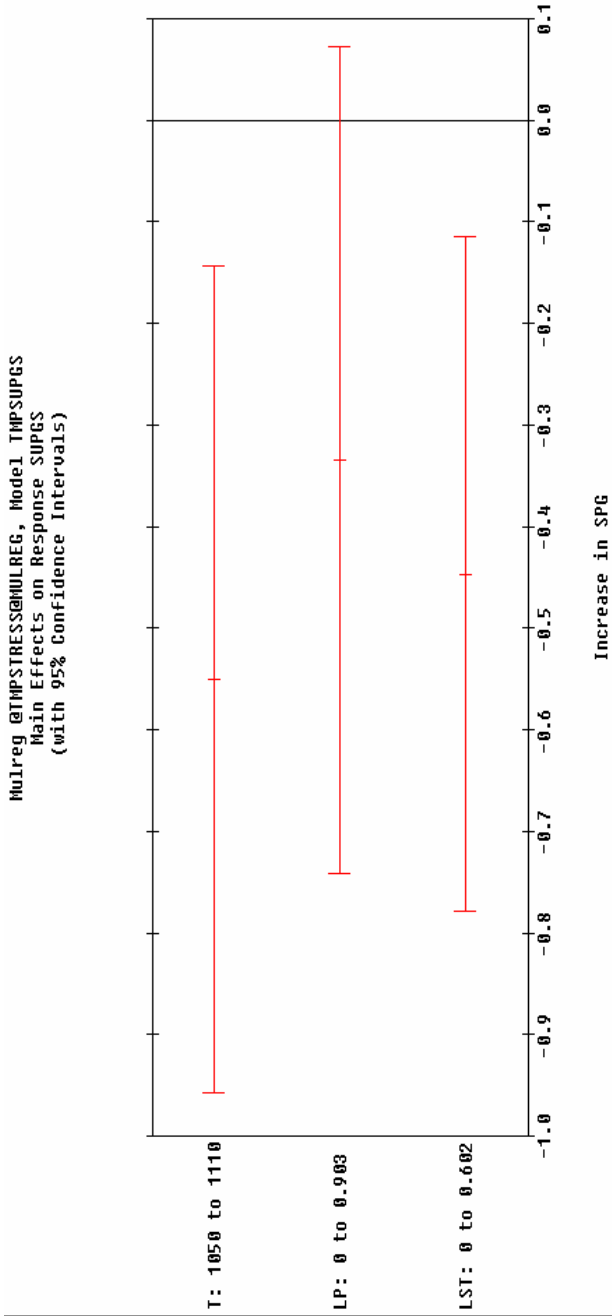
Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	5.966475	0.080882	73.77	0.0001	
2 ~T	-0.275000	0.099034	-2.78	0.0100	((T-1.08e+03)/3e+01)
3 ~LP	-0.167369	0.098981	-1.69	0.1028	((LP-4.5155e-01)/4.5155e
4 ~LST	-0.223348	0.080866	-2.76	0.0104	((LST-3.0105e-01)/3.0105
No. cases = 30 R-sq. = 0.4117 RMS Error = 0.4429					
Resid. df = 26 R-sq-adj. = 0.3439 Cond. No. = 1.023					
~ indicates factors are transformed.					

A-5.—Supersolvus mean grain size regression results.

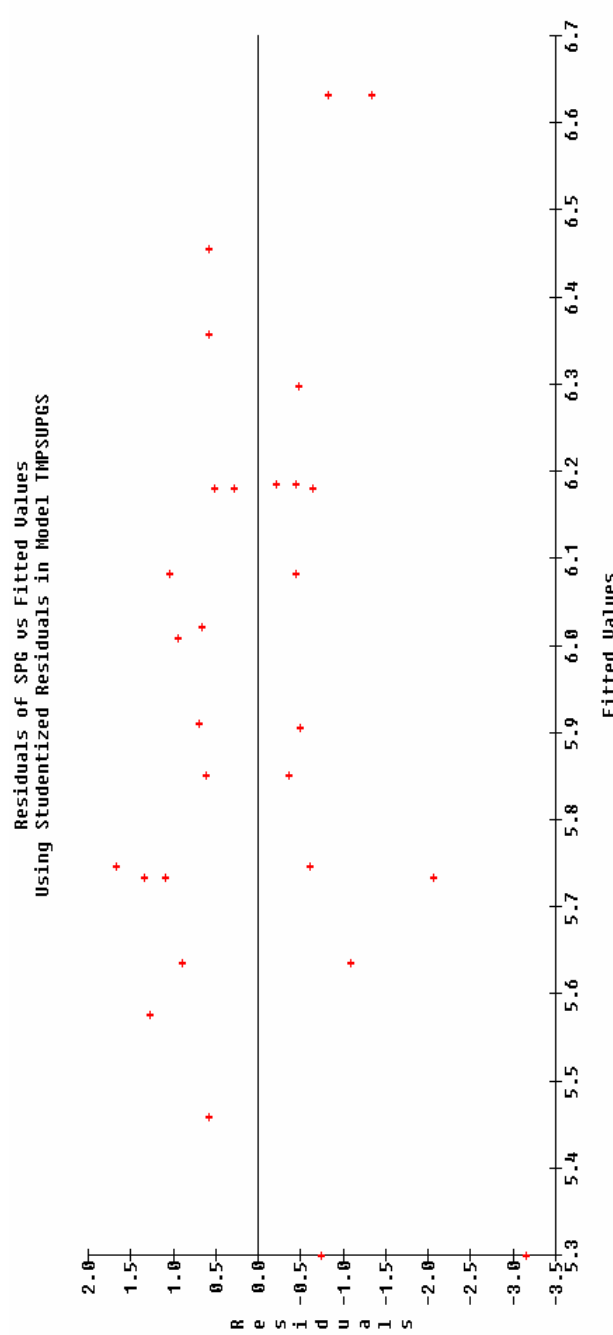
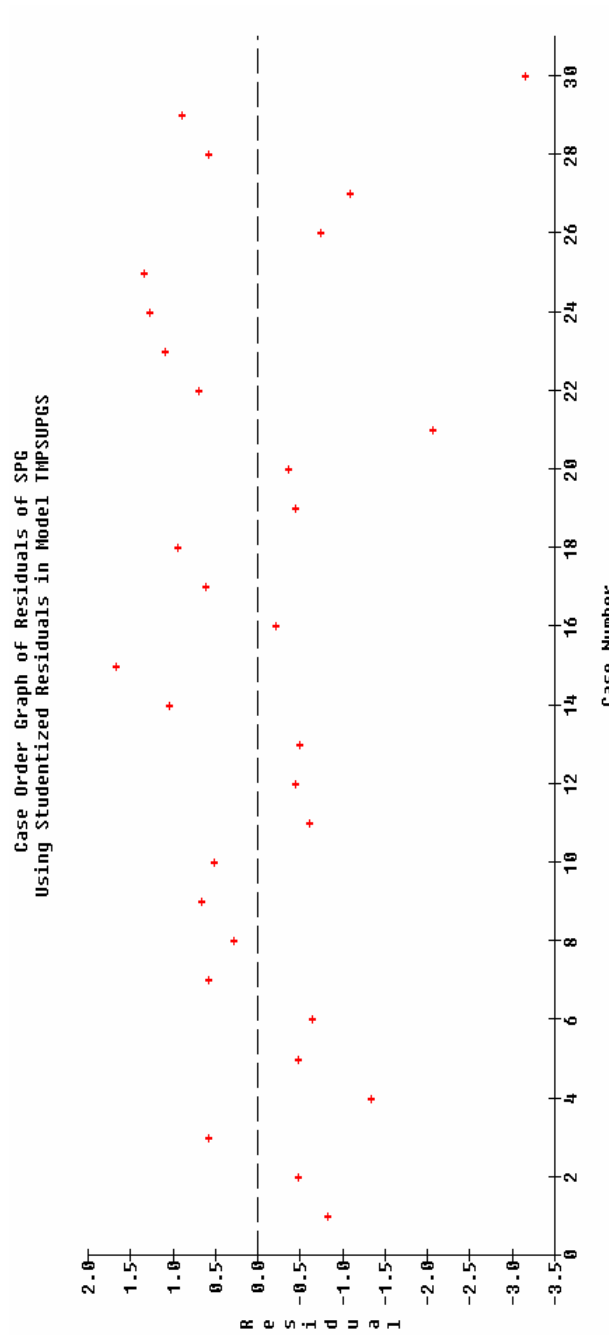


# ANOVA

Least Squares Summary ANOVA, Response SPG Model TMPSUPGS						Least Squares Components ANOVA, Response SPG Model TMPSUPGS						
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Transformed Term
1 Total(Corr.)	29	8.669667				1 Constant	1	1067				
2 Regression	3	3.569682	1.189894	6.07	0.0028	2 ~T	1	1.512500	1.512500	7.71	0.0100	((T-1.08e+03)/3e+01)
3 Residual	26	5.099985	0.196153			3 ~LP	1	0.560849	0.560849	2.86	0.1028	((LP-4.5155e-01)/4.5155e
						4 ~LST	1	1.496333	1.496333	7.63	0.0104	((LST-3.0105e-01)/3.0105
						5 Residual	26	5.099985	0.196153			
						~ indicates factors R-sq. = 0.4117 are transformed. R-sq-adj. = 0.3439 Type 3 sum of squares.						

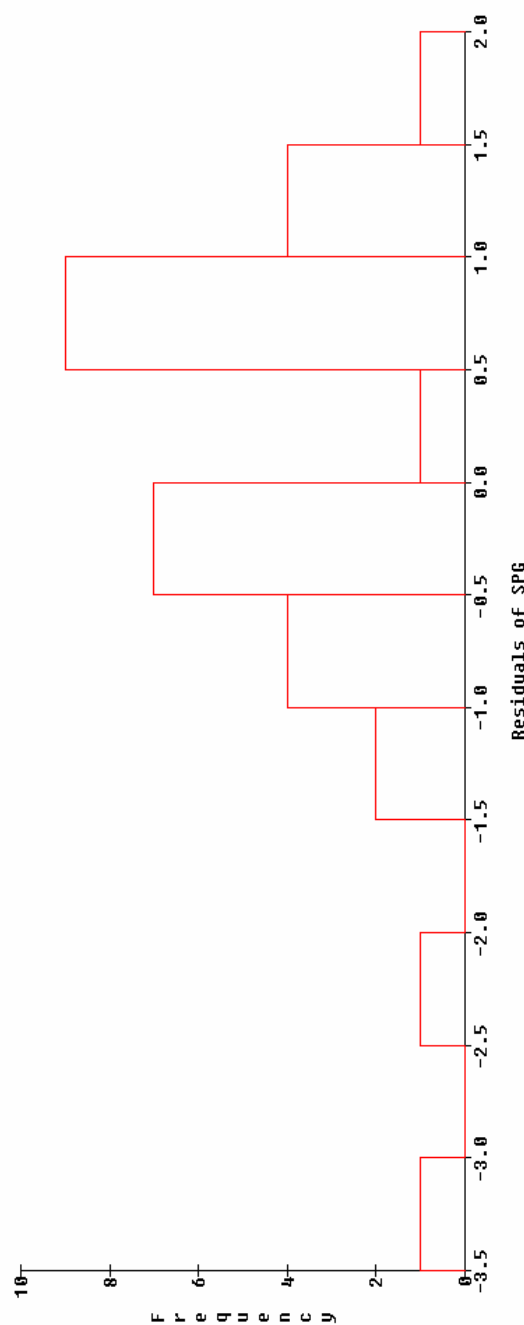
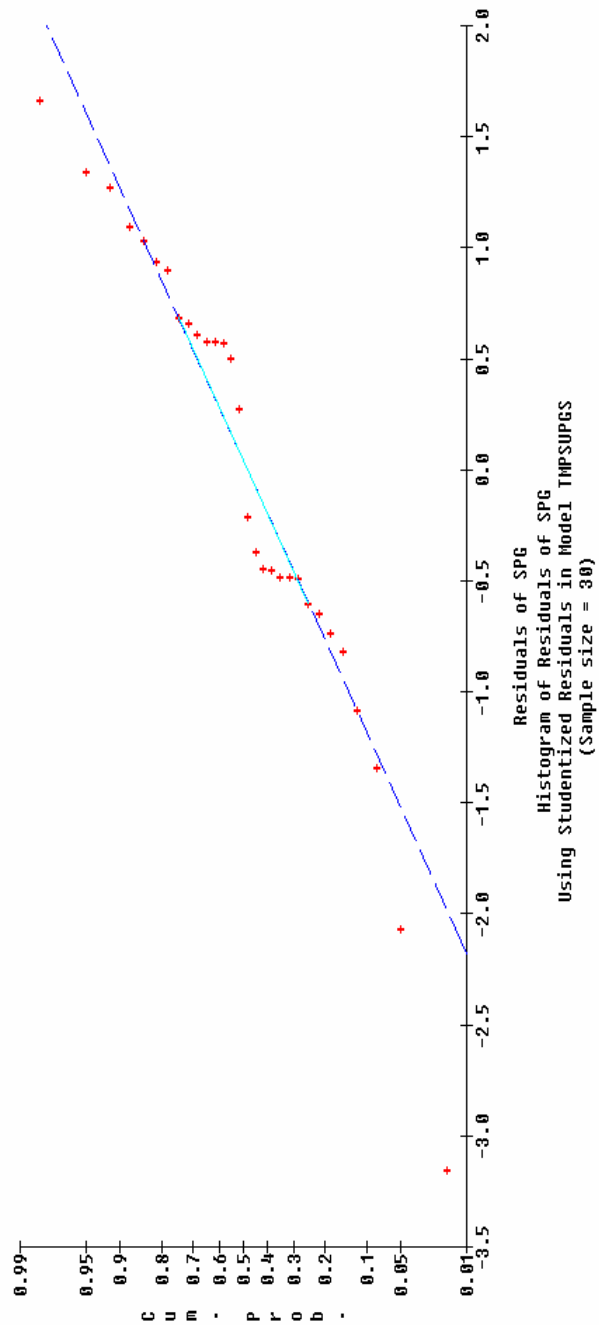


A-5.—Supersolvus mean grain size regression results.



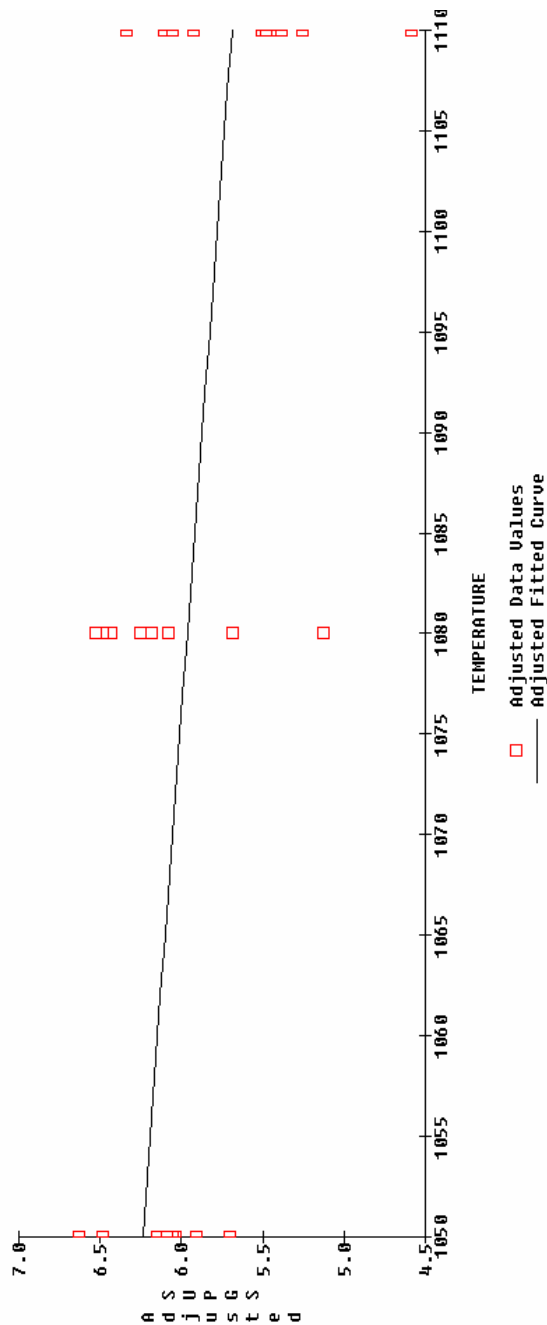
A-5.—Supersolvus mean grain size regression results.

Normal Probability Plot of Residuals of SPG  
Using Studentized Residuals in Model T1MPSUPG6  
(Sample size = 30)

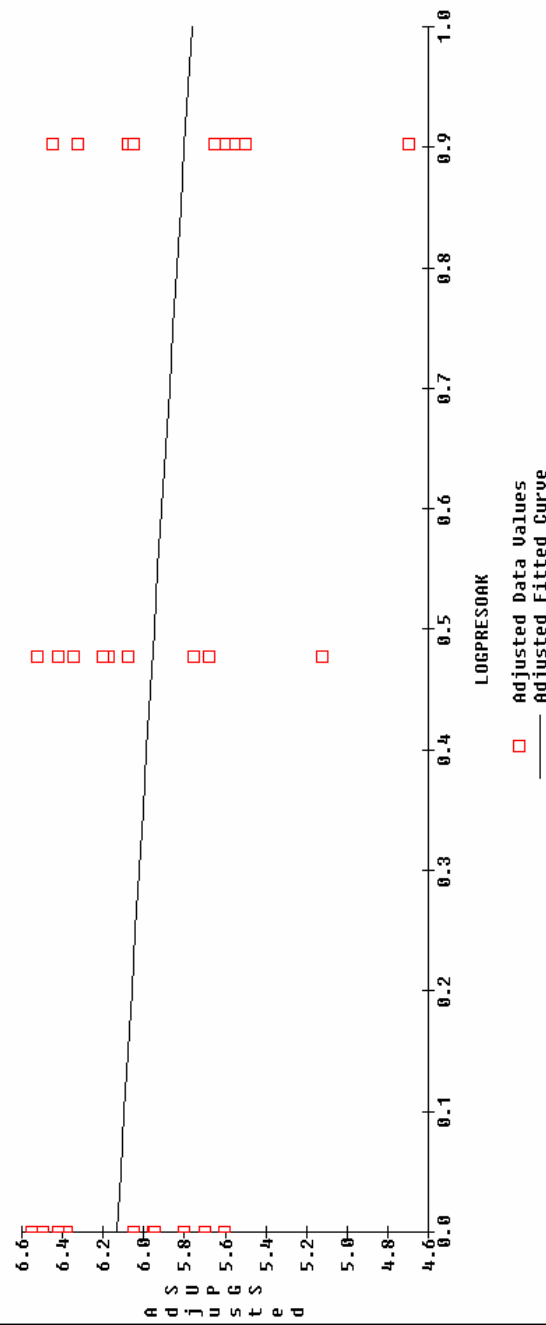


A-5.—Supersolvus mean grain size regression results.

SUPGS vs TEMPERATURE, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUPGS

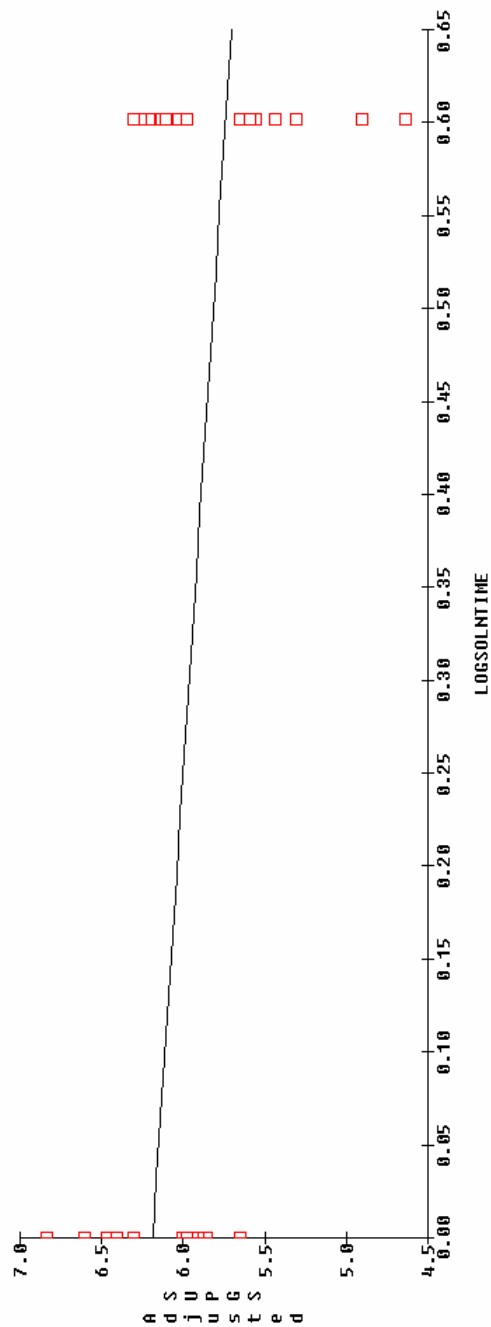


SUPGS vs LOGPRESOAK, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUPGS



A-5.—Supersolvus mean grain size regression results.

SUPGS vs LOGSOLNTIME, Adjusted for Remaining Predictors  
Using Multireg @TMPSTRESS@MULREG, Model TMPSUPGS

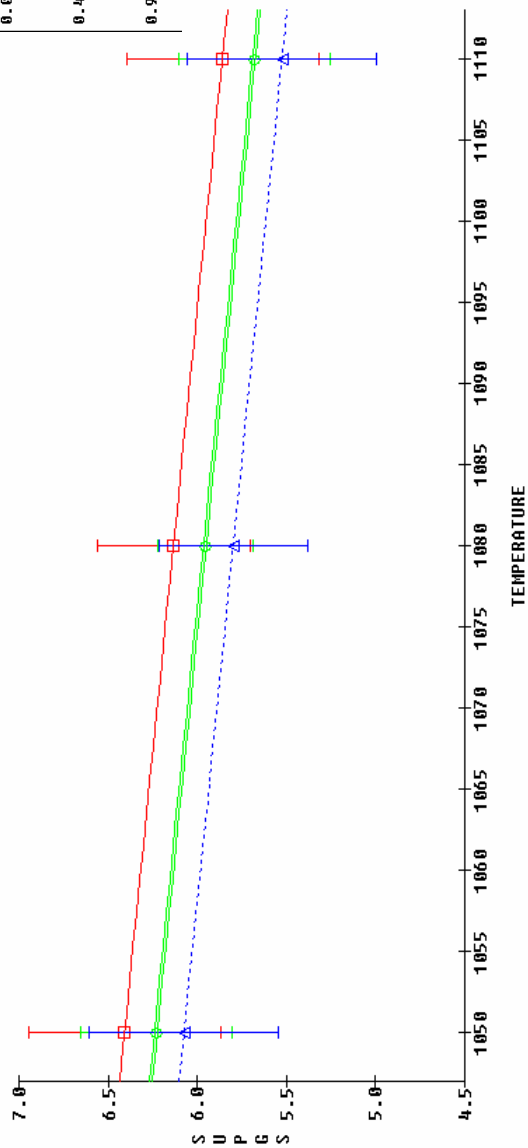


□ Adjusted Data Values  
— Adjusted Fitted Curve

Predictions and 95% simultaneous confidence intervals  
for mean responses of SUPGS using model TMPSUPGS  
LST = 0.30103

Predictions and 95% simultaneous confidence intervals  
for mean responses of SUPGS using model TMPSUPGS  
LST = 0.30103

LP	T=1050	T=1080	T=1110
0.0000	Lower 5.869513 Predicted 6.488860 Upper 6.948206	5.705723 6.133860 6.561996	5.319513 5.858860 6.398206
0.4771	Lower 5.808374 Predicted 6.232020 Upper 6.655666	5.688911 5.957020 6.225128	5.258374 5.682020 6.105666
0.9031	Lower 5.542344 Predicted 6.074121 Upper 6.605897	5.380561 5.799121 6.217680	4.992344 5.524121 6.055897



A-5.—Supersolvus mean grain size regression results.



# ALL TERMS

Least Squares Coefficients, Response SPA, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	1.696492	0.330914	5.13	0.0001	
2 ~T	-1.166137	0.405209	-2.88	0.0096	((T-1.08e+03)/3e+01)
3 ~LSR	-1.191713	0.405209	-2.94	0.0084	(LSR+2.5229)
4 ~LP	-0.698299	0.404961	-1.72	0.1009	((LP-4.5155e-01)/4.5155e
5 ~LST	-0.189514	0.330936	-0.57	0.5736	(LST-3.0105e-01)/3.0105
6 ~T*LSR	-1.312500	0.453002	-2.90	0.0092	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.783000	0.452857	-1.73	0.1000	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	0.025002	0.405204	0.06	0.9514	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.732556	0.452857	-1.62	0.1222	(LSR+2.5229)*((LP-4.5155
10 ~LSR*LST	-0.050003	0.405204	-0.12	0.9031	(LSR+2.5229)*((LST-3.010
11 ~LP*LST	0.327030	0.404988	0.81	0.4294	((LP-4.5155e-01)/4.5155e

No. cases = 30 R-sq. = 0.6490 RMS Error = 1.812

Resid. df = 19 R-sq-adj. = 0.4643 Cond. No. = 1.023

~ indicates factors are transformed.

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMPSTRESS\MULREG, Model DESIGN\_COPY, Response SPA

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.010	
3 LSR	1	0.008	
4 LP	1	0.101	
5 LST	1	0.574	
6 T*LSR	1	0.009	
7 T*LP	1	0.100	
8 T*LST	1	0.951	
9 LSR*LP	1	0.122	
10 LSR*LST	1	0.903	
11 LP*LST	1	0.429	

No. cases = 30 R-sq. = 0.6490 RMS Error = 1.812

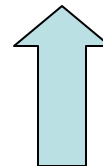
Resid. df = 19 R-sq-adj. = 0.4643 Obey Hierarchy: no

Mulreg @TMPSTRESS\MULREG, Model DESIGN\_COPY, Response SPA

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.005	
3 LSR	1	0.004	
4 LP	1	0.077	
5 LST	1		0.564
6 T*LSR	1	0.005	
7 T*LP	1	0.076	
8 T*LST	1		0.949
9 LSR*LP	1	0.096	
10 LSR*LST	1		0.898
11 LP*LST	1		0.406

No. cases = 30 R-sq. = 0.6309 RMS Error = 1.689

Resid. df = 23 R-sq-adj. = 0.5347 Obey Hierarchy: no



A-6.—Supersolvus as-large-as grain size regression results.

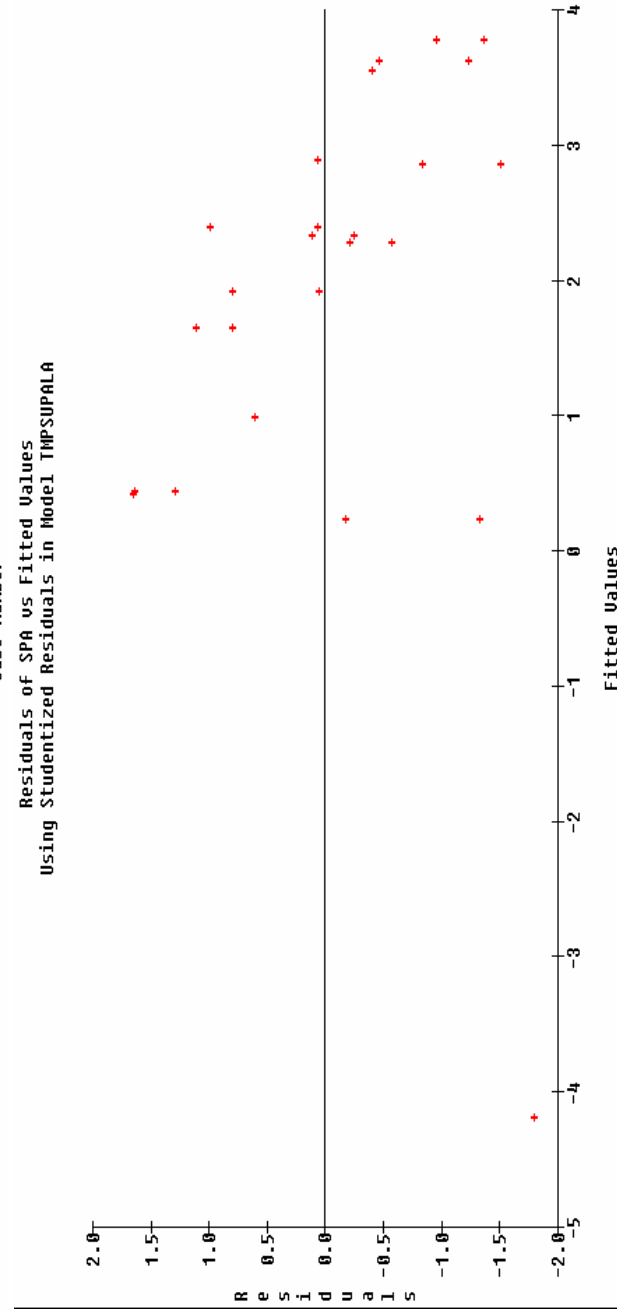
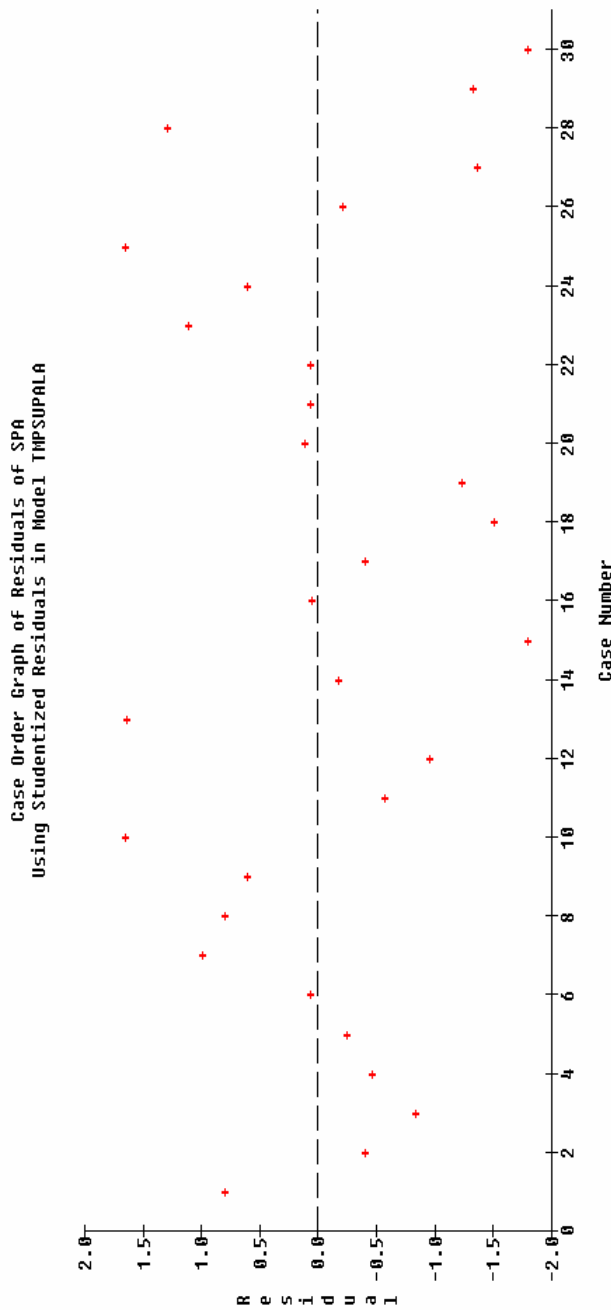
## MODEL TMPSUPALA

Least Squares Coefficients, Response SPA, Model TMPSUPALA						
Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term	
1 1	1.696504	0.308411	5.50	0.0001		
2 ~T	-1.166139	0.377654	-3.09	0.0052	((T-1.08e+03)/3e+01)	
3 ~LSR	-1.191710	0.377654	-3.16	0.0044	(LSR+2.5229)	
4 ~LP	-0.698321	0.377422	-1.85	0.0772	((LP-4.5155e-01)/4.5155e	
5 ~T*LSR	-1.312500	0.422196	-3.11	0.0049	((T-1.08e+03)/3e+01)*(LS	
6 ~T*LP	-0.783000	0.422061	-1.86	0.0764	((T-1.08e+03)/3e+01)*(L	
7 ~LSR*LP	-0.732556	0.422061	-1.74	0.0960	(LSR+2.5229)*((LP-4.5155	
No. cases = 30 R-sq. = 0.6309 RMS Error = 1.689						
Resid. df = 23 R-sq-adj. = 0.5347 Cond. No. = 1.023						
~ indicates factors are transformed.						

## ANOVA

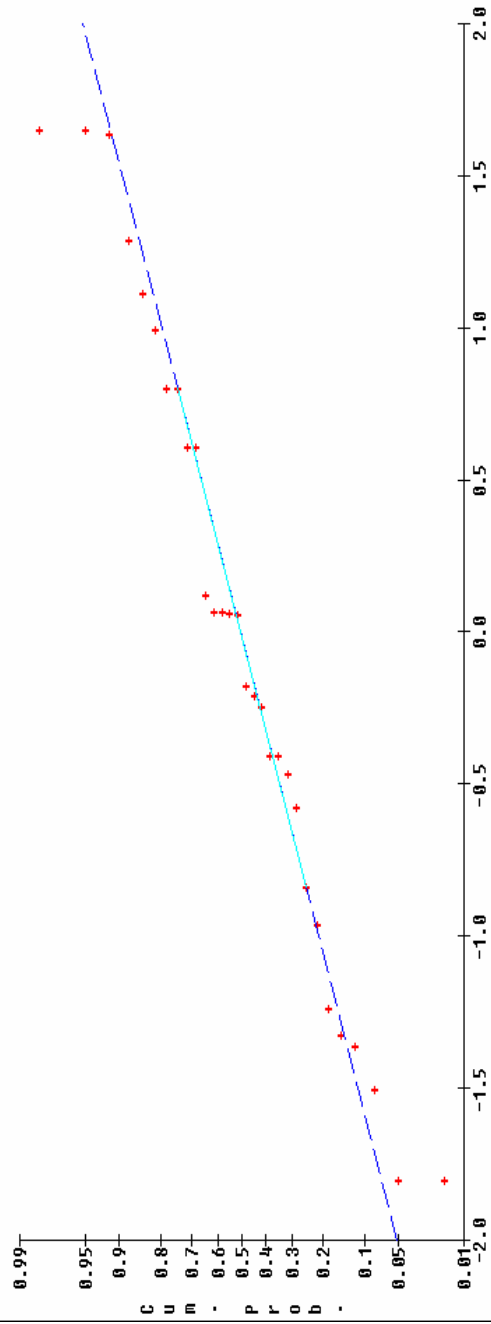
Least Squares Summary ANOVA, Response SPA Model TMPSUPALA											
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Least Squares Components ANOVA, Response SPA Model TMPSUPALA					
1 Total(Corr.)	29	177.7417				Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif. Transformed Term
2 Regression	6	112.1459	18.6910	6.55	0.0004	1 Constant	1	86.2978			
3 Linear	3	65.3556	21.7852	7.64	0.0010	2 ~T	1	27.1933	27.1933	9.54	0.0052 ((T-1.08e+03)/3e+01)
4 Non-linear	3	45.9699	15.3233	5.37	0.0059	3 ~LSR	1	28.3989	28.3989	9.96	0.0044 (LSR+2.5229)
5 Residual	23	65.5958	2.8520			4 ~LP	1	9.7635	9.7635	3.42	0.0772 ((LP-4.5155e-01)/4.5155e-01)
						5 ~T*LSR	1	27.5625	27.5625	9.66	0.0049 ((T-1.08e+03)/3e+01)*(LSR+2.5229)
						6 ~T*LP	1	9.8157	9.8157	3.44	0.0764 ((T-1.08e+03)/3e+01)*(LP-4.5155e-01)
						7 ~LSR*LP	1	8.5917	8.5917	3.01	0.0960 (LSR+2.5229)*((LP-4.5155e-01)*(LSR+2.5229))
						8 Residual	23	65.5958	2.8520		
						~ indicates factors are transformed. R-sq. = 0.6309					
						Type 3 sum of squares. R-sq-adj. = 0.5347					

A-6.—Supersolvus as-large-as grain size regression results.

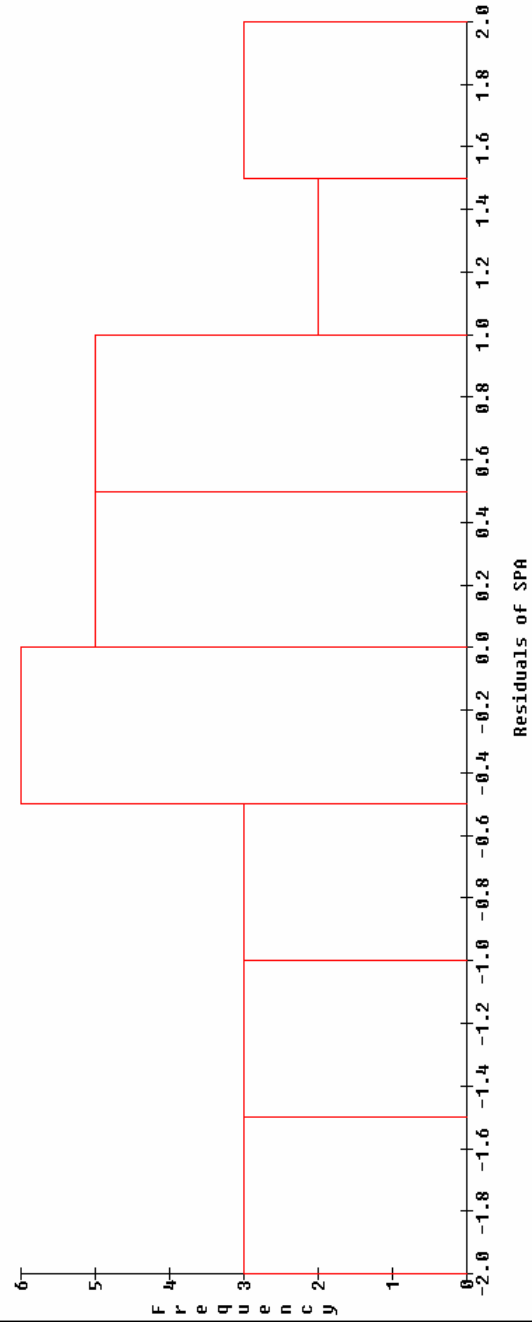


A-6.—Supersolvus as-large-as grain size regression results.

Normal Probability Plot of Residuals of SPA  
Using Studentized Residuals in Model TMPSUPALA  
(Sample size = 30)

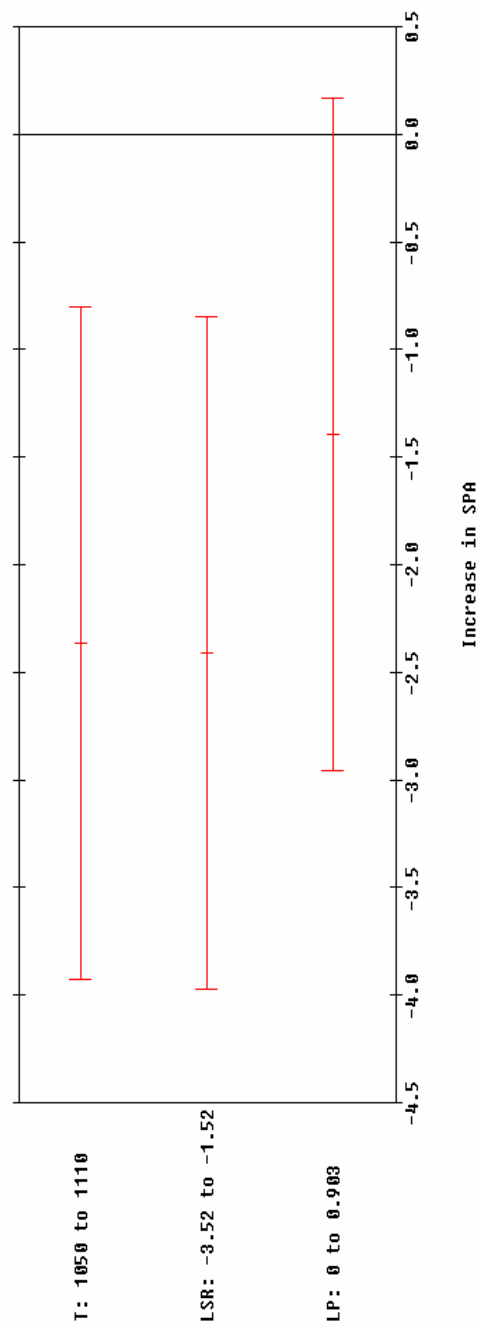


Histogram of Residuals of SPA  
Using Studentized Residuals in Model TMPSUPALA  
(Sample size = 30)

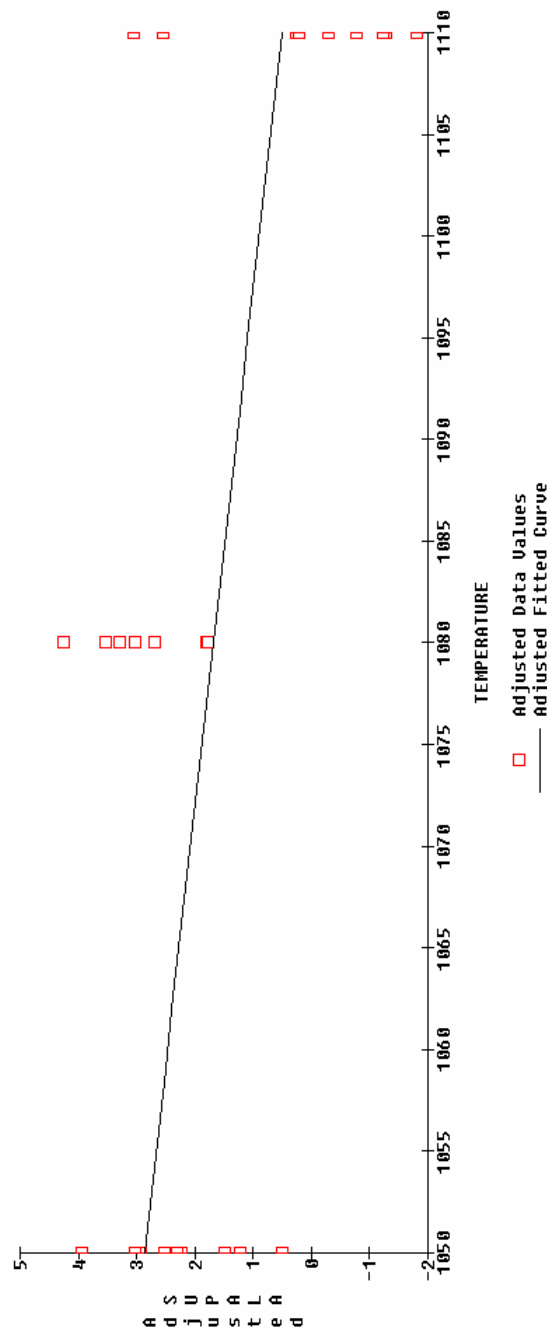


A-6.—Supersolvus as-large-as grain size regression results.

Mulreg @TMPSTRESS@MULREG, Model THPSUPALA  
Main Effects on Response SUPALA  
(with 95% Confidence Intervals)



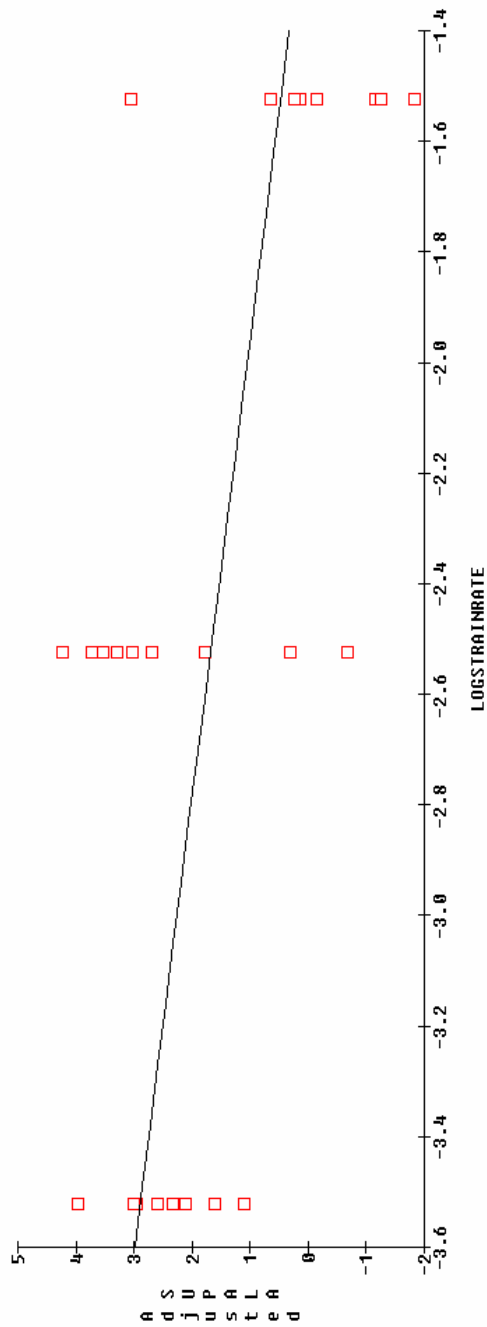
SUPALA vs TEMPERATURE, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model THPSUPALA



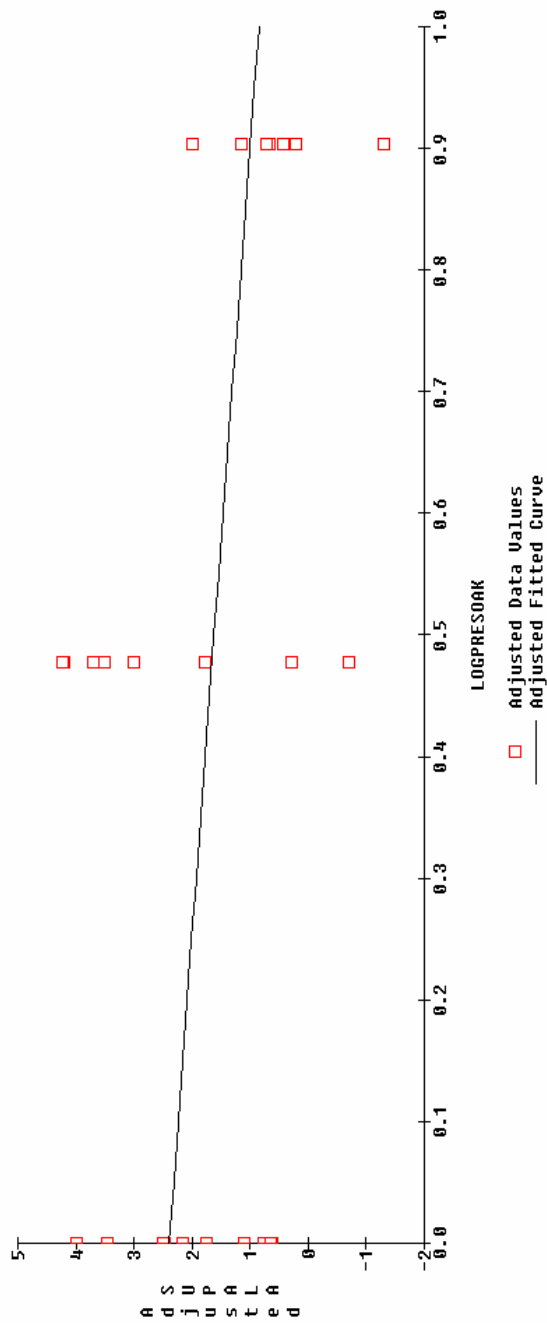
A-6.—Supersolvus as-large-as grain size regression results.



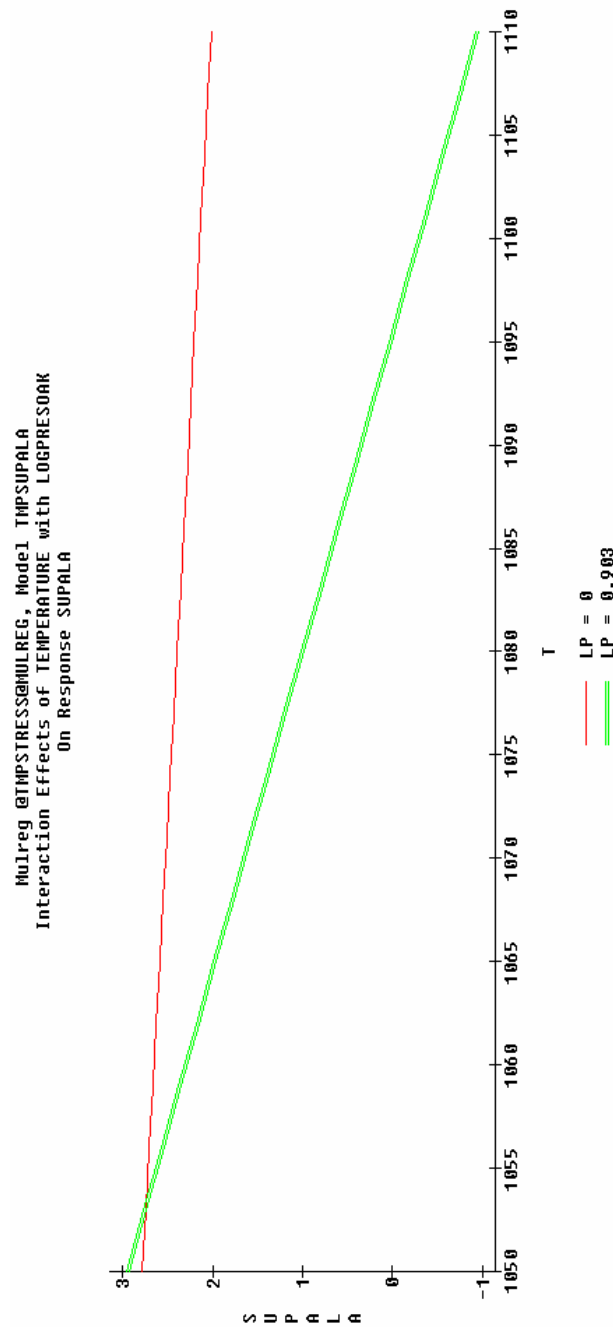
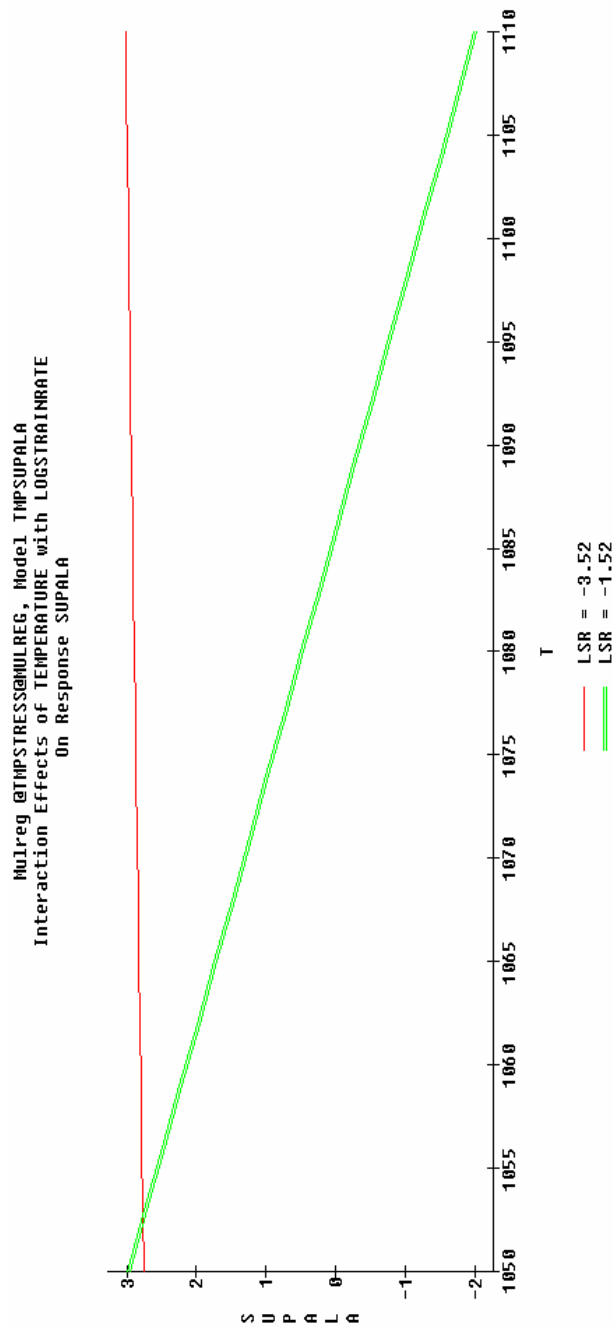
SUPALA vs LOGSTRAINRATE, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUPALA



SUPALA vs LOGPRESOAK, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUPALA

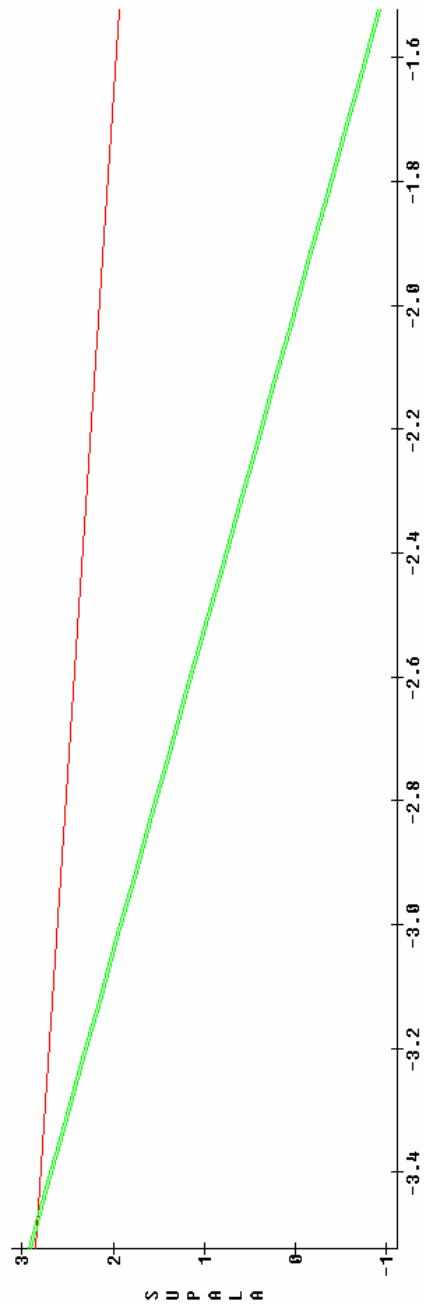


A-6.—Supersolvus as-large-as grain size regression results.



A-6.—Supersolvus as-large-as grain size regression results.

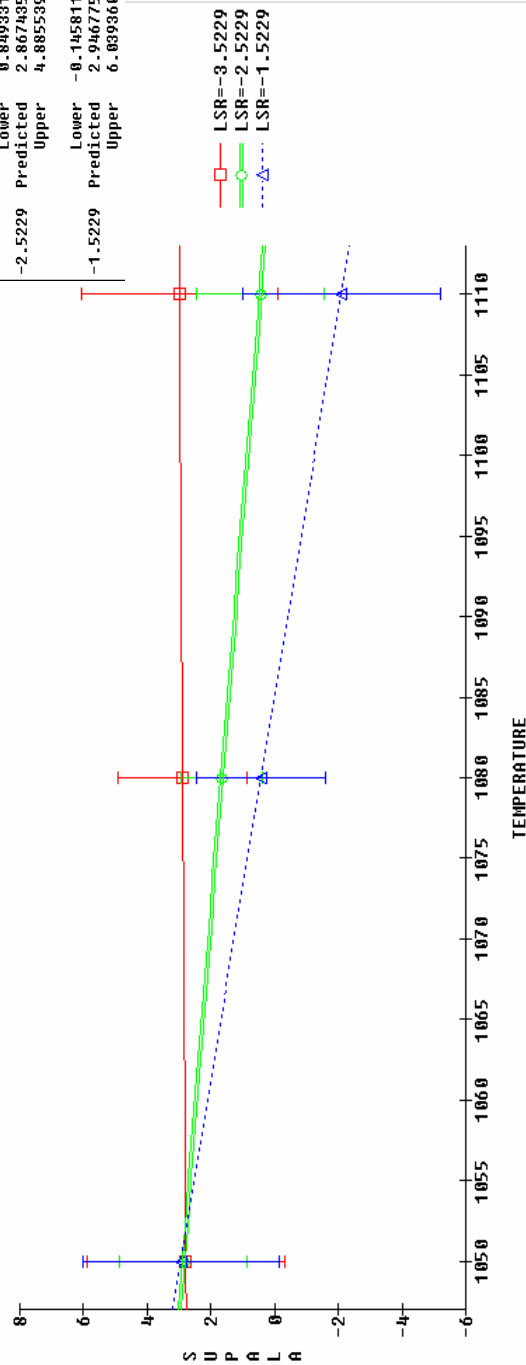
Mulreg @TMPSTRESS@HULREG, Model TMPSUPALA  
Interaction Effects of LOGSTRAINRATE with LOGPRESOAK  
On Response SUPALA



Predictions and 95% simultaneous confidence intervals  
for mean responses of SUPALA using model TMPSUPALA  
LP = 0.4771

LSR  
LP = 0  
LP = 0.903

Predictions and 95% simultaneous confidence intervals  
for mean responses of SUPALA using model TMPSUPALA  
LP = 0.4771



A-6.—Supersolvus as-large-as grain size regression results.

## All Terms

Least Squares Coefficients, Response SBPG, Model DESIGN

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	5.913509	0.078932	74.92	0.0001	
2 ~T	-0.059913	0.096654	-0.62	0.5427	((T-1.08e+03)/3e+01)
3 ~LSR	0.095384	0.096654	0.99	0.3361	(LSR+2.5229)
4 ~LP	-0.009991	0.096595	-0.10	0.9187	((LP-4.5155e-01)/4.5155e
5 ~LST	-0.193527	0.078937	-2.45	0.0241	(LST-3.0105e-01)/3.0105
6 ~T*LSR	0.318750	0.108054	2.95	0.0082	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.007872	0.108019	-0.07	0.9427	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	-0.030002	0.108019	-0.31	0.7596	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.033987	0.108019	-0.31	0.7565	(LSR+2.5229)*((LP-4.5155
10 ~LSR*LST	-0.015001	0.096652	-0.16	0.8783	(LSR+2.5229)*((LST-3.010
11 ~LP*LST	0.009611	0.096601	0.10	0.9218	((LP-4.5155e-01)/4.5155e
No. cases = 30 R-sq. = 0.4618 RMS Error = 0.4322					
Resid. df = 19 R-sq-adj. = 0.1785 Cond. No. = 1.023					
~ indicates factors are transformed.					

## FORWARD AND REVERSE STEPWISE SELECTION

Mulreg @TMPSTRESS@MULREG, Model DESIGN_COPY, Response SBPG					Mulreg @TMPSTRESS@MULREG, Model DESIGN_COPY, Response SBPG				
Term	df	P-Remove	P-Enter		Term	df	P-Remove	P-Enter	
1 1	1	0.000			1 1	1	0.000		
2 T	1	0.543			2 T	1		0.488	
3 LSR	1	0.336			3 LSR	1		0.268	
4 LP	1	0.919			4 LP	1		0.908	
5 LST	1	0.024			5 LST	1	0.009		
6 T*LSR	1	0.008			6 T*LSR	1	0.002		
7 T*LP	1	0.943			7 T*LP	1		0.928	
8 T*LST	1	0.760			8 T*LST	1		0.730	
9 LSR*LP	1	0.757			9 LSR*LP	1		0.736	
10 LSR*LST	1	0.878			10 LSR*LST	1		0.863	
11 LP*LST	1	0.922			11 LP*LST	1		0.912	
No. cases = 30 R-sq. = 0.4618 RMS Error = 0.4322					No. cases = 30 R-sq. = 0.4165				
Resid. df = 19 R-sq-adj. = 0.1785 Obey Hierarchy: no					Resid. df = 27 R-sq-adj. = 0.3733 Obey Hierarchy: no				

A-7.—Subsolvus plus supersolvus mean grain size regression results.

## MODEL TMPSUBPGS

Least Squares Coefficients, Response SBPG, Model TMPSUBPGS				
Term	Coeff.	Std. Error	T-value	Signif. Transformed Term
1 1	5.913320	0.068922	85.80	0.0001
2 ~LST	-0.193346	0.068927	-2.81	0.0092 ((LST-3.0105e-01)/3.0105
3 ~T*LSR	0.318750	0.094375	3.38	0.0022 ((T-1.08e+03)/3e+01)*(LS
No. cases = 30 R-sq. = 0.4165 RMS Error = 0.3775				
Resid. df = 27 R-sq-adj. = 0.3733 Cond. No. = 1				
~ indicates factors are transformed.				

## ANOVA

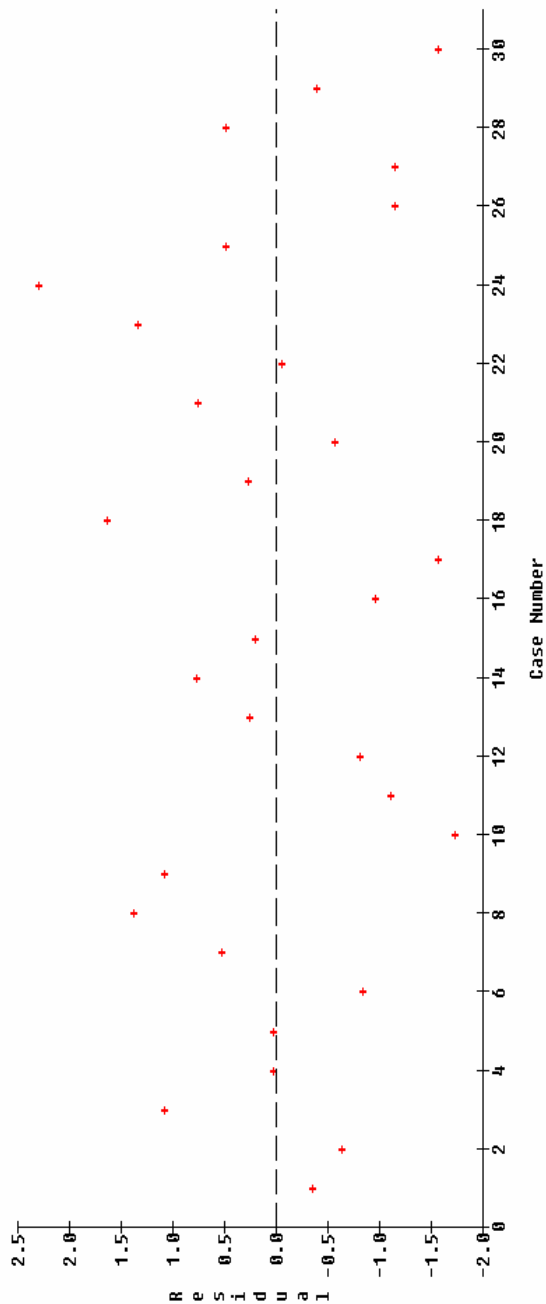
Least Squares Summary ANOVA, Response SBPG Model TMPSUBPGS				
Source	df	Sum Sq.	Mean Sq.	F-Ratio Signif.
1 Total(Corr.)	29	6.594667		
2 Regression	2	2.746958	1.373479	9.64 0.0007
3 Linear	1	1.121333	1.121333	7.87 0.0092
4 Non-Linear	1	1.625625	1.625625	11.41 0.0022
5 Residual	27	3.847708	0.142508	
R-sq. = 0.4165				
R-sq-adj. = 0.3733				

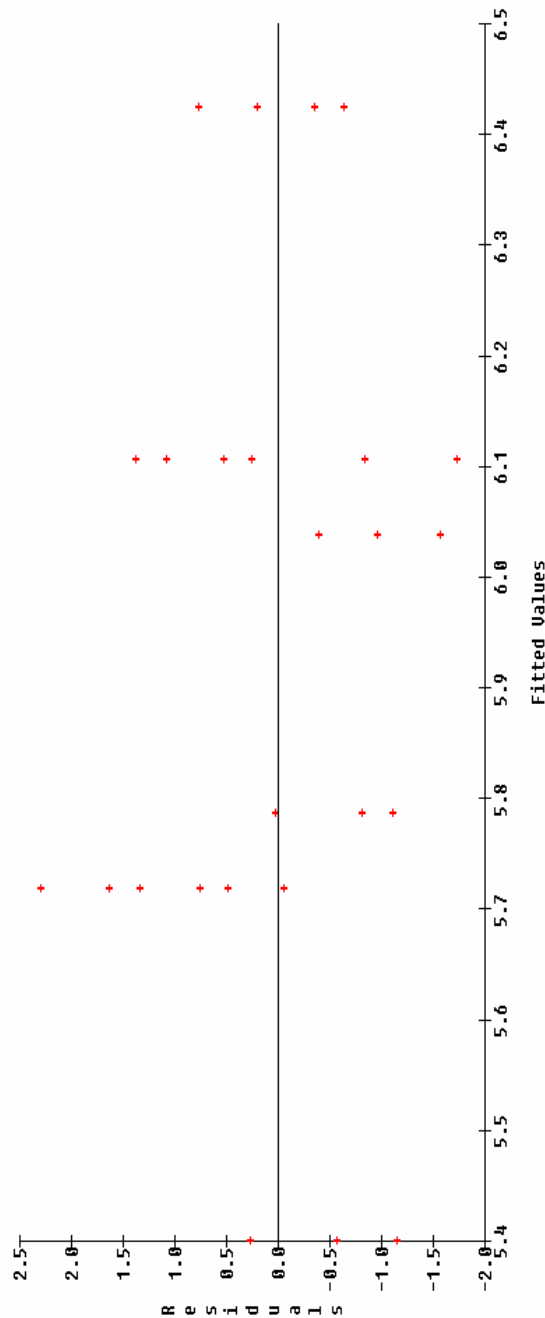
Least Squares Components ANOVA, Response SBPG Model TMPSUBPGS				
Source	df	Sum Sq.	Mean Sq.	F-Ratio Signif. Transformed Term
1 Constant	1	1049		
2 ~LST	1	1.121333	1.121333	7.87 0.0092 ((LST-3.0105e-01)/3.0105
3 ~T*LSR	1	1.625625	1.625625	11.41 0.0022 ((T-1.08e+03)/3e+01)*(LS
4 Residual	27	3.847708	0.142508	
~ indicates factors are transformed. R-sq. = 0.4165				
Type 3 sum of squares. R-sq-adj. = 0.3733				

A-7.—Subsolvus plus supersolvus mean grain size regression results.

Case Order Graph of Residuals of SBPG  
Using Studentized Residuals in Model TMPSUBPGS

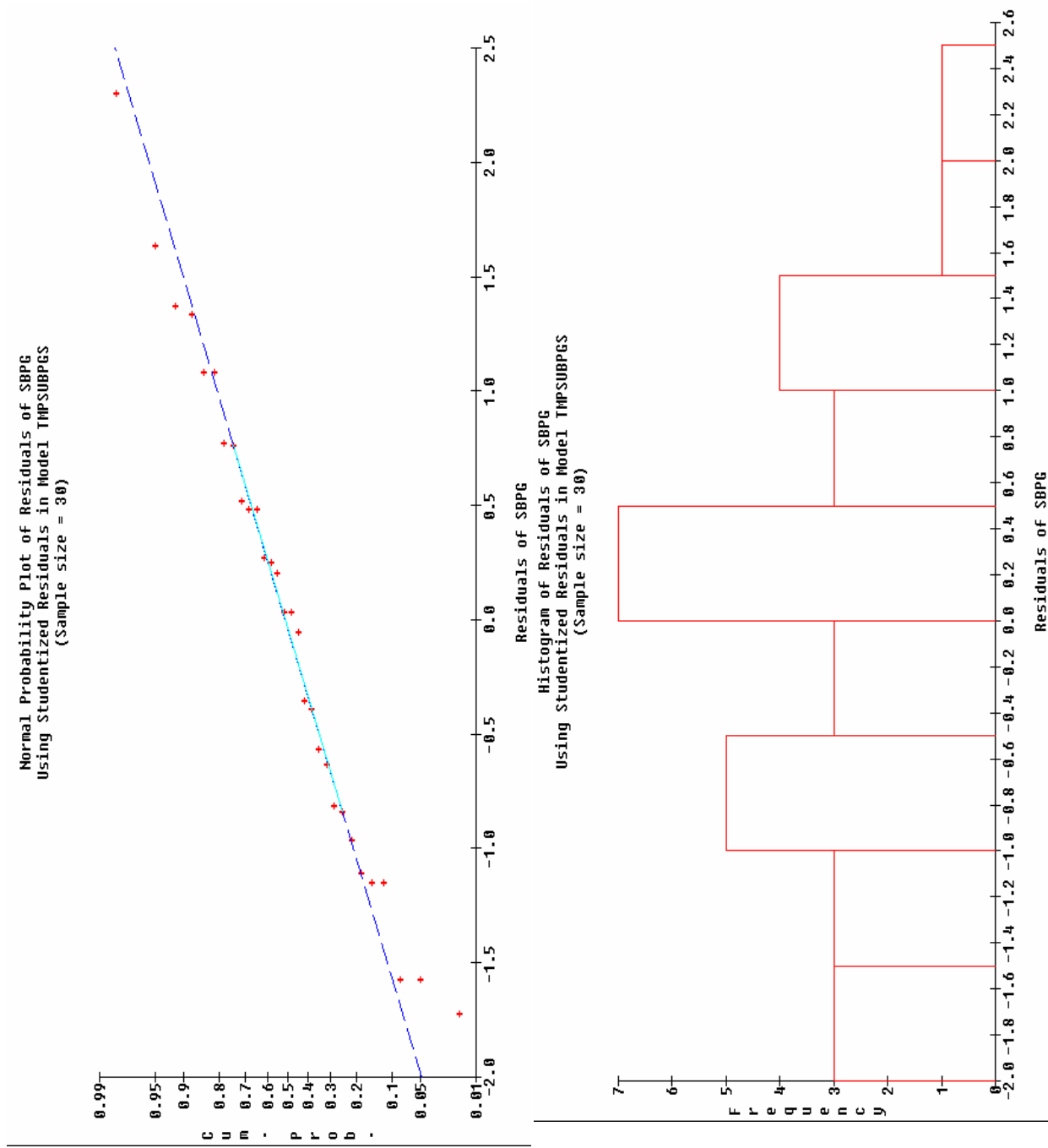


Residuals of SBPG vs Fitted Values  
Using Studentized Residuals in Model TMPSUBPGS



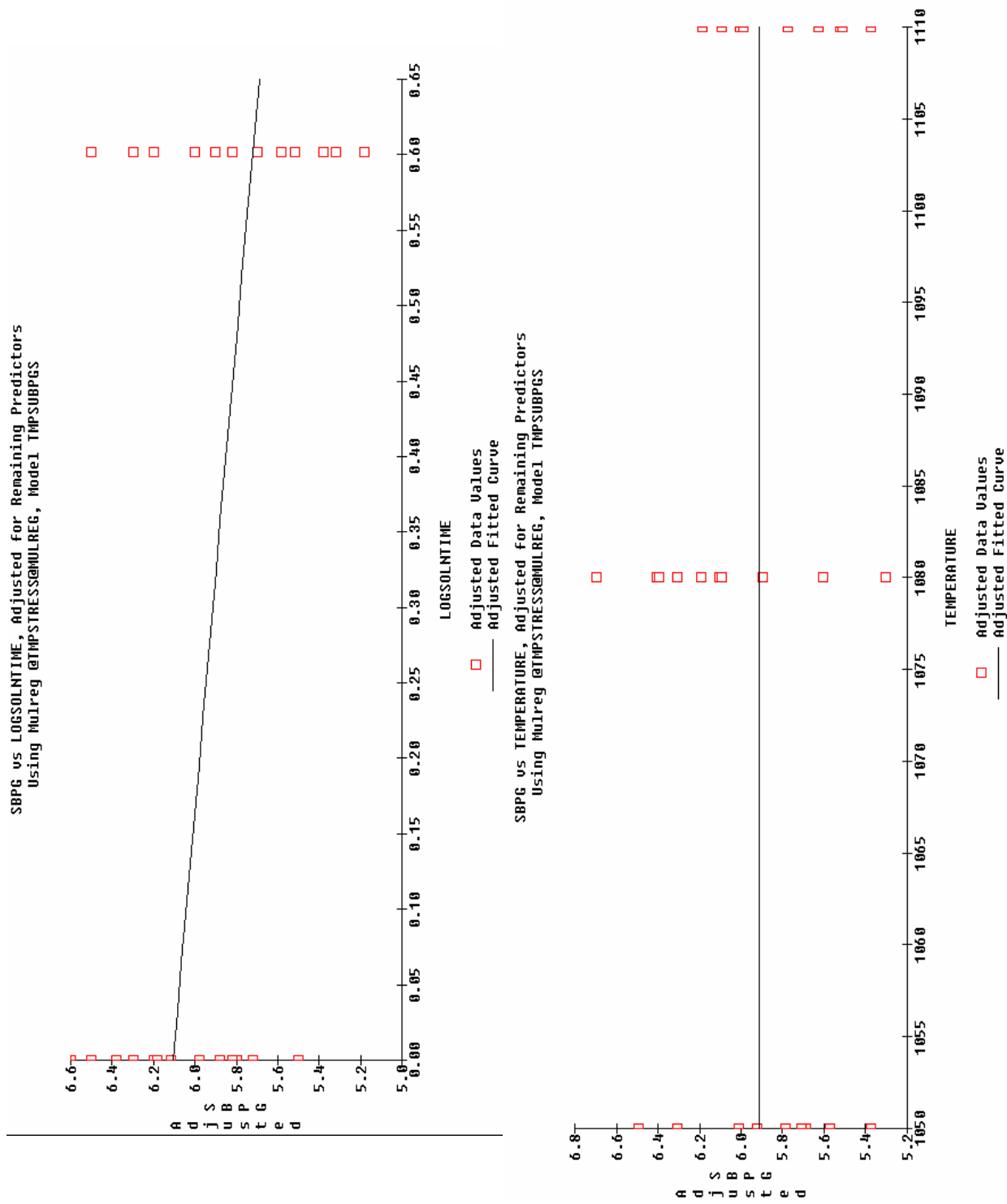
A-7.—Subsolvus plus supersolvus mean grain size regression results.



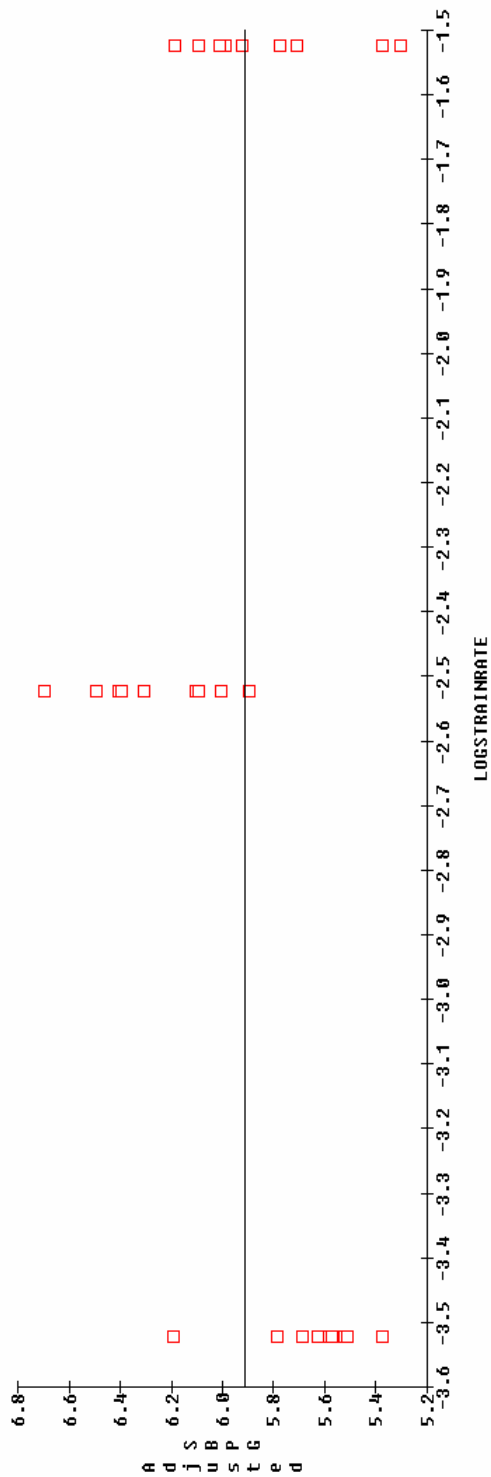


A-7.—Subsolvus plus supersolvus mean grain size regression results.

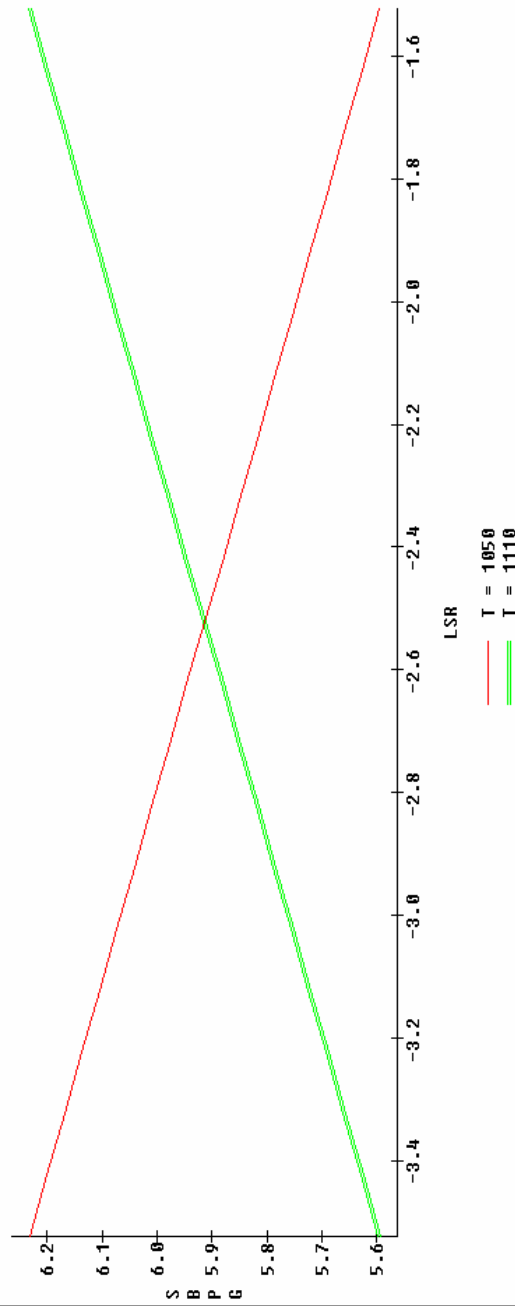
SBPG vs LOGSOLTIME, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@MULREG, Model TMPSUBPGS



SBPG vs LOGSTRAINRATE, Adjusted for Remaining Predictors  
Using MuIreg @TMPSTRESS@MULREG, Model TMPSUBPGS



MuIreg @TMPSTRESS@MULREG, Model TMPSUBPGS  
Interaction Effects of LOGSTRAINRATE with TEMPERATURE  
On Response SBPG

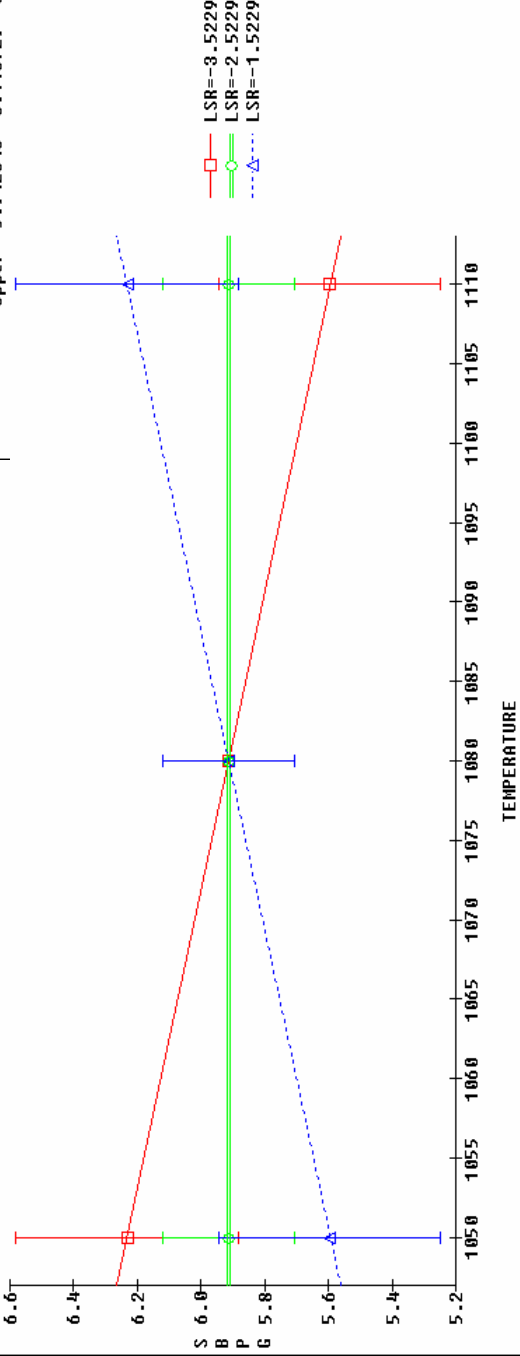


A-7.—Subsolvus plus supersolvus mean grain size regression results.

Predictions and 95% simultaneous confidence intervals  
for mean responses of SBPG using model THPSUBPGS  
LST = 0.30103

LSR		T=1050	T=1080	T=1110
	Lower	5.883818	5.707938	5.246318
-3.5229	Predicted	6.232083	5.913333	5.594583
	Upper	6.580348	6.118729	5.942848
	Lower	5.707938	5.707938	5.707938
-2.5229	Predicted	5.913333	5.913333	5.913333
	Upper	6.118729	6.118729	6.118729
	Lower	5.246318	5.707938	5.883818
-1.5229	Predicted	5.594583	5.913333	6.232083
	Upper	5.942848	6.118729	6.580348

Predictions and 95% simultaneous confidence intervals  
for mean responses of SBPG using model THPSUBPGS  
LST = 0.30103



A-7.—Subsolvus plus supersolvus mean grain size regression results.

## All Terms

Least Squares Coefficients, Response SBPA, Model THPSUBSUPALA

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	1.862915	0.275576			
2 ~T	-0.668075	0.337448			((T-1.08e+03)/3e+01)
3 ~LSR	-0.542333	0.337448			(LSR+2.5229)
4 ~LP	-0.685139	0.337241			((LP-4.5155e-01)/4.5155e
5 ~LST	-0.112213	0.275595			((LST-3.0105e-01)/3.0105
6 ~T*LSR	-0.500000	0.377248	-1.33	0.2008	((T-1.08e+03)/3e+01)*(LS
7 ~T*LP	-0.613291	0.377127	-1.63	0.1204	((T-1.08e+03)/3e+01)*(L
8 ~T*LST	-0.225015	0.337443	-0.67	0.5129	((T-1.08e+03)/3e+01)*(L
9 ~LSR*LP	-0.679285	0.377127	-1.80	0.0876	(LSR+2.5229)*((LP-4.5155
10 ~LSR*LST	-0.300020	0.337443	-0.89	0.3851	(LSR+2.5229)*((LST-3.010
11 ~LP*LST	-0.236561	0.337263	-0.70	0.4915	((LP-4.5155e-01)/4.5155e
No. cases = 30 R-sq. = 0.5170 RMS Error = 1.509					
Resid. df = 19 R-sq-adj. = 0.2628 Cond. No. = 1.023					
~ Indicates factors are transformed.					

## FORWARD AND REVERSE STEPWISE SELECTION

Mu1reg @TMPSTRESS@MULREG, Model THPSUBSUPALA\_COPY, Response SBPA

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.062	
3 LSR	1	0.125	
4 LP	1	0.056	
5 LST	1	0.688	
6 T*LSR	1	0.201	
7 T*LP	1	0.120	
8 T*LST	1	0.513	
9 LSR*LP	1	0.088	
10 LSR*LST	1	0.385	
11 LP*LST	1	0.492	

No. cases = 30 R-sq. = 0.5170 R-sq-adj. = 0.2628  
Resid. df = 19 R-sq-adj. = 0.2628  
Obey Hierarchy: no

Mu1reg @TMPSTRESS@MULREG, Model THPSUBSUPALA\_COPY, Response SBPA

Term	df	P-Remove	P-Enter
1 1	1	0.000	
2 T	1	0.053	
3 LSR	1	0.111	
4 LP	1	0.047	
5 LST	1		0.672
6 T*LSR	1		0.178
7 T*LP	1	0.107	
8 T*LST	1		0.504
9 LSR*LP	1	0.076	
10 LSR*LST	1		0.371
11 LP*LST	1		0.476

No. cases = 30 R-sq. = 0.4239 R-sq-adj. = 0.3039  
Resid. df = 24 R-sq-adj. = 0.3039  
Obey Hierarchy: no

A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

# MODEL TMPSUBSUPALA

Least Squares Coefficients, Response SBPA, Model TMPSUBSUPALA

Term	Coeff.	Std. Error	T-value	Signif.	Transformed Term
1 1	1.862922	0.267791	6.96	0.0001	
2 ~T	-0.668060	0.327915	-2.04	0.0528	((T-1.08e+03)/3e+01)
3 ~LSR	-0.542313	0.327915	-1.65	0.1112	(LSR+2.5229)
4 ~LP	-0.685123	0.327714	-2.09	0.0473	((LP-4.5155e-01)/4.5155e
5 ~T*LP	-0.613291	0.366473	-1.67	0.1072	((T-1.08e+03)/3e+01)*((L
6 ~LSR*LP	-0.679285	0.366473	-1.85	0.0761	(LSR+2.5229)*((LP-4.5155

No. cases = 30      R-sq. = 0.4239      RMS Error = 1.466  
 Resid. df = 24      R-sq-adj. = 0.3039      Cond. No. = 1.023  
 ~ indicates factors are transformed.

## ANOVA

Least Squares Summary ANOVA, Response SBPA Model TMPSUBSUPALA

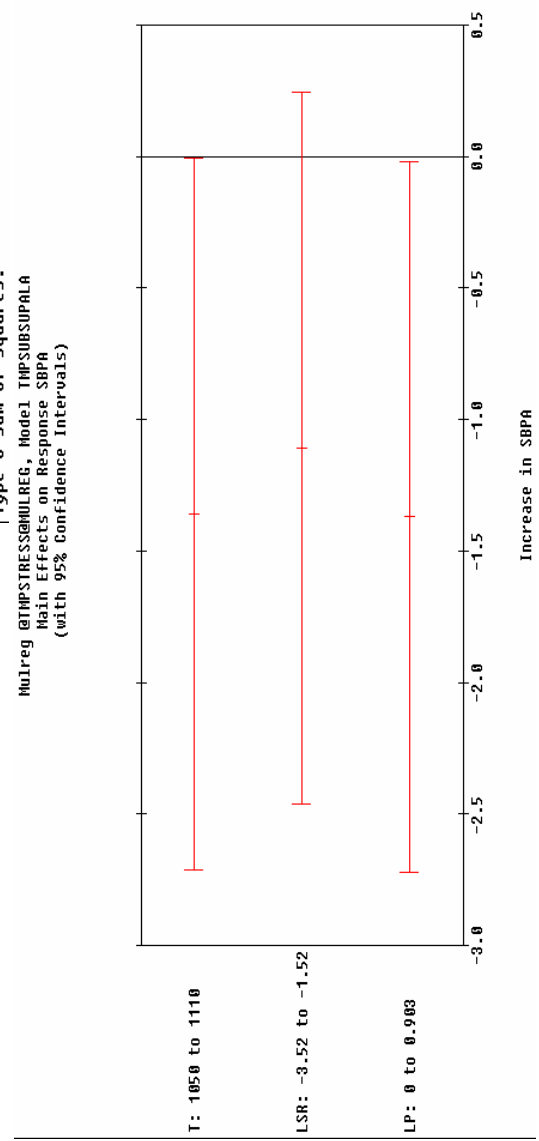
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.
1 Total(Corr.)	29	89.57500			
2 Regression	5	37.96983	7.59397	3.53	0.0156
3 Linear	3	24.20366	8.06789	3.75	0.0243
4 Non-linear	2	13.40944	6.70472	3.12	0.0625
5 Residual	24	51.60517	2.15022		

R-sq. = 0.4239  
 R-sq-adj. = 0.3039

Least Squares Components ANOVA, Response SBPA Model TMPSUBSUPALA

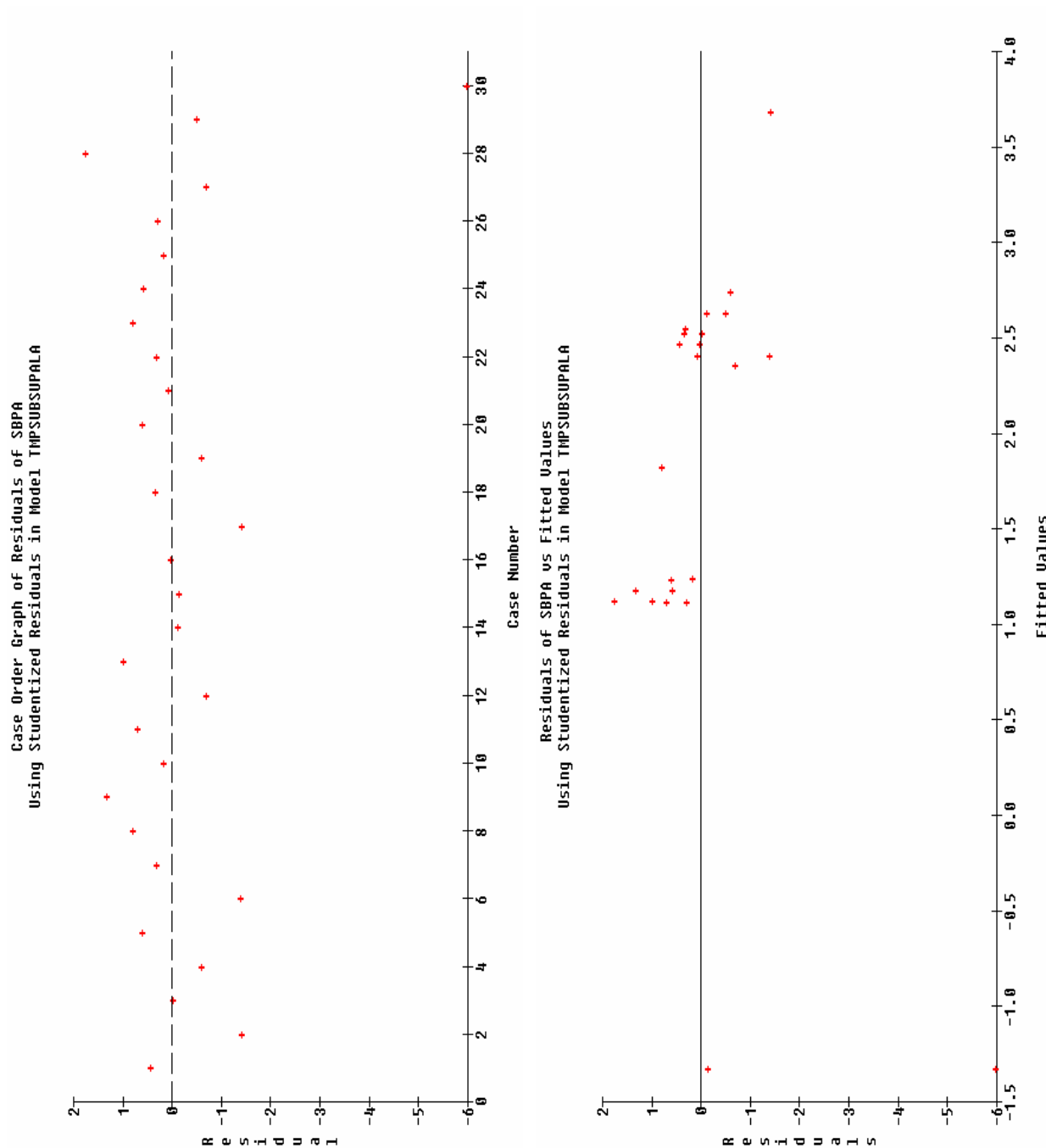
Source	df	Sum Sq.	Mean Sq.	F-Ratio	Signif.	Transformed Term
1 Constant	1	104.05889				
2 ~T	1	8.92465	8.92465	4.15	0.0528	((T-1.08e+03)/3e+01)
3 ~LSR	1	5.88112	5.88112	2.73	0.1112	(LSR+2.5229)
4 ~LP	1	9.39789	9.39789	4.37	0.0473	((LP-4.5155e-01)/4.5155e
5 ~T*LP	1	6.02186	6.02186	2.80	0.1072	((T-1.08e+03)/3e+01)*((L
6 ~LSR*LP	1	7.38757	7.38757	3.44	0.0761	(LSR+2.5229)*((LP-4.5155
7 Residual	24	51.60517	2.15022			

~ indicates factors are transformed. R-sq. = 0.4239  
 R-sq-adj. = 0.3039  
 Type 3 sum of squares.

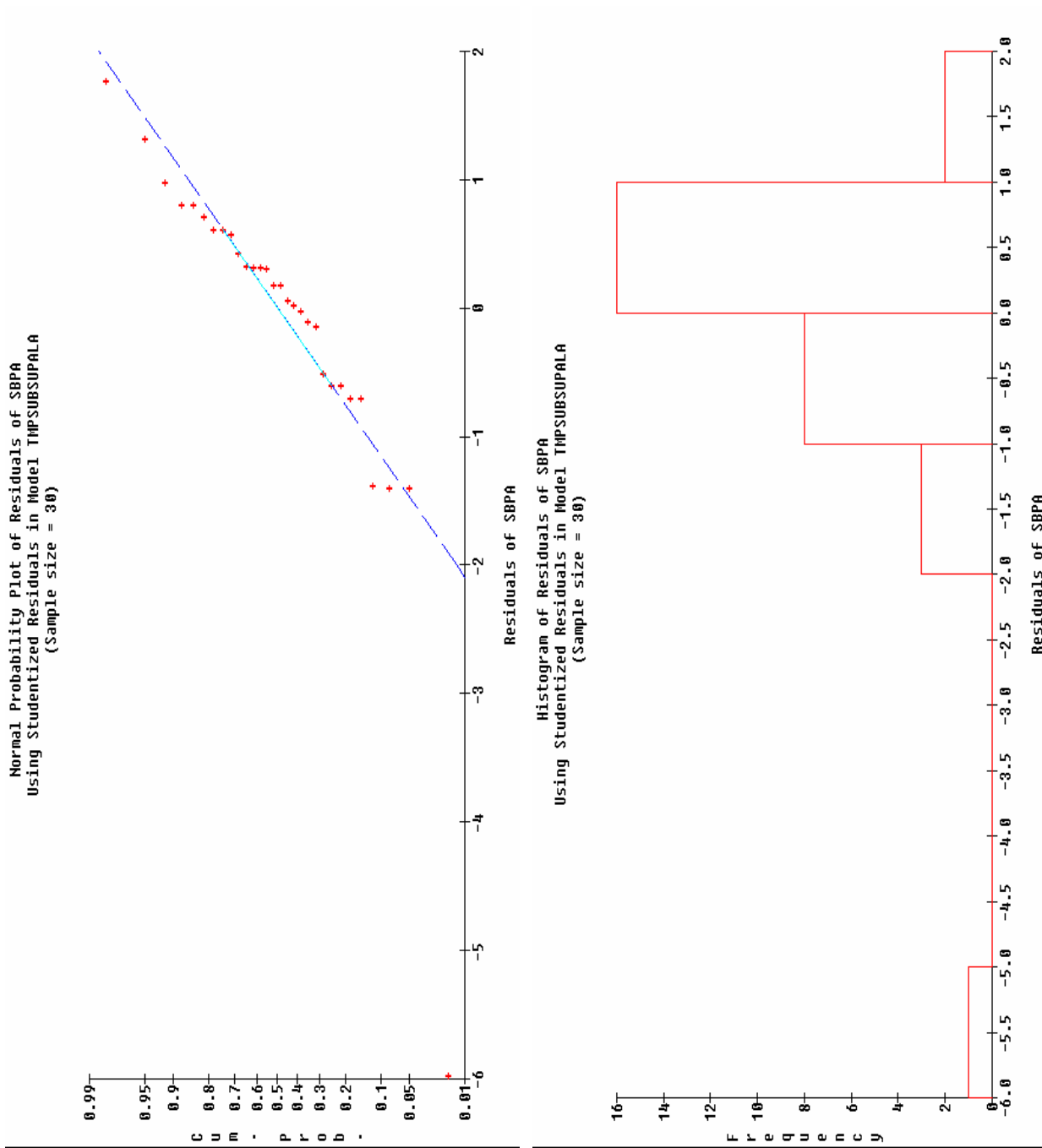


A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

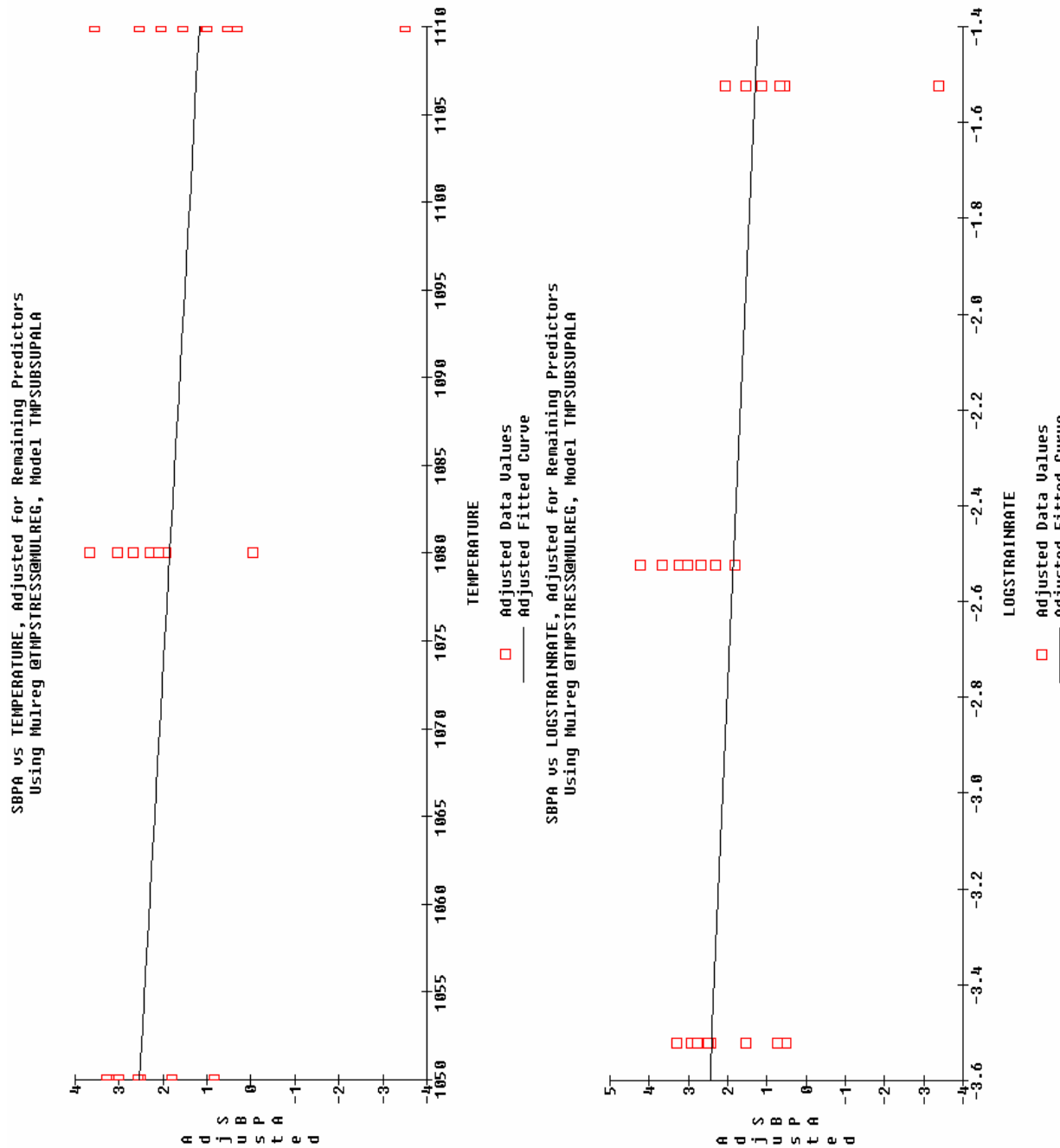




A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

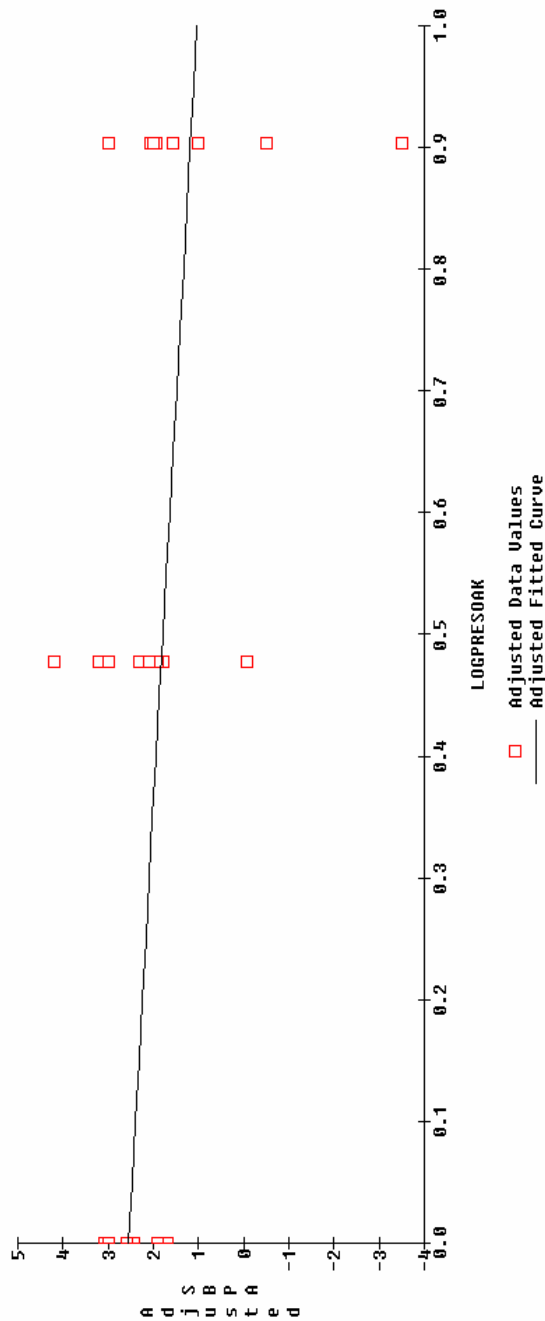


A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

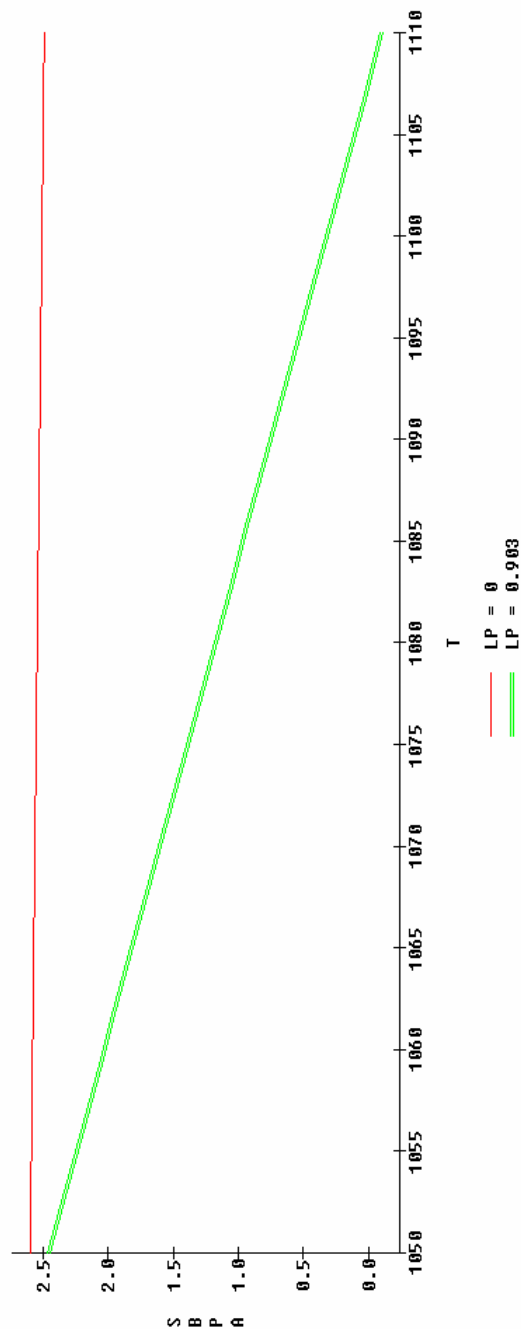


A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

SBPA vs LOGPRESOAK, Adjusted for Remaining Predictors  
Using Mulreg @TMPSTRESS@HULREG, Model TMPSUBSUPALA

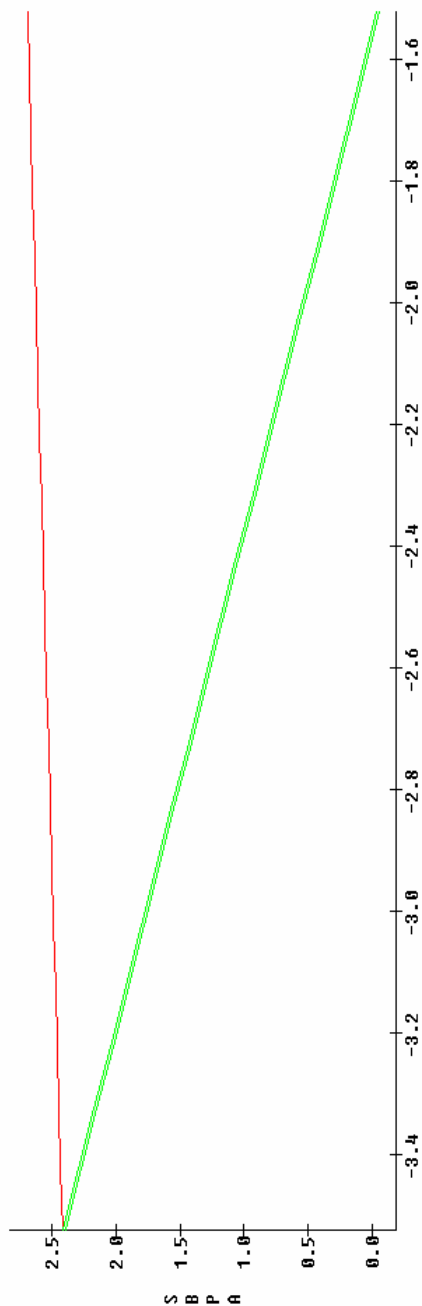


Mulreg @TMPSTRESS@HULREG, Model TMPSUBSUPALA  
Interaction Effects of TEMPERATURE with LOGPRESOAK  
On Response SBPA



A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

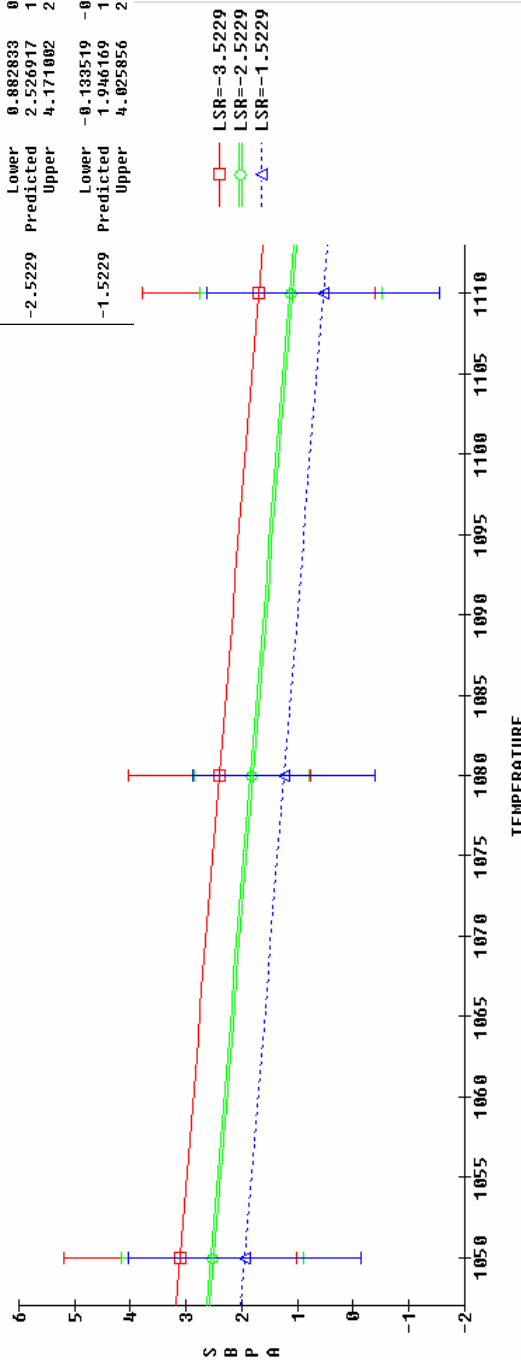
Mulreg @TMPSTRESS@MULREG, Model TMPSUBSUPALA  
Interaction Effects of LOGSTRAINRATE with LOGPRESOAK  
On Response SBPA



Predictions and 95% simultaneous confidence intervals  
for mean responses of SBPA using model TMPSUBSUPALA  
LP = 0.4771

LSR	T=1050	T=1080	T=1110
	Lower	Lower	Lower
-3.5229	Predicted	Predicted	Predicted
	Upper	Upper	Upper
-2.5229	Predicted	Predicted	Predicted
	Lower	Lower	Lower
-1.5229	Predicted	Predicted	Predicted
	Upper	Upper	Upper

Predictions and 95% simultaneous confidence intervals  
for mean responses of SBPA using model TMPSUBSUPALA  
LP = 0.4771



A-8.—Subsolvus plus supersolvus as-large-as grain size regression results.

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13. ABSTRACT (Maximum 200 words) The powder metallurgy disk alloy LSHR was designed with a relatively low $\gamma'$ precipitate solvus temperature and high refractory element content to allow versatile heat treatment processing combined with high tensile, creep and fatigue properties. Grain size can be chiefly controlled through proper selection of solution heat treatment temperatures relative to the $\gamma'$ precipitate solvus temperature. However, forging process conditions can also significantly influence solution heat treatment-grain size response. Therefore, it is necessary to understand the relationships between forging process conditions and the eventual grain size of solution heat treated material. A series of forging experiments were performed with subsequent subsolvus and supersolvus heat treatments, in search of suitable forging conditions for producing uniform fine grain and coarse grain microstructures. Subsolvus, supersolvus, and combined subsolvus plus supersolvus heat treatments were then applied. Forging and subsequent heat treatment conditions were identified allowing uniform fine and coarse grain microstructures.				
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